

IMAGE PROCESSING AND COMPUTER VISION

UNIT-I: Introduction to Computer Vision and Image Processing (CVIP) — Basics of CVIP, History of CVIP, Evolution of CVIP, CV Models
component labeling, Hierarchal segmentation – Spatial clustering, Split and Merge, Rule-based Segmentation, Motion-based segmentation(70 to 89) Area Extraction – Concepts, Data-structures, Edge, Line Links and L
transform, Line fitting, Curve fitting (Least-square fitting)(89 to 102)
Region Analysis – Region properties, Extremal points, Spatial moments, Mixed spatial gray-level moments
Facet Model Recognition – Labeling lines, Understanding line drawings, Classification of shapes by labeling of edges, Recognition Perspective Projective geometry, Inverse perspective Projection, Image matching – Intensity matching of 1D signals, Matching of 2D image, Hierarchical image, Projection of 1D signals, Matching of 2D
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image matching - Intensity matching - Intensity matching
Image matching – Intensity matching of 1D signals, Matching of 2D Object Models and Matching – 2D representation, Global vs. Local features(136 to 138) Knowledge Based of the St. Control of the Projection, (129 to 132) Image matching – Intensity matching of 1D signals, Matching of 2D Object Models and Matching – 2D representation, Global vs. Local features(136 to 138)
UNIT-V: 2D representation, Global vs. Local features(136 to 138)
strategies, Information integration — Knowledge representation, Control
Principal compositions, Shape corresponder and other simple object
Machine learning for image shape recognition(145 to 176)

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INTRODUCTION TO COMPUTER VISION AND IMAGE PROCESSING (CVIP) – BASICS OF CVIP, HISTORY OF CVIP, EVOLUTION OF CVIP, CV MODELS

Q.1. Explain the basics of computer vision and image processing (CVIP).

Ans. Computer vision can be defined as a scientific field that extracts information out of digital images. It has been expanded into wide area of field ranging from recording raw data into extraction of image pattern and information interpretation. It has a combination of concepts, techniques and ideas from digital image processing, pattern recognition, artificial intelligence and computer graphics. Most of the tasks in computer vision are related to the process of obtaining information on events or descriptions, from input scenes (digital images) and feature extraction. The methods used to solve problems in computer vision depend on the application domain and the nature of the data being analyzed.

Basically, computer vision is a combination of image processing and pattern recognition. The output of the computer vision process is image understanding. Development of this field is done by adapting the ability of human vision in taking information. Computer vision is the discipline of extracting information from images, as opposed to computer graphics. The development of computer vision is dependent on the computer technology system, whether about image quality improvement or image recognition. There is an overlap with image processing on basic techniques, and some authors use both terms interchangeably. The main purpose of computer vision is to create models and extracts data and information from images, while image processing is about implementing computational transformations for images, such as sharpening, contrast, among others. It also has similar meaning and sometimes overlapping with in human and computer interaction (HCI). Its coverage focus on more broad design, interface and all aspects of technologies related to interaction between human and computer. HCI is then developed as a separate discipline (which is the field of inerdisciplinary science) which discusses the

development including human aspects. Functionally, computer vision and human vision are the same, with the aim of interpreting spatial data i.e. data indexed by more than one dimension. However, computer vision cannot be expected to replicate just like the human eye.

Because of this the computer vision system has limited performance and function compared to human eye. Even though many scholars have proposed wide area of computer vision techniques to replicate human eye, however, in many cases, there are many limitations of the performance of computer vision system. One of the major challenges in their technique is the sensitivity of the parameters, the strength of the algorithm, and the accuracy of the results. It impacts on the complexity of performance evaluation of computer vision systems. Generally, the performance evaluation involves measuring some of the basic behaviours of an algorithm to achieve accuracy, strength, or extensibility to control and monitor system performance. The computer vision at the intersection of multiple scientific fields is shown in fig. 1.1.

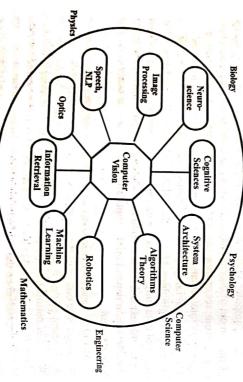


Fig. 1.1 Computer Vision Q.2. What is digital image processing?

Ans. Generally, digital image processing refers to processing of a 2-D picture by a digital computer.

In case of broader context, it implies digital processing of any 2-D data. DIP has a broad spectrum of applications, like radar, sonar, medical processing image transmission and storage for business applications, acoustic image processing, remote sensing via satellites and other spacecrafts and automated inspection of industrial parts.

There are two principal of image processing -

- (i) Improving image quality.
- (ii) Machine perception of visual information.

For performing image processing, first digitize a picture into an image file. Then digital technique is applied to rearrange image puts, to improve the quality of shading or to improve colour separations. An example of enhance the quality of a picture is appeared in fig. 1.2. Similar techniques are employed to analysis galaxies images.

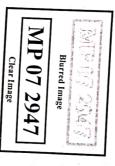


Fig. 1.2 Digital Image Processing

Q.3. Describe history of CVIP.

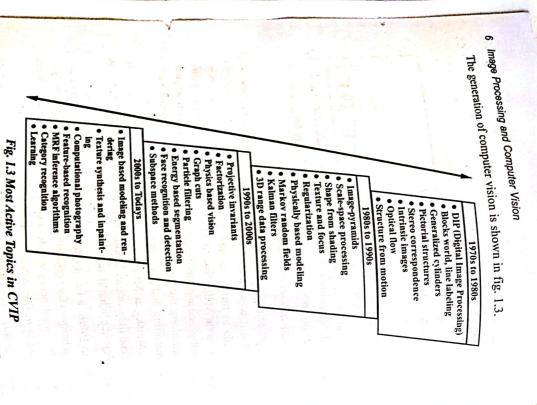
Ans. In between 1960-1970, when computer vision first started out in the early 1970's, it was viewed as the visual perception component of an ambitious agenda to mimic human intelligence and to endow robots with intelligent behaviour. At that time, it was believed by some of the early pioneers of artificial intelligence and robotics that solving the visual input problem would be an easy step along the path of solving more difficult problems such as least evel reasoning and planning. According to one well known story, in Sussman to spend the summer linking a camera to a computer and getting the computer to describe what it saw.

In 1980s to 1990s, a lot of attention was focused on more sophisticated mathematical techniques for performing quantitative image and scene analysis. Image pyramids started being widely used to perform tasks such as image blending and coarse to fine correspondence search.

In 1990s to 2000s, while a lot of the previously mentioned topics continued to be explored, a few of them became significantly more active. A burst of activity in using projective invariants for recognition evolved into a concentrated effort to solve the structure from motion problem.

From 2000s to till today, this past decade has continued to see a deepening interplay between the vision and graphics fields. In particular, many of the topics introduced under the rubric of image-based rendering such as image stitching, light-field capture and rendering etc.

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analysis is the process of distinguishing the objects from the background and quality of a digital image so as to remove defects such as geometric distortion, producing quantitative information, which is subsequently used for decision image data. These include, in an increasing order of complexity such as, binary making. Processing and analysis can be performed on many different types of improper focus, repetitive noise, non-uniform lighting and camera motion. Image images, multi-sensor and multimedia systems, and image sequences and video images, grayscale, color, polarized-light, multi-spectral and hyper-spectral, 3D Image processing involves a series of image operations to enhance the

or operations, but all are potentially available to deal with particular problems and grading. The terms machine vision or computer vision is often used for representation and description, and (iii) high level processing which involves (ii) intermediate level processing which involves image segmentation, image number of steps in sequential order. Not all situations require all of these steps recognition techniques. Hence, the process of making a decision involves a the entire subject, including image processing and analysis and pattern recognition of ROIs (regions of interests) and interpretation for quality sorting processing which includes image acquisition and pre-processing of image The image processing consist three levels of processing, viz. (i) low level

as shown in fig. 1.4. First, image acquisition operations to convert images into Computer vision generally consists of the following five steps or operations

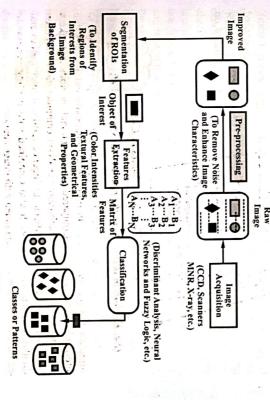


Fig. 1.4 The Operational Steps for CVIP

simulated human visualization. It also combined with lighting systems facilitate image acquisition constitutions. expanded into a branch of artificial intelligence (artificial intelligence) and simulated human visualization.

facilitate image acquisition continued with image analysis.

long time and require complex laboratory analysis, computer vision has expanded into a branch of order. information from an object. Compared to conventional methods that take some time and require conventional methods. That been long time and require conventional methods.

stimulate human visualization in order to automatically extract valuable information from an object.

Ans. Computer vision works by using algorithm and optical sensors ulate human viscoslitudes.

Q.4. Explain in detail about the operational step of CVIP.

rourum, vojove mere shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and fifth, classification or objects, such as size, shape, color and texture; and the size of the objects, sorting operations to identify objects by classifying them into different groups, sorting operations to identify objects by classifying them into different groups, Fourth, object measurement operations to measure the characteristics of operations to partition a digital image into disjoint and non-overlapping regions, with the same dimensions as the original image. Third, image segmentation digital form. Second, pre-processing operations to obtain an improved image digital form. Second, pre-processing operations to obtain an improved image.

Q.5. Explain some examples of application using digital image processing

Ans. Some examples of application using digital image processing are as

released. These electrons flow at high speed to the positively charged anode. cathode and anode. The cathode is heated, causing free electrons to be imaging are generated using X-ray tube, which is a vacuum tube with a extensively in industry and other areas like astronomy. X-ray for medical type of imaging. X-ray is among the oldest sources of EM radiation used for When the electrons strike a nucleus, energy is released in the form of X-ray imaging. The use of X-rays is medical diagnostics, but they also are used follows -(i) In X-ray Imaging - X-ray imaging is perhaps the most familiar

ultra-sonography are some popular pieces of medical equipment based on tomography (SPECT), nuclear magnetic resonance (NMR) spectroscopy and recognition, etc. X-radiation (X-rays), computed tomography scan (CT scan) positron-emission tomography (PET), single-photon emission computed for various purposes, such as image enhancement, image compression, object image processing. (ii) In Health Care - Several medical tools use image processing

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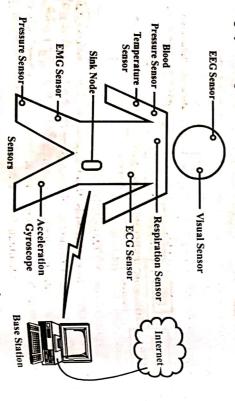


Fig. 1.5 Body Area Sensor Network

techniques in various spectrums, such as hyper spectral imaging, infrared, measurement, etc., are possible with good accuracy through the use of imaging of agriculture. Various paramount tasks such as weed detection, food grading, processing. Irrigated land mapping, determination of vegetation indices, canopy harvest control and fruit picking are done automatically with the help of image (iii) In Agriculture - Image processing, plays a vital role in the field

this information, system predict immediate rainfall intensity, role in weather forecasting, such as prediction of rainfall, hailstorms, flooding. Meteorological radars are widely used to detect rainfall clouds and, based on (iv) In Weather Forecasting - Image processing also plays a crucial

of upcoming movies. For a global media and entertainment company, latent were analyzed using machine learning (ML) algorithms and image processing using image analytics. The colour schemes and objects in the movie posters view extracted over 6000 movie posters from IMDB along with their metadata operations. Image processing-based methods are used to predict the success and video editing tools which are based on image and video processing quality enhancement. In movies, many complex scenes are created with image extensively used in newspapers and magazines for the purpose of picture techniques. (genre, cast, production, ratings, etc.), in order to predict the movies' success (v) In Photography and Film - Retouched and spliced photos are

sharp, lines are not perfectly straight, and curves are not necessarily smooth is still in need of development. This process has many challenges because and recognition also plays a significant role in authenticating the signature of is also being used in the bank customer authentication process. Some banks use 'facial-biometric' to protect sensitive information. Signature verification check image is extracted and used in place of a physical check. Face detection checks electronically using mobile devices or scanners. The data from the handwritten signatures are imprecise in nature, as their corners are not always the customers. However, a robust system used to verify handwritten signatures techniques is rapidly increasing in the field of financial services and banking 'Remote deposit capture' is a banking facility that allows customers to deposi (vi) In Banking and Finance - The use of image processing-based

documents. Identifying document forgery becomes increasingly challenging business documentation. Documents like passports and driving licenses are and civil cases, such as contested wills, financial paper work and professional frequently tampered with in order to be used illegally as identification proof Forensic departments have to identify the authenticity of such suspicious (vii) In Forensics - Tampered documents are widely used in criminal

10 Image Processing and Computer Vision due to the available. The difference of the art computer scan documents are copied latest technology to perfect his art. Computer scan documents are copied latest technology to perfect his art. Computer scan documents are copied latest technology to perfect his art. Computer scan documents are copied latest technology to perfect his art. Computer scan documents are copied latest technology to perfect his art. due to the availability of advanced document-editing tools. The forger uses the medical imaging, insurance claims and journalism. remarkable role in remarkable ro from one documents, it is also gaining popularity in images. Imagery has a confined to documents, it is also gaining popularity in images. Imagery has a latest technology we remark to make them genuine. Forgery is not only from one document to another to make them genuine. Forgery is not only from one documents it is also gaining popularity in images. Images. confined to documents, such as forensic investigation, criminal remarkable role in various areas, intelligence systems, sports, legal servicemental remarkable role in various areas, intelligence systems, sports, legal servicemental remarkable role in various areas, intelligence systems, sports, legal servicemental remarkable role in various areas, such as forensic investigation, criminal remarkable role in various areas, such as forensic investigation, criminal remarkable role in various areas, such as forensic investigation, criminal remarkable role in various areas, such as forensic investigation, criminal remarkable role in various areas, such as forensic investigation, criminal remarkable role in various areas, intelligence systems, sports, legal servicemental remarkable role in various areas, intelligence systems, sports, legal servicemental remarkable role in various areas, intelligence systems, sports, legal servicemental remarkable role in various areas, intelligence systems, sports, legal servicemental remarkable remarkable role in various areas are sports, legal servicemental remarkable remarkab

alers 101 paruvum. analyze peoples' movements and activities. Several banks employed in order to analyze peoples image processing-based video recogninon vi numericale pehaviour, video surveillance systems are being alerts for particularly undesirable behaviour, wideo surveillance systems are being alerts for particularly undesirable behaviour, video surveillance systems are being alerts for particularly undesirable behaviour, video surveillance systems are being (viii) in security. Biometric verification techniques are used for of authenticity and confidentiality. Biometric verification techniques are used for of authennous and on their behaviours or characteristics To create recognition of humans based on their behaviour video surveillance system-(viii) In Security - Biometric verification systems provide a high level

systems in order to detect undesired activities. and other departments are using these image processing-based video surveillance

Q.6. Explain some applications of computer vision.

successful applications of computer vision to recognize characters and Ans. Applications of computer vision are as follows -(i) Optical Character Recognition - This is, one of the oldest

numbers. This can be used to read zipcodes, or license plates. (ii) Mobile Visual Search - With computer vision, we can do a

search on Google using an image as the query.

motors compete to be the first to build a fully autonomous car. applications of computer vision. Companies like Tesla, Google or General (iii) Self-driving Cars - Autonomous driving is one of the hottest

products you take and they charge you as you walk out of the store. has no checkout. With computer vision, algorithms detect exactly which (iv) Automatic Checkout - Amazon Go is a new kind of store that

movement in real time and allows players to interact directly with a game through moves. (v) Vision-based Interaction - Microsoft's Kinect captures

multiple companies are competing to provide the best mobile AR platform. Apple's ARKit has some impressive applications. (vi) Augmented Reality - It is also a very hot field right now, and

to billions of photos on google to find the best matches. We can then identify where a photo was taken. For instance, a photo of a landmark can be compared to billions of whoto of a landmark can be compared to billions of whoto of a landmark can be compared to billions of whoto of a landmark can be compared to billions of whoto of a landmark can be compared to billions of whoto of a landmark can be compared to billions of whoto of a landmark can be compared to billions of whoto of a landmark can be compared to billions of whoto of a landmark can be compared to be compared t (vii) Scene Recognition – It is possible to recognize the location hate were to be a possible to recognize the location

the best match and deduce the location of the photo. take better pictures, and focus on the faces, Smile detection can allow (viii) Face Detection - It has been used for multiple years in cameras etter nictures and cameras

> we can also use computer vision for biometrics, using unique iris pattern data, companies like Facebook are able to get very good performance. Finally, recognition is more difficult than face detection, but with the scale of today's recognition or fingerprints. camera to take pictures automatically when the subject is smiling. Face

Q.7. Discuss about the image model in CVIP.

either color at the perceptual level or multispectral at the signal level. Existing associated a scalar quantity called a gray level, or a vector quantity called known image models are the function, the random process, and the ordered and consequently the mathematical language used in the formulation. The well models differ primarily in terms of how the image quantity values are formulated is formed by pixels usually considered as sampled locations. With each pixel is these image models, the emphasis is put on image quantities. The image support have been accepted and are in recurrent use over the last several decades. In Ans. In image processing and computer vision, several image models

set. The image is a function $L_x \times L_y \to G^m$, where $L_x = \{1,...,N_x\}$ and

a binary image n = 1, image processing has roots in data structure, graph n is the maximal quantity and m is the number of image bands. In the case of a collection of random variables $\{X(i,j) | (i,j) \in L_x \times L_y\}$. In this case, the set, discrete mathematics and mathematical morphology are the foundation. the Markov processes are the roots. When the image is modeled as an ordered probability density function, moments, sufficient statistics, time series, and differential geometry are the foundation. An image can also be represented as this case, function theory, functional analysis, differential equations, and the image is modeled as a real function (analog image where $G, L_x, L_y \subset \mathbb{R}$). In theory, language theory, logic, discrete geometry, and so on. If n > 1, usually $L_y = \{1,..., N_y\}, N_x \times N_y$ is the resolution of the image, $G = \{0,1,...,n\}$, where

to retrieve all objects properties at any step of the processing to complete a computational image model in terms of a data structure in which it is possible not well defined. For a given computer vision or image processing task, no not apparent and the association between the support and image quantities is roots in mathematics, the full functionality and role of the image support is as points, lines, surfaces, and time. Although all image models have deep variables (image support) represent geometrical or temporal elements such non-modular and sometimes not easy to reproduce. Our goal is to give a geometrical properties of objects and their precise functionality as part of formal mechanism is given for the integration of physical topological, the image model. Consequently, the resulting computational schemes are Fundamentally, an image is a physical or mathematical quantity where

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given task without overhead operations or drawback on the efficiency of the quantities, the association between quantities and variables that allow to processing. The processing is the formal specification of the image variables, image sense that the image is the formal specification of the image variables, image sense that the image is the formal specification of the image variables, image sense that the image variables in the specification of the image variables, image sense that the image variables in the specification of the image variables, image sense that the image is the formal specification of the image variables, image sense that the image is the formal specification of the image variables, image sense that the image is the formal specification of the image variables, image sense that the image is the formal specification of the image variables, image sense that the image is the formal specification of the image variables, image sense that the image is the formal specification of the image variables. given use minimum and the green as an abstract data structure in the processing. This model can be seen as an abstract data structure in the processing. This model can be seen as an abstract data structure in the extraction, image segmentation, and image enhancement. such as read and write and those that are problem dependent such as feature operations are of two kinds – the operations that are problem independent (e.g. texture). These quantities are scalar, vector or tensor. The allowable color and gray level) or any feature that can be deduced from the radiometry meaningful operations. The attributes are the image support and quantities meaningful operations. pnysical and a collection of used in computer programs is defined by its attributes and a collection of physical and mathematical behaviour. This abstract view of the image as quanumes, and topological properties of objects as well as their capture the geometrical and topological properties of objects as well as their capture the geometrical hehaviour. This abstract view of the income to the capture of the c that are assigned to the image support such as the image radiometry (e.g.,

IMAGE FILTERING, IMAGE REPRESENTATIONS, IMAGE STATISTICS, RECOGNITION METHODOLOGY -CONDITIONING, LABELING, GROUPING, EXTRACTING AND MATCHING

Q.8. Write short note on image filtering.

function of its input thus, its result varies in a non-intuitive manner. is achieved through convolution and Fourier multiplication whereas non-linear There are broadly two types of algorithms - linear and non-linear. Linear filter example, smoothing an image reduces noise, blurred images can be rectified filter cannot be achieved through any of these. Its output is not the linear Ans. Image filtering is done to improve the quality of the image. For

of the input pixels in the image. The neighbourhood pixels are identified through their locations which are relative to the input pixel linear filtering is done through applying the algorithm on the neighbour pixels frequently used filters as it is simplest and fastest. Unlike non-linear filters, the in large amount but the magnitude of noise is low. Linear filters are the most whereas linear low-pass filter is sufficient when the input given contains noise should be selected for any specific purpose. If the image or input given has non-linear filters are the algorithms which are used for filtering. Right filter can be done for noise removal, blur removal, edge detection etc. Linear and less amount of noise but the magnitude is high then non-linear filters are used Filtering of image is an important process done in image processing It on a mid

Q.9. Write short note on spatial filters

filter mask from point to point in an image. At each point (x, y) the response of the filter at that point is calculated using a predefined relationship. directly on the pixels of an image. The process consists simply of moving the Ans. Spatial filtering term is the filtering operations that are performed

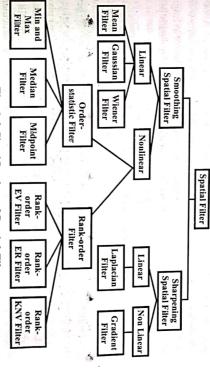


Fig. 1.6 Classification of Spatial Filter

neighbourhood, and they do not explicitly use coefficients in the sum-of filtering operation is based conditionally on the values of the pixels in the sharpening spatial filters. These filters can be either linear or nonlinear. In products manner. Noise reduction can be achieved effectively with a nonlinear in the neighbourhood of the corresponding pixel in the input image. Nonlinear linear filter each pixel value in the output image is a weighted sum of the pixe Spatial filter can be classified into (i) smoothing spatial filters and (ii)

Q.10. Explain in brief about smoothing spatial filters

Blurring is used in preprocessing tasks like removal of small details from an accomplished. By blurring with linear and nonlinear filters, noise reduction can be image prior to object extraction, and bridging of small gaps in lines or curves Ans. Smoothing filters are used for noise reduction and for blurring

spatial filter is the average of the pixels contained in the neighbourhood of the filter mask (i) Smoothing Linear Filters - The output of a smoothing, linear

regions that are small with respect to the size of the filter mask, filters is in the reduction of irrelevant detail in an image. Irrelevant means pixel result from using an insufficient number of intensity levels. A main use of averaging application of this type of process is that the smoothing of false contours which averaging filters have the undesirable side effect that they blur edges. Another noise reduction. Although, sharp intensity transitions characterize edges. So of sharp transitions in intensity levels, the most obvious smoothing application is neighbourhood specified by the filter mask. The results of this process in an value of every pixel in an image by the average of the intensity levels in the image with reduced "sharp" transitions in intensities. Due to random noise consists The concept behind smoothing filters is straightforward. By replacing the

effective in the presence of impulse noise, also called salt and pepper noise of similar size for certain types of random noise. Median filters are particularly capabilities with considerably less blurring as compare to linear smoothing filter a pixel by the median of the intensity values in the neighbourhood of that pixel because of its appearance as white and black dots superimposed on an image Median filters are quite popular because they provide excellent noise-reduction known filter is the median filter, which, as its name implies, replaces the value of pixel with the value determined by the ranking result. In this category, the best image area encompassed by the filter, and then replacing the value of the center spatial filters whose response is based on ordering the pixels contained in the (ii) Order-statistic (Nonlinear) Filters - These filters are nonlinear

Q.11. Discuss the various types of smoothing linear filters.

Ans. The various types of smoothing linear filter are as follows -

input pixel. The following figure illustrates the local effect of the mean filter. pixel by finding the statistical mean of the neighbourhood of the corresponding Mean Filter - The filter computes the value of each output

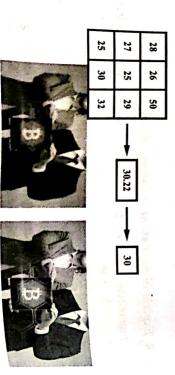


Fig. 1.7 The Effect of Mean Filter

value associated with the pixel at the center of the neighbourhood The statistical mean of the neighbourhood on the left is passed as the output

by Norbert Wiener in the 1930's and 1940's. The Wiener filtering executes an attempting to remove noise from images. It was developed (for 1D applications) optimal in terms of the mean square error. The Wiener filter has two separate additive noise and inverts the blurring simultaneously. The Wiener filtering is optimal tradeoff between inverse filtering and noise smoothing. It removes the the noise with a compression operation (low pass filtering) the deconvolution by inverse filtering (high pass filtering) but also removes parts, an inverse filtering part and a noise smoothing part. It not only performs (ii) Wiener Filter - The Wiener filter is a classic method for











(a) Original Image (b) Image Blurred (c) Image after (d) Image after the Inverse Filter Wiener Filter

Fig. 1.8 Wiener Filter Applied to a Noise Image

same image. Thus, both global statistics (mean variance, etc. of the whole image) are important. Wiener filtering is based on both the global statistics and image) and local statistics (mean, variance, etc. of a small region or sublocal statistics Image statistics vary too much from a region to another even within the

distribution. It is used to remove Gaussian noise and is a realistic model of performs a weighted average of surrounding pixels based on the Gaussian calculating weighted averages in a filter box. The Gaussian smoothing operator defocused lens (iii) Gaussian Filter - A Gaussian filters smoothens an image by





Fig. 1.9 Gaussian Smoothing

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different levels of detail within an image Gaussian Blur is distinct from other blurs in that it has a well-defined effect on Gaussian Blurs produce a very pure smoothing effect without side effects. A This removes fine image detail and noise leaving only larger scale changes.

Q.12. Describe various types of nonlinear smoothing filters

Ans. The various types of nonlinear smoothing filters are as follows –

center pixel with the value determined by the ranking result. the image area encompassed by the filter, and then replacing the value of the filters whose response is based on ordering (ranking) the pixels contained in (i) Order-statistic Filter - Order-statistics filters are nonlinear spatia

range spread of its neighbours, it is passed on to the output image unchanged region around the pixel. If the intensity of the central pixel lies within the intensity minimum and maximum intensity values of all the pixels within a windowed of pixel values. This is accomplished by a procedure which first finds the value within the pixel values and maximum filter selects the largest value within (a) Min and Max Filter - The minimum filter selects the smallest

Table 1.1 The Example and Description of Max, Min and Midpoint

0 219	150	22 48	Example Image
Midpoint Filter	Min Filter	Max Filter	Filter Type
The center pixel would be changed from 77 to 109 as it is the midpoint between the brightest pixel 219 and the darkest pixel 0 within the current window.	The center pixel would be changed from 77 to 0 as it is the darkest pixel within the current window.	The center pixel would be changed from 77 to 219 as it is the brightest pixel within the current window.	Description

the minimum value, it is set equal to the minimum value. it is set equal to the maximum value; if the central pixel intensity is less than However, if the central pixel intensity is greater than the maximum value,

pixel is replaced by that pixel which is mid-way in ranking. the pixels in the neighbourhood are ranked by intensity level and the center used to remove the impulsive noise from an image. With the median filter, all (b) Median Filter – Median filter is the nonlinear filter more



(a) Noise Image



by using Median Filter

(with respect to intensity) within the specified window size. replacing each pixel with the average of the highest pixel and the lowest pixel (c) Midpoint Filter - The midpoint filter blurs the image by

Midpoint = (Darkest + Lightest)/2

- averaging of the selected pixels. There are three rank-order filters Rank-order the further correction of the central pixel within the window using some kind of EV filter, Rank-order ER filter and Rank-order KNV filter. interval from the limited number of pixels belonging to the filtering window with the filtering window. Rank-order filters are adaptive to the signal local statistics nonlinear filters, which are based on the correction of the local histogram within Image processing with rank-order filters is reduced to the creation of the filtering (ii) Rank-order Filters - Rank-order filters are spatial-domain
- most important property of this filter is that it smoothens the brightness jumps greater than EV. The EV filter is highly effective for reduction of white noise less than or equal to EV (which is a main control parameter for this filter). The window whose absolute difference from the central pixel brightness value is composed of all brightness values belonging to the pixels within the filtering which are less than or equal to EV, and preserves the brightness jumps that are (a) Rank-order EV Filter - A filtering interval for this filter is
- types with unknown statistics, and for the reduction of any complicated noise composed of all brightness values belonging to the pixels within the filtering containing an impulsive component. for this filter. This filter is effective for the reduction of complicated noise the variational series is less than or equal to ER, which is main control parameter window whose rank difference from the central pixel brightness value rank in (b) Rank-order ER Filter – A filtering interval for this filter is

objects whose area is less than the number of square pixels that are equal to KNV, and preserve the objects whose area is greater than KNV. the central pixel brightness value (KNV is a main control parameter for this the filtering window) which is equal to KNV and whose values are closest to is composed of the number of brightness values (belonging to the pixels within filter). The most important property of this filter is that it smoothens only the (c) Rank-order KNV Filter – A filtering interval for this filter

Q.13. Discuss about median filtering.

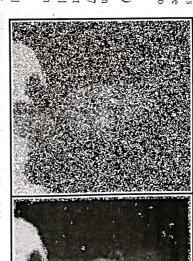
(R.GP.V., June 2017)

value in the processed image following tasks are performed by the median extended this concept to two dimensional images. To determine each pixel which utilizing the median of the neighbourhood, to smoothen the image. Prat as median filters. Turkey introduces the concept of a median filter in 1997 Ans. The best known filter in order statistical nonlinear filters are known

which are identified by the mask are sorted in descending or ascending order For the processed image, sorted median value is calculated and In the original image, all pixels in the neighbourhood of the pixel

neighbours, and whose area is less than m²/2 (one half the filter area), here the tilter eliminates isolated clusters of pixels which are light or dark with their points with distinct intensity levels to be their neighbours. An $m \times m$ median which results in a median of 20. Hence, the median filters are used to force 16, 17, 18, 19, 20, 20, 20, 20, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 100). 22, 23, 24, 26, 27, 28, 29, 30). These values are sorted as (10, 12, 13, 14, 15, has values (10, 20, 20, 20, 15, 20, 20, 25, 100, 12, 13, 14, 16, 17, 18, 19, 21, neighbourhood are the same. For instance, assume that a 5×5 neighbourhood 5 neighbourhood. All equal values are grouped, when several values in a corresponding pixel in the filtered image. For instance, the median is the 5th largest value in a 3 × 3 neighbourhood and it is the 13th largest value in a 5 × the neighbourhood than find their median, and finally, assign that value to the set are equal or less than to ξ and half are equal or greater than to ξ . For performing median filtering at a point in an image, first sort the pixel values in on an image. The median ξ of a set of values is such that half the values in the pepper noise because of its appearance as black and white dots superimposed noise, median filters are specially effective they are also known as salt-andas compared to similar size linear smoothing filters. In the presence of impulse have very good noise-reduction capabilities with considerably, minimum blurring neighbourhood of that pixel. For certain types of random noise, median filters Median filter replaces the pixel value by the intensity median values in the and y(k) the relation is given below -

Larger clusters will be affected considerably less. word eliminated implies that forced to the median intensity of the neighbours





Q.14. Write some properties of median filter.

Ans. There are several properties of median filter as follows -

half the number of pixels in the window, median filter performance is not good (i) When the number of noise pixels in the window is larger than or (ii) Median filter is a non linear filter. Hence for two functions x(k)

 $median\{x(k) + y(k)\} \neq median\{x(k)\} + median\{y(k)\}$

for eliminating isolated lines or pixels. (iii) While preserving spatial resolutions, median filter can be used

Q.15. Explain in brief about sharpening spatial filters

and medical imaging to industrial inspection and autonomous guidance in military discontinuities and deemphasizes areas with slowly varying intensities. operator is applied. Hence, image differentiation enhances edges and other to the degree of intensity discontinuity of the image at the point at which the defining and implementing operators for sharpening by digital differentiation. integration. This, in fact, is the condition, and deals with various ways of accomplished by spatial differentiation due to averaging is analogous to averaging in a neighbourhood. It is logical to conclude that sharpening can be systems. Image blurring could be accomplished in the spatial domain by pixel image sharpening vary and include applications ranging from electronic printing Basically, the strength of the response of a derivative operator is proportional Ans. The sharpening is used to highlight transitions in intensity. Uses of

areas of constant intensity, at the onset and end of discontinuities, and alon intensity ramps. Such discontinuities can be employed to model noise points

that change can occur is between adjacent pixels. possible intensity change also is finite, and the shortest distance over which spanned by the coordinates Since we are dealing with digital quantities whose values are finite, the maximum integers. The real plane part or ramp, must be nonzero (iii) must be zero along ramps of constant slope in which x and y are (i) in constant area, must be zero (ii) at the onset and end of an intensity ster row. Normally, the value of the image is indicated f(x, y), at any coordinates (x, y) must be nonzero along ramps. Similarly, any definition of a second derivative Here, the notation (0, 1) is employed to signify the second sample along the first intensity (ii) at the onset of an intensity step or ramp, must be nonzero (iii coordinate value along the first row of the image represented as f(x, y) = f(0, 1) that any definition uses for a first derivative (i) must be zero in areas of constan Thus, the value of the digital image at the origin is f(x, y) = f(0, 0). The next There are multiple methods to define these differences. Although, it is require integer value for these discrete coordinates, for national clarity and convenience.

function f(x) is the difference given below – A fundamental definition of the first-order derivative of a one dimensional

$$\frac{\partial f}{\partial x} = f(x+1) - f(x)$$

is true for the second derivative. does not affect in any way the nature of what we are trying to accomplish with partial derivatives along the two spatial axes. Use of partial derivative Clearly, $\partial U \partial x = dU dx$ if there is only one variable in the function and the same we consider an image function of two variables, f(x, y), at the time of dealing as shown in fig. 1.12. A Here, a partial derivative is used in order to keep the notation same as if ways to represent f(x, y)

which is given below -The second-order derivative of f(x) can be defined as the difference

$$\frac{\partial^2 f}{\partial x^2} = f(x+1) + f(x-1) - 2f(x) \qquad \dots$$

It is easily verified that these two definitions satisfy the cases stated above

Q.16. Discuss about the image representation.

recognition and image understanding. A good representation schema should to a great extent. Image representation is of primary importance for object recognition and image representation is of primary importance for object recognition and image representation is of primary importance. always be determined by the selection of different image representation methods to a great extent Image. stored in the computer. The efficiency of image processing algorithms will Ans. Image representation is the way in which images are described and

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Fig. 1.12

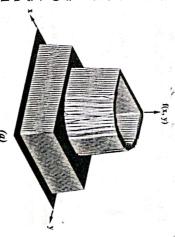
derivatives. In particular, we are interested in these derivatives behaviour honestly and quickly, and make them accessible to higher processing layers. second order derivatives, respectively. We focus attention on one dimensional data structure, a representation should capture the distribution of image features We consider in some detail sharpening filters which are based on first an, be honest, general, brief and helpful for advanced tasks. As a fundamental

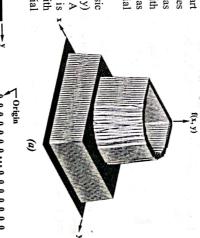
Q.17. Discuss the method of representing digital images.

intensity ramps. For an image. The behaviour of derivatives during transition Ans. Consider a communication is converted into a digital image by using sampling and v is f(u, v). This function is converted into a digital image by using sampling and v is f(u, v). This function is converted into a digital image by using sampling and v is f(u, v). This function is converted into a digital image by using sampling and v is f(u, v). In terms of differences, the derivatives of a digital function are specified has M rows and N columns, where (x, y) are discrete coordinates. We shall use and quantization. Assume that the image f(x, y) is a continuous in 2D array which

spatial (time) domain, with m and n being referred to as coordinates) spatial variables (spatial of an images is known as

plot of the function is two axes finding spatial shown in fig. 1.12 (a) with There are three basic





location and the third axis being the values of fas a function of the two spatial

variables x and y. In fig. 1.12 (b), the representation is more common. It point intensity is proportional to the value of f at that point. There are only indicates f(x, y) as it would seam on a photograph or monitor. Here, each only sections of the image are printed and analyzed as numerical values. Fig. printing the complete array should be bulky and communicate little information, this example, the size of f is 600×600 elements (360000 numbers). Obviously, representation is easily to show the numerical values of f(x, y) as an array. In converts these three values to black, gray, or white respectively. The third to the interval [0, 1]. As shown in fig. 1.12 (b), a monitor or printer easily the image has the value 0, 0.5, or 1 when the intensity (gray level) is generalized three equally spaced intensity values, as shown in fig. 1.12 (b). Each point in However, if developing algorithms, this representation is quite useful when 1.12 (c) represents this concept graphically.

In equation form, the representation of an M × N numerical array can be For processing and algorithm development, numerical arrays are used

$$\mathbf{f}(\mathbf{x}, \mathbf{y}) = \begin{bmatrix} f(0, 0) & f(0, 1) & \cdots & f(0, N-1) \\ f(1, 0) & f(1, 1) & \cdots & f(1, N-1) \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ f(M-1, 0) & f(M-1, 1) & \cdots & f(M-1, N-1) \end{bmatrix} \dots (i)$$

array is known as image element, picture element, pixel or pel. The words image and pixel are employed to represent a digital image and its elements -The right side is a array or matrix of real numbers. Every element of this

$$\begin{array}{c}
a_{0,0} & a_{0,1} & \cdots & a_{0,N-1} \\
A = \begin{bmatrix}
a_{1,0} & a_{1,1} & \cdots & a_{1,N-1} \\
\vdots & \vdots & \vdots & \vdots \\
a_{M-1,0} & a_{M-1,1} & \cdots & a_{M-1,N-1}
\end{bmatrix}$$

Obviously, $a_{ij} = f(x = i, y = j) = f(i, j)$, so equations (i) and (ii) are similar

Q.18. Explain elements of digital image processing system.

purpose image processing system and explain each component in detail. Draw a neat block diagram representing components of a general

used for digital image processing is shown in fig. 1.13. Ans. The basic components consisting a typical general purpose system for digital image program.

below -There are following components of an image processing system as given

- Image sensors Specialized image processing hardware
- Image processing software
- (vi) Image displays
- (vii) Hardcopy Mass storage (viii) Networking

outputs are converting into digital data with the help of digitizer. electrical output proportional to light intensity in a digital video camera. These digital image. The first is a physical device which is sensitive to the energy radiated the output of the physical sensing device into digital form. The sensors create an by the object to image. The second is known as digitizer device which is converted (i) Image Sensors - Image sensing are required two elements to acquire

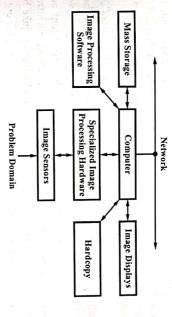


Fig. 1.13 Components of DIP System

arithmetic and logical operations in parallel on whole images. Sometimes, this characteristic is speed. up of the digitizer and hardware. The term hardware which is performed kind of hardware is known as front end subsystem and its most differentiating other primitive operations, like an arithmetic logic unit (ALU). ALU performs (ii) Specialized Image Processing Hardware - It generally made

component in details for off-line image processing operations is appropriate.

(R.G.P.V., Nov. 2019)

7... In this systems, almost any well-equipped personal computer-type machine are employed to obtain a required performance level in dedicated applications. but our interest here is on general purpose digital image processing systems. system. This term is also known as general-purpose computer and can range from personal computer to a super computer. Sometimes designed computers (iii) Computer - The computers are used in digital image processing

which perform specific operations. For the user, a well-designed package also (iv) Image Processing Software - It made up of specialized modules

processing applications, a digital storage falls into three basic principal. system may be a challenge when dealing with thousands of images. For image system may be a challenge when dealing with thousands of images. size of image 100 byte) of storage space if an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage space if is an 8-bit quantity, needs one megabyte (1 MB = 106 byte) of storage in an important storage in a storage in an important storage in a size of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels, where the gray (intensity) level of each pixels are of image 1024×1024 pixels. the image is uncompressed. Providing sufficient storage in an image processing the image is uncompressed. those modules. (v) Mass Storage Capability - It is a must in DIP applications, A

and may be accessed rapidly, usually at video rates 30 frames/second. Frame specialized boards as known as frame buffers, which store one or more images memory is a technique of giving short term storage. Another is through buffers normally are housed in the specialized image processing hardware uni illustrated in fig. 1.13. (a) During processing, short term storage is used. Computer

factor characterizing on-line storage is frequent access to the stored data normally takes the form of magnetic disks or optical-media storage. The main (b) On line storage for relatively fast recall, on line storage

are the usual media for archival applications. require for access. Magnetic tapes and optical disks housed in "juke boxes" Archival storage is characterized by massive storage requirements but infrequent (c) Archival storage, characterized by infrequent access.

in goggles worn by the user and it is required to have stereo displays. these are implemented in the form headgear having two small displays embedded available commercially as element of the computer system. For some cases, applications, seldom are there needed which cannot be met by display cards processing system. Colour television (TV) monitors are used to display the regarding what constitutes a "good" enhancement result. which are an integral element of the computer system. For image display importance because of the significant increase in the use of digital images over image. Monitors are driven by the image outputs and graphics display cards

acceptance as the standard. is employed, images are shown on film transparencies or in a digital means. Internet, that are characterized by significant pictorial content. Image for presentations. For presentation of image, the latter procedure is gaining compression is familiar to most users of computers in the form of image file s employed, images are shown on film transparencies or in a digital medium Internet, that are characterized hy cinnificant situe in uses of the for presentations. For presentations of the same of the same shown on film transparencies or in a digital medium internet, that are characterized hy cinnificant situation of the same shown on film transparencies or in a digital medium internet, that are characterized hy cinnificant situations for presentations. medium of selection for written material. When equipment of image projection cannot be said for transmission canacity. Particularly over the past decade, the same is employed, images are shown as a file. highest possible resolution is provided by the film, but paper is the clear storage technology has improved significant. printers, heat-sensitive devices, film cameras, inkjet units and digital units include cations and or actions. (vii) Hardcopy - It is used for recording images such as laser into smaller regions.

system in use today. The consideration is bandwidth in image transmission due dedicated networks, this typically is not a problem, but communications with is enhancing quickly as a result of optical fiber and other broadband techniques remote sites through the Internet are not always as efficient. Luckily, this problem to the larger amount of data inherent in image processing applications. For (viii) Networking - This is almost a default function in any computer

Q.19. What are the fundamental steps in image processing?

Ans. There are several steps in image processing as follows -

provided an image which is already in digital form. In general, the image acquisition stage includes preprocessing like scaling Image Acquisition - Acquisition could be as easy as being

image so that the result is more appropriate as compared to the original for a for example, a procedure which is quite useful for enhancing X-ray images cannot be the best method for enhancing satellite images taken in the infrared establishes at the outset that enhancement methods are problem oriented. Hence, particular application. The word particular is important here, because it band of the electromagnetic spectrum. (ii) Image Enhancement - It is the process of manipulating an

(vi) Image Displays - Image output is the final stage of the image Enhancement, on the other hand, is based on human subjective preferences the appearance of an image. Although, unlike enhancement, which is subjective, based on mathematical or probabilistic models of image degradation. image restoration is objective, in the sense that restoration methods tend to be (iii) Image Restoration - It is an area which also deals with improving

the Internet. (iv) Color Image Processing - It is an area that has been gaining in

and for pyramidal representation, in which images are subdivided successively degrees of resolution. Particularly, this is used for image data compression (v) Wavelets - These are foundation for showing images in various

extensions like jpg file extension used in the JPEG image compression standard (vi) Compression - It deals with methods for reducing the storage

image components which are useful in the representation and description (vii) Morphological Processing — It deals with tools for extraction and described the representation and described the representatio

Unit - 1 27

or objects. Usually, autonomous segmentation is one of the most difficult tasks in digital image processing. A rugged segmentation method brings tasks in digital image processing. A rugged segmentation method brings process a long way toward successful solution of imaging problems are process a long way toward successful solution of imaging problems are require objects to be identified individually.

require objects to be identified individually. or objects. Usually, autonomous segmentation is one of the most difficult image processing. A rugged segmentation method has a mage processing. (viii) Segmentation – It partition an image into its constituent of the most in Page 1.

interest or are basic for differentiating one class of objects from another with extracting attributes which result in some quantitative information interest are high lighted. Description, also known as feature selection. It deal transforming raw data into a form suitable for subsequent computer processing some applications. Selecting a representation is only part of the solution purposes, the image representation methods are grouped into four categories. For describing the data, a procedure must also be specified so that features texture or skeletal shape. These representations complement each other as a boundary or as a complete region. Boundary representation is appropria Regional representation is appropriate if the focus is on internal properties. if the focus is on external shape characteristics, like corners and inflection The first decision which must be made is whether the data should be should b converting the data to a form suitable for computer processing is necessary the boundary of a region or all the points in the region itself. In either the

to single headed arrows linking the processing modules. arrows between the processing modules and the knowledge base, as oppositions that of pixel based representations. Block based representations can be modules. The difference is made in fig. 1.14 by the use of double acopy same that of pixel based representations. Rlock based representations. the interaction between modules to guiding the operation of each process divided in a set of (rectangular) array size. The number of elements is slightly modules. The difference is to guiding the operation of each process maller than with pixel-based, still only local information is stored which is the interaction between many interactions. The knowledge base comb or an image database containing high-resolution satellite images of a region medical imaging where each pixel has got its own importance connection with change database. Interrelated list of all major possible defects in a materials inspection problemedical imaging where each pixel has got its own improprants. seeking that information. The knowledge base can be quite complex, floring formally big and is used for disniaving the image and is the image known to be located, hence limiting the search that has to be conducted information for each element. Each pixel contains only local seeking that information are easy as detailing regions of an image where the information of interest in an all points addressable display device. The representation includes simple known to be located to the information of interest in the informa in fig. 1.14. In the form of a knowledge database, knowledge about a proble representation to define an image. In digital imaging, a pixel, pel, or picture about the interaction between the knowledge base and the processing moduli domain is coded into an image processing system. This knowledge can be element is a physical point in a raster image, or the smallest addressable element easy as detailing and reseable distance of the smallest addressable element easy as detailing and reseable distance of the smallest addressable element easy as detailing and reseable distance of the smallest addressable element easy as detailing and reseable distance of the smallest addressable element easy as detailing and reseable distance of the smallest addressable element easy as detailing and research addresses and research addresses and research end at the small established element easy as detailing and research addresses and research end at the small established element end end element element element end element eleme objects. So far we have said nothing about the require for prior knowledge processing with the development of procedures for recognition of individu object based on its descriptors. We conclude our coverage of digital image Recognition - It is the process which assigns a label to

Representation & Description Morphological Recognition Segmentation Processing Object Compression Outputs of These Processes are Images Knowledge Base Wavelets and Multi-resolution Processing Image Restoration Image Filtering & Enhancement Acquisition Color Image Processing Image Problem Domain

Fig. 1.14 Representation of Fundamental Steps

Q.20. Classify image representation methods based on level of processing.

viz. pixel based, block based, region based and hierarchical based Ans. Based on the level of processing of images by a machine for different

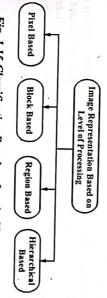


Fig. 1.15 Classification Based on Level of Processing

(i) Pixel Based Representation - This representation is the simples

(ii) Block-based Representation - In this method, the image is

shape. image components which are useful in the representation and description of (vii) Morphological Processing – It deals with tools for extracting

require objects to be identified individually. process a long way toward successful solution of imaging problems which tasks in digital image processing. A rugged segmentation method brings the or objects. Usually, autonomous segmentation is one of the most difficult (viii) Segmentation – It partition an image into its constituent parts

some applications. Selecting a representation is only part of the solution for interest or are basic for differentiating one class of objects from another. with extracting attributes which result in some quantitative information of interest are high lighted. Description, also known as feature selection. It deals transforming raw data into a form suitable for subsequent computer processing as a boundary or as a complete region. Boundary representation is appropriate For describing the data, a procedure must also be specified so that features of texture or skeletal shape. These representations complement each other in Regional representation is appropriate if the focus is on internal properties, like if the focus is on external shape characteristics, like corners and inflections The first decision which must be made is whether the data should be shown converting the data to a form suitable for computer processing is necessary the boundary of a region or all the points in the region itself. In either case, of a segmentation stage, which usually is raw pixel data, constituting either (ix) Representation and Description - It always follow the output

seeking that information. The knowledge base can be quite complex, like an information for each element. The number of elements in the representation is ezsy as detailing regions of an image where the information of interest is in an all points addressable display device. The representation includes simple about the interaction between the knowledge base and the processing modules objects. So far we have said nothing about the require for prior knowledge or arrows between the processing modules and the knowledge base, as opposed or an image database containing high-resolution satellite images of a region in medical imaging where each pixel has got its own importance known to be located, hence limiting the search that has to be conducted in neighbourhood relations between elements. Each pixel contains only local domain is coded into an image processing system. This knowledge can be as element is a physical point in a raster image, or the smallest addressable element processing with the development of procedures for recognition of individual object based on its descriptors. We conclude our coverage of digital image to single headed arrows linking the processing modules. connection with change detection applications. The knowledge base controls interrelated list of all major possible defects in a materials inspection problem normally big and is used for displaying the image and it has applications in in fig. 1.14. In the form of a knowledge database, knowledge about a problem representation to define an image. In digital imaging, a pixel, pel, or picture modules. The difference is made in fig. 1.14 by the use of double headed smaller than with pixel-based, still only local information is stored which is the interaction between modules to guiding the operation of each processing divided in a set of (rectangular) array size. The number of elements is slightly Recognition - It is the process which assigns a label to an

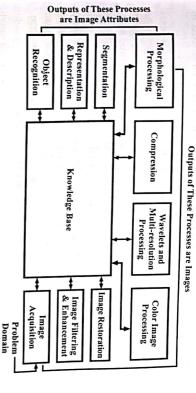


Fig. 1.14 Representation of Fundamental Steps

Q.20. Classify image representation methods based on level of processing

purposes, the image representation methods are grouped into four categories viz. pixel based, block based, region based and hierarchical based Ans. Based on the level of processing of images by a machine for different

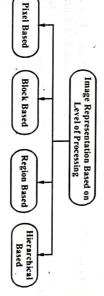


Fig. 1.15 Classification Based on Level of Processing

(i) Pixel Based Representation - This representation is the simplest

same that of pixel based representations. Block based representations can be (ii) Block-based Representation - In this method, the image is

compression, segmentation, extracting different image features, etc. done for both gray-scale and binary images. The representation is used in

representation. The adjacency information between regions orientation subbands are vertical similar and connected pixels. The adjacency graph) or combinatorical orientation subbands are vertical representation. Here the regions are not rectangular and it is formed by grouping representation. Here the regions are not rectangular and it is formed by grouping representation. (iii) Region Based Representation — It is also known as super-pixel space into three different scales

unions of multiple regions have to be considered. similar and vortical map. (V), horizontal (H) and diagonal represented usually as RAG (region-adjacency graph) or combinatorial map. (V), horizontal (H) and diagonal represented usually as for chiect detection and segmentation, but Alex representation is used for object detection and segmentation, but different (D). Visually each subband The representation is used for object detection and segmentation, but different (D). Visually each subband (iv) Hierarchical Representation — The representation uses most likely

image segmentation and filtering, image simplification, etc. unions of regions of region-based representations. The image representation unions of regions of region-based representations. can be usure at the case of th unions of regular varieties. Examples includes min-/max-tree, α -tree, quad by $V_i(x, y)$, $H_i(x, y)$ and $D_i(x, y)$ and

Q.21. Explain in detail about the image statistics.

filter (QMF) pyrama a decomposition (LAHD). These image statistics are collected from image subband is generated by convolving the image, I(x, y), with the low-pass representations that decompose an image using basis functions that are localized in the vertical direction and the high-pass filter in the horizontal direction in both spatial positions and scales, implemented as a multi-scale image as filter (QMF) pyramid decomposition and the local angular harmonic response (FIR) low-pass and Ans. Two multiscale image decompositions, namely, the quadrature mirror 1-D 2n + 1 tap finite impulse

mage analysis. In fig. 1.16 (QMF). One important reason for choosing this decomposition, is that it minimizes nultiscale image decomposition, based on separable quadrature mirror filters liasing from the reconstructed image, making it suitable for the purpose of Quadrature Mirror Filter Pyramid Decomposition - This is a first

subband is normalized into the purpose of display, each sition of a "disc" image. For QMF pyramid decompothe magnitude of a three-scale bands. And in fig. 1.16 (b) zontal and diagonal subthe low pass, vertical hori-2, and from left to right, are bottom, are scales 0, 1 and lecomposition. From top to domain decomposition with three scale QMF pyramid

(a), an idealized frequency

(a) Three Scale QMF Pyramid Decomposition

vertical, horizontal and diagonal energy in an image. The resulting and within each scale, into three subbands at scale i are denoted sition splits the image frequency subbands are the result of con-The QMF pyramid decompo-

QMF Pyramid Decomposition of Disc (b) The Magnitude of a Three-scale

volving the image with a pair of

$$V_1(x, y) = \sum_{m=-N}^{N} h(m) \sum_{n=-N}^{N} I(n)I(x-m, y-n)$$

The horizontal subband is generated by convolving the image with the low-pass filter in the horizontal direction and the high-pass filter in the vertical irection as -

$$H_1(x, y) = \sum_{m=-N}^{N} I(m) \sum_{n=-N}^{N} h(n) I(x-m, y-n)$$

bass filter in both directions as -The diagonal subband is obtained by convolving the image with the high-

$$D_{1}(x, y) = \sum_{m=-N}^{N} h(m) \sum_{n=-N}^{N} h(n) I(x - m, y - n)$$

Finally, convolving the image with the low-pass filter in both directions enerates the residue low-pass subband, as -

$$L_{1}(x, y) = \sum_{m=-N}^{N} l(m) \sum_{n=-N}^{N} l(n) l(x - m, y - n)$$

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The next scale is obtained by first down-sampling the residual low-pass subband L_1 and recursively filtering with I(.) and h(.), as

$$V_{2}(x, y) = \sum_{m=-N}^{N} h(m) \sum_{n=-N}^{N} l(n) L_{1}(\lfloor x/2 \rfloor - m, \lfloor y/2 \rfloor - n)$$

$$H_{2}(x, y) = \sum_{m=-N}^{N} l(m) \sum_{n=-N}^{N} h(n) L_{1}(\lfloor x/2 \rfloor - m, \lfloor y/2 \rfloor - n)$$

$$D_{2}(x, y) = \sum_{m=-N}^{N} h(m) \sum_{n=-N}^{N} h(n) L_{1}(\lfloor x/2 \rfloor - m, \lfloor y/2 \rfloor - n)$$

$$L_{2}(x, y) = \sum_{m=-N}^{N} l(m) \sum_{n=-N}^{N} l(n) L_{1}(\lfloor x/2 \rfloor - m, \lfloor y/2 \rfloor - n)$$

$$L_{2}(x, y) = \sum_{m=-N}^{N} l(m) \sum_{n=-N}^{N} l(n) L_{1}(\lfloor x/2 \rfloor - m, \lfloor y/2 \rfloor - n)$$

by first transforming to RGB colors. Color images using other color systems (e.g., HSV or CMYK) are decomposed bands are denoted as $V_i^c(x,y), H_i^c(x,y)$, and $D_i^c(x,y)$, with $c \in \{r,g,b\}$. performed by decomposing each color channel independently. These sub-Subsequent scales are generated similarly by recursively decomposing the residual low-pass subband. The decomposition of a RGB color image is

the n^{th} -order local angular harmonic decomposition of an image, I(x, y), is decomposition is the local angular harmonic decomposition (LAHD). Formally, Local Angular Harmonic Decomposition - The another image

$$A_{n}(I)(x,y) = \int_{\Gamma} \int_{\theta} I_{(x,y)}(r,\theta) R(r) e^{in\theta} dr d\theta$$

onto a set of angular Fourier basis kernels, $e^{in\theta}$. The function R(r) serves as can be regarded as a local decomposition of image structure by projecting (x, y) in the image plane, and R(r) is an integrable radial function. The LAHD where $I_{(x,y)}(t,\theta)$ is the polar parameterization of image I(x,y) about point

the local windowing function as in the Gabor filters, which localizes the analysis

not possible to reconstruct the image from the LAHD is highly over-complete and it is usually corners and boundaries. Note that the basis in capture image structures such as edges, in fig. 1.18. Both the magnitudes and the phases the first 4-order LAHD of an image is shown $A_n(I)$ (x, y), is a complex-valued 2-D signal. The magnitudes and phases of in both the spatial and frequency domains. The output of the n-th LAHD,



Fig. 1.17 Original Image

Fig. 1.18 The first 4-order LAHD of a Natural Image. The Top Row

Shows the Magnitudes and the Bottom Row Shows the Phase Angles Q.22. Describe the fundamental step in image recognition.

pixel in relation to its neighbours. From this information, image recognition recognized, and, in the case of stereoscopic images, depth information which recognition system is the light intensities of each pixel and the location of a represented by a pixel matrix. The only information available to an image systems must recover information which enables objects to be located and Ans. Image recognition is usually performed on digital images which are

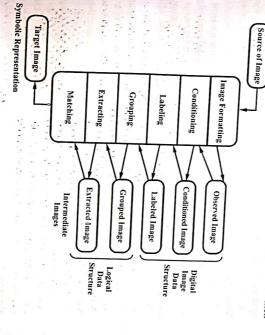


Fig. 1.19 Image Recognition

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informs us of the spatial relationship between objects in a scene. The $vario_{US}$ steps required to transform iconic information into recognition information as shown in fig. 1.19.

 (i) Image Formatting — This formatting means capturing an image by bringing it into a digital form.

(ii) Conditioning – In an image, there are usually features which are uninteresting, either because they were introduced into the image during the digitization process as noise, or because they form part of a background. An observed image is composed of informative patterns modified by uninteresting random variations. Conditioning suppresses, or normalizes, the uninteresting variations in the image, effectively highlighting the interesting parts of the image.

(iii) Labeling – In this step, informative patterns in an image have structure. Patterns are usually composed of adjacent pixels which share some (e.g., an edge). Edge detection techniques focus on identifying continuous adjacent pixels which differ greatly in intensity or colour, because these are adjacent pixels which differ greatly in intensity or colour, because these are likely to mark boundaries, between objects, or an object and the background, edge will have been identified. However, not all of the edges are significant. More complex labeling operations may involve identifying and labeling shape primitive and corner finding.

civ) Grouping – In this step, labeling finds primitive objects, such as edges. Grouping can turn edges into lines by determining that different edges belong to the same spatial event. The first 3 operations represent the image as a digital image data structure (pixel information), however, from the grouping operation the data structure needs also to record the spatial events to which each pixel belongs. This information is stored in a logical data structure.

(v) Extracting – In this step, grouping only records the spatial event(s) to which pixels belong. Feature extraction involves generating a list of properties for each set of pixels in a spatial event. These may include a set's centroid, area, orientation, spatial moments, grey tone moments, circumscribing circle, inscribing circle, etc.

Additionally properties depend on whether the

Additionally properties depend on whether the group is considered a region or an arc. If it is a region, then the number of holes might be useful. In the case of an arc, the average curvature of the arc might be useful to know feature extraction can also describe the topographical relationships between different groups. Do they touch? Does one occlude another? Where are they in relation to each other? etc.

grouped into objects and the relationship between the different objects has been determined, the final step is to recognize the objects in the image. Matching and determining the best match template matching.

MORPHOLOGICAL IMAGE PROCESSING – INTRODUCTION,
DILATION, EROSION, OPENING, CLOSING, HIT-OR-MISS
TRANSFORMATION, MORPHOLOGICAL ALGORITHM
ALGORITHM OPERATIONS ON BINARY IMAGES, MORPHOLOGICAL
THICKENING, REGION GROWING, REGION SHRINKING

Q.23. Discuss briefly about mathematical morphology.

technique at the Ecole des Mines in Paris. For developing this technique, the motivation comes from the structural information collection about the image domain. For extracting image elements, mathematical morphology is a tool. morphology content is fully depended on set theory. In mathematical morphology, there are several useful operators which specified by using set 3-D image domain with their integer elements in a binary image. In a binary description, x and y coordinates are the elements of a 3-D tuple which represents procedures for image. Mathematical morphology, there are several useful operators which specified by using set 3-D image domain with their integer elements in a binary image. In a binary description, x and y coordinates are the elements of a 3-D tuple which represents procedures for image. Mathematical morphology plays a important role in image-segmentation methods with a wide range of applications.

Q.24. Explain about basic set theory.

Ans. Morphology is depend on set theory. Set theory includes various operations such as union, intersection, complement, difference, reflection, translation are given below —

(i) Union $-P \cup Q$ represents union of images P and Q, $P \cup Q$ represents the set whose elements can be elements of P and Q or either element of P or element of Q. The expression is written as

 $P \cup Q = def\{x | x \in P \text{ or } x \in Q\}$

image Q. The expression is written as -P ∩ Q represents the set whose elements are common for both image P and (ii) Intersection - P \(\cap \) Q represents intersection of images P and Q

$$P \cap Q = def\{x \mid x \in P \text{ and } x \in Q\}$$

represents the set which involving everything not in image P. The expression (iii) Complement - Pc represents complement of image P. pc

$$P^{c} = def \{x \mid x \notin P\}$$

image P, which are in image Q. The expression is written as image Q. P.- Q represents the set which involves subtracts all elements of (iv) Difference - P - Q represents difference between image P and

$$P - Q = def\{x \mid x \in P \text{ and } x \notin Q\}$$

(v) Reflection - Q represents reflection of image Q. The expression

$$\hat{Q} = \{\hat{w}|w = -q \text{ for } q \in Q\}$$

expression is -(vi) Translation – $(P)_z$ represents translation of image P. The

$$(P)_z = \{c|c = p + z, \text{ for } p \in P\}$$

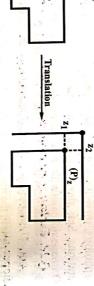


Fig. 1,20 Image P Translation

Q.25. Write a short note on binary morphology.

17.61 P. 15.65

or 1 and image background pixels mean white pixels or off or 0. In binary operations. In a binary image, foreground pixels mean black pixels or ON pattern matching at fast speed. Binary morphology is related with sets year ago we can not be imagined but we are using binary morphology for morphology gives general routines for pattern matching and it is fast, element of binary image. memory efficient. Today, processors are fast, memory is cheap and 10 images, tuple or a 2-dimensional vector of the (x, y)-plane represents each Ans. Binary morphology was used as a principal method because binary Contracted Self-organization

in image processing? Ans. The applications of morphological based operations are as follows -(i) To remove noise in the image (ii) To quantitative description of images (iii) To segment images from the background

Ans. There are several features of morphological operations as follows-Q.27. Give the features of morphological operations. (iv) To enhance the image structure.

algebra for representation and optimization. morphological operations remove information of a greater extent. (ii) Morphological operations uses a well-developed morphological

(i) When the size of the structural element expands, then

very small class of primitive morphological operations. (iii) This is possible to describe digital algorithm in the form of a

geometric content of an image. characteristics, morphological operations give systematic alteration of the (iv) While managing the stability of the important geometric

linear transformations. (v) Non invertibility of morphological operations characterize their

primitive morphological operations. which one may get the expression of morphological filters in form of the (vi) Morphological operations use rigorous representation theorems,

Q.28. Explain some basic morphological operations.

and opening. Ans. The basic operations of morphology are dilation, erosion, closing

the size of the structuring element. The dilation (operator \oplus) is defined as – and broken areas, and connecting areas that are separated by spaces smaller than pixels to the perimeter of each image object (sets their values to 1), filling in holes (i) Dilation - A dilation operation enlarges a region. A dilation adds

dilation (x) =
$$x \oplus s = \bigcup_{a \in s} x_a$$

s is the structuring element (mask), the erosion (operator Θ) is defined as border of larger image objects (sets the pixel value to 0). If x is an image and smaller than the structuring element and removes perimeter pixels from the (ii) Erosion - Erosion is an operator that basically removes objects

erosion
$$(x) = x \Theta s = \bigcap_{a \in S} x_{-a}$$

and x_a would indicate the reverse shift operation. where x_a indicates a basic shift operation in the direction of element 'a' of s

complement operation. According to this rule erosion and dilation are duals with respect to the

(viii) Expansively -

separate objects that are connected in a binary image. Opening generally thin protrusions. Mathematically, the opening function can be described by smoothes the contour of an object, breaks narrow isthmuses, and eliminates (iii) Opening - An opening operation (erosion then dilation) can

opening (x) = dilation (erosion (x))

or, using the operator o,

$$s \oplus (s \ominus x) = s \circ x$$

close up internal holes and gaps in a region and eliminate bays along the boundary by an erosion using the same structuring element. A closing operation can (iv) Closing - The closing operation is defined as dilation followed

closing
$$(x) = erosion (dilation (x))$$

or, using the operator •

$$\mathbf{x} \cdot \mathbf{s} = (\mathbf{x} \oplus \mathbf{s}) \ominus \mathbf{s}$$

Q.29. What is the use of dilation and erosion?

called to be two pixels. element is used to repairing the gaps. The maximum length of the gaps is Ans. Use of Dilation - It is used for bridging gaps. Simple structuring

Structuring element is helped to eliminate irrelevant detail from a binary image. Use of Erosion - It is used for eliminating irrelevant detail from binary image

Q.30. What is the properties of dilation and erosion?

Ans. There are several properties of dilation and erosion as follows -

(ii) The dilation and erosion are translation invariant. Dilation and erosion are not inverses of each other

(III) Increasing -

If

 $s \subset s' \Rightarrow x \ominus s \subset x \ominus s'$ $x \subset x' \Rightarrow x \Theta s \subset x' \Theta s$ $x \oplus s \subset x' \oplus s$ Υ×

If and

 $x \oplus (s \cup s') = (x \oplus s) \cup (x \oplus s')$ $x \ominus (s \cup s') = (x \ominus s) \cap (x \ominus s')$

(iv) Distributivity -

(v) Iteration – $(x \ominus s) \ominus s' = x \ominus (s \oplus s')$ (vi) Local Knowledge - $(x \oplus s) \oplus s' = x \oplus (s \oplus s')$

 $(x \cap z) \ominus s = (x \ominus s) \cap (z \ominus s)$ $x^c \oplus s = (x \ominus s)^c$

(xi) Commutative -

erosion is anti-expansive.

expansive. But the output image of erosion operation is not expanded, so that

The output image of dilation operation is expanded, so that dilation is

 $x \le x \oplus s$ (Dilation)

 $x \ge x \ominus s$

(Erosion)

 $x \oplus s = s \oplus x$ (Erosion)

 $x \ominus s \neq s \ominus x$ (Dilation)

Q.31. What are the properties of open and close operations? Ans. There are several properties of open operation as follows -

(i) x o s is a subset of x.

(ii) When P is a subset of Q, then P o s is a subset of Q o s.

(iii) Open is increase operation. Hence,

xos≤yos

by dilation in open operation. Hence, (iv) The open operation is anti-expansive because erosion is followed

 $X \circ S \leq X$

image xc. (v) The opening of x equivalents to the closing of the complemented $x \circ s \leq (x^c \cdot s)^c$

 $S \circ (S \circ X) = S \circ X$

There are several properties of close operation as follows -

(i) x is a subset of x · s.

(ii) If P is a subset of Q, then P • s is a subset of Q • s.

(iii) Close is increase operation. Hence,

 $x \cdot s \leq y \cdot s$

erosion in close operation. Hence, (iv) The close operation is expansive because dilation is followed by

 $X \leq X \cdot S$

image xc. (v) The closing of x equivalents to the opening of the complemented

 $S \cdot (S \cdot X) = S \cdot X$ $x \cdot s \le (x^c \circ s)^c$

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Q.32. Explain how hit-or-miss transformation is used for finding local (R.G.P.V., June 2015)

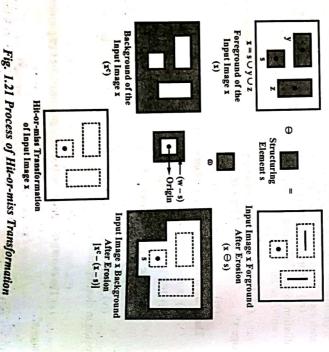
Ans. A transformation which is employed for template matching is known as hit-or-miss transformation. It is a morphological operator which is used for searching structuring element size or local patterns of pixels. Hit-or-miss transformation investigates the inside and outside of images at the same time by using two different structuring elements. When the first structuring element translated to that pixel fits the image and the second structuring translation element misses object, then a pixel belonging to an object is preserved by the hit-or-miss operation. Two template sets s and (w-s) is included by the hit-or-miss operation. These two sets are disjoint. Image background is matched by template (w-s) and image foreground is matched by template s. Intersection of the foreground erosion with s and the background erosion with (w-s) is the hit-or-miss transformation. Expression for the hit-or-miss transform can be written as -

$$HM(x, s) = (x \ominus s) \cap [x^c \ominus (w - s)]$$

Here, x = Input image

s = Structuring element

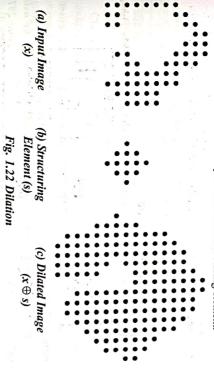
w = Small window which includes at least one pixel, thicker than s.



Q.33. Explain morphological operation on binary image.

Ans. There are two basic morphological operations as follows –

shape is known as dilation. It is an expansion operation. It is also an expansion operator. It increases size of binary objects. Structuring element is used to determine the way of binary image expand. The size of structuring element is small as compare to original image, and usually the size which is used for the structuring element is 3 × 3. The structuring element is reflected and shifted from top to bottom and from left to right at each shift, the process will look. For any overlapping similar pixels between the structuring element and that of binary image. When there is any overlapping found between pixels then pixels will be turned to black or 1 under the centre position of the structuring element.



Let us assumes as the structuring element and x as the reference image. The expression of dilation operation is as follows –

$$x \oplus s = \{z | [(\hat{s})_z \cap x] \subseteq x\}$$

Here, \hat{s} = Images moved about the origin.

The above equation states that the outcome element z should be that there will be at least one element in s that intersects with an element in x when the structuring element dilates image x. When this is the condition, the place in which the structuring element is being centred on the image will be black or 1 or ON.

(ii) Erosion – Erosion is the process of decrease the binary image from its original shape. It is a thinhing operation. It is also a thinning operator. It decreases size of binary objects, The structuring element is used to determine the way of binary image shrink. The size of structuring element is small as compare to original image, and usually the size which is used for the structuring element is 3 × 3. The erosion process can shift the element of structuring

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by the centre of the structuring element is white (0) when there is no overlapping total overlap with element of structuring or not. The centre pixel represented centre at the centre position, the process will observe to whether there is a from top to bottom and left-to-right. Presented by the structuring element

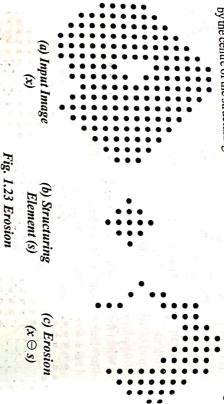


image. The expression of erosion operation is as follows -Let us assume s as the structuring element and x as the reference binary

$$x \ominus s = \{z|(s)_z \subseteq x\}$$

equal to the binary image x then the output element z is taken only. The above expression states that if the structuring element is a subset or

Q.34. Explain opening and closing operations on images by using (R.G.P.V., June 2015)

With necessary figures, explain the opening and closing operations? (R.GRV, Nov. 2018)

and removes thin portions of the image and to remove noise and CCD It is used to smooth the inside of the object contour, breaks narrow strips such as erosion and dilation. This is erosion operation followed by a dilation. defects in the images. The mathematical expression of opening is written Ans. Opening Operation - It is based on morphological operation

$$\mathbf{x} \circ \mathbf{s} = (\mathbf{x} \ominus \mathbf{s}) \oplus \mathbf{s}$$

by the dilation of the result by s. In words, the opening of x by s is simply the erosion of x by s, followed

where x represents input image and s represents structuring element.

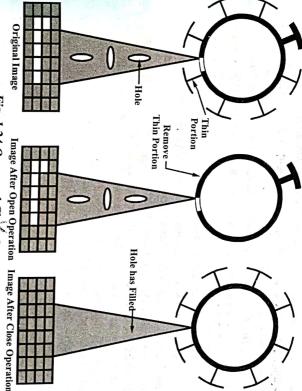


Fig. 1.24 Open and Close Operations

closing is written as gaps in a single pixels object. Closing also tends to smooth sections of contours It manages the shapes and sizes of images. The mathematical expression of dilation operation followed by an erosion. It is used to fill the small holes and Closing Operation - It is opposite of the opening operation. This is

$$\mathbf{s} \cdot \mathbf{s} = (\mathbf{x} \oplus \mathbf{s}) \ominus \mathbf{s}$$

by the erosion of the result by s. In words, the closing of x by s is simply the dilation of x by s, followed

Where x represents input image and s represents structuring element.

HX.

Q.35. Explain morphological operations on gray-scale images.

morphology. We use these operations to develop several basic gray-scale morphological algorithms. Ans. Dilation, erosion, opening and closing are basic operations of

(i) Dilation – Gray-scale dilation of x by s, denoted $x \oplus s$ is defined

as

$$x \oplus s(m,n) = \max\{x(m-p,n-q)+s(p,q)\}$$

$$|(m-p), (n-q) \in D_x; (p, q) \in D_s|$$

where, D_x and D_S are the domains of x and s, respectively

first, if all the values of the structuring element are positive, the output image

The general effect of performing dilation on a gray scale image is twofold,

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eliminated, depending on how their values and shapes relate to the structuring tends to be brighter than the input. Second, dark details either are reduced or element used for dilation.

(ii) Erosion – Gray-scale erosion, denoted $x \Theta s$ is defined as – $x \ominus s (m, n) = \min\{x(m+p, n+q) - s(p,q) | (m+p), (n+q)\}$

 $\in D_x; (p,q) \in D_s$

where D_X and D_S are the domains of x and s respectively.

The general effect of performing erosion on a gray-scale image is twofold -

first, if all the elements of the structuring element are positive, the output image tends

element is reduced, with the degree of that are smaller in area than the structuring the effect of bright details in the input image to be darker than the input image. Second, reduction being determined by the gray-level structuring element itself. values surrounding the bright detail and by the shape and amplitude values of the

and reflection. That is with respect to function complementation Gray-scale dilation and erosion are duals

 $(x \ominus s)^c$ $(m, n) = (x^c \oplus \hat{s})(m, n)$

where $x^c = -x(p, q)$ and $\hat{s} = s(-p, -q)$

image as shown in fig. 1.25 (a). In fig. 1.25 of a parallel epiped of unit height and size (b), the result of dilating this image with a and in which small, dark details have been an image that is brighter than the original 5×5 pixels. Dilation is expected to produce reduced or eliminated. In fig. 1.25 (c), the 'flat top' structuring element in the shape small, bright features were reduced. result of erosion is opposite effect to dilation. The eroded image is darker, and the size of For example, take a simple-gray-scale

image x by subimage s, denoted xos is (iii) Opening - The opening of

 $s \oplus (s \ominus x) = s \circ x$

simply the erosion of x by s. Followed by a dilation of the result by s. 12 on an and Fig. 1.25 As in the binary case, opening is





(b) Result of Dilation



(c) Result of Erosion

The gray-scale opening operation satisfies the following properties -(a) (x∘s) ⊥ x

(b) If $x_1
ightharpoonup x_2$, then $(x_1 \circ s)
ightharpoonup (x_2 \circ s)$

(c) $(x \circ x) \circ x = x \circ s$

domain of r and also that $e(p,q) \le r(p,q)$ for any (p,q) in the domain of e. The notation e⊥r is used to indicate that the domain of e is a subset of the (iv) Closing - The closing of x by s, denoted x.s is defined as -

 $\mathbf{x} \cdot \mathbf{s} = (\mathbf{x} \oplus \mathbf{s}) \ominus \mathbf{s}$

The closing operation satisfies the following properties

(a) x→(x•s)

(b) If $x_1 \, \exists \, x_2$, then $(x_1.s) \, \exists \, (x_2.s)$.

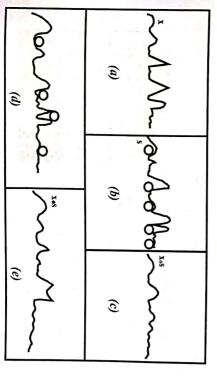
(iii) $(x \cdot s) \cdot x = x \cdot x$.

complementation and reflection. That is The opening and closing for gray-scale images are duals with respect to The usefulness of these expressions is similar to that of their binary counterparts.

$$(\mathbf{x} \cdot \mathbf{s})^{\mathbf{c}} = \mathbf{x}^{\mathbf{c}} \circ \hat{\mathbf{s}}$$

where $x^c = -x(p, q)$, above equation can be written as $-(x \cdot s) = (-x \cdot \hat{s})$.

geometrically as the process of pushing the ball against the underside of the that we open x by a spherical structuring element, s viewing this element as a whose value of any point (p, q) is the value of x at those coordinates. Suppose p- and q axes being the usual spatial coordinates and the third axis being gray-Suppose that we view an image function x(p, q) in 3-D perspective, with the "rolling ball". Then the mechanics of opening x by s may be interpreted level values. In this representation, the image appears as a discrete surface Opening and closing of images have a simple geometric interpretation.



7

Fig. 1.26 Opening and Closing Gray-scale Image

81 4

-

surface is traversed. The opening xos then is the surface of the highest points Fig. 1.26 (a) shows a scan line of gray-scale image as a continuous function reached by any part of the sphere as it slides over the entire undersurface of x. And last fig. 1.26 (d) and (e) shows the result of closing x by s. to simplify. And the rolling ball in various positions as shown in fig. 1.26 (b). Fig. 1.26 (c) shows the complete result of opening x by s along the scan line

Ans. Some various application of gray-scale morphology are as follows-Q.36. Give some application of gray-scale morphology. (i) Morphological Gradient - Dilation and erosion often are used

to compute the morphological gradient of an image, denoted g. $g = (x \oplus \hat{s}) - (x \ominus s)$

of two texture regions. The objective is to find the boundary between the two (ii) Textural Segmentation - A simple gray-scale image composed

regions based on their textural content. (iii) Granulometry—It is a field that deals principally with determining

the size distribution of particles in an image. (iv) Morphological Smoothing - One way to achieve smoothing is

to perform a morphological opening followed by a closing. function with a flat top is useful for enhancing detail in the presence of shading. original name to the use of a cylindrical or parallelepiped structuring element (v) Top-hat Transformation - This transformation which owes its

Q.37. Explain thinning operation of morphology.

amount, needed for shape description. The thinning operation is based on the only to simplify the computational methods but also to decrease the pixels Ans. Thinning a binary image down to a unit-width skeleton is useful not

hit-or-miss transformation as given below - $X \otimes B = X - HM(X, B)$

Fig. 1.27 shows the different possibilities of structuring elements. Origin $X \otimes B = X \cap HM(X, B)^c$

ᄧ X **B**₂ 3

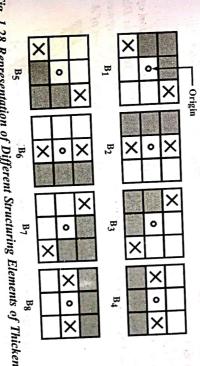
Fig. 1.27 Representation of Different Structuring Element of Thinning Operation

or vanishes even when the iteration operation continues. (ii) By a label showing an image. The operation converges if the connected skeleton does not change pixels of a connected component which are neither important for preserving the connectivity of image nor represent any significant geometrical features of distance labels is used to derive the resulting skeleton. the distance of the pixel to the boundary, thinning operation encodes distance information for every pixel of the pattern. The pixels set with local minimum The operation of thinning is divided into two types - (i) It deletes boundary

Q.38. Explain thickening operation of morphology.

as dilation or closing. Following equation defines the thickening operationregions of foreground pixels in binary images. This operation is somewhat such Ans. Thickening is the morphological operation. It is used to grow selected

is the dual of thinning, i.e., thinning the foreground is equivalent to thickening element. The thickened image comprises of the original image plus any additional can be used in the thickening operation. changes in the image. Fig. 1.28 shows the different structuring elements which the background. This process is normally continued until it causes no further foreground pixels switched on by hit or miss transform. The thickening operation In equation (i), X represents the input image and B represents the structuring $X \cdot B = X \cup HM(X, B)$



...(i)

Fig. 1.28 Representation of Different Structuring Elements of Thickening Operation

structuring element to each possible pixel position in the image, and at each determining the skeleton by zone of influence. applications of thickening operation are determining the convex hull and element is set to black. Otherwise, it is remained unchanged means white. The pixels in the image, then the image pixel underneath the origin of the structuring white pixels in the structuring element exactly match the black and white position comparing it with the underlying image pixels. When the black and The operation of thickening is computed by translating the origin of the A

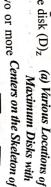
skeleton of each character. Spurs characterizes these skeletons. Spurs are of hand-printed characters, a general method is to analyze the shape of the

caused during erosion by non uniformities in the strokes composing the

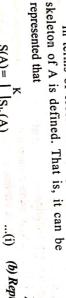
Q.39. Explain about skeletons in morphology.

a skeleton, S(A), of a set A is intuitively easy. We deduce from this figure that -Ans. As represents in fig. 1.29, the notion of

is known as a maximum disk. containing $(D)_z$ and involved in A. The disk $(D)_z$ contained in A, one cannot find a larger disk and $(D)_z$ is the largest disk centered at z and (i) When z represents a point of S(A)



different locations is touched by the disk (D)z. In terms of erosions and openings, the (ii) The boundary of A at two or more Centers on the Skeleton of A



represented that

 $S(A) = \bigcup_{k=1}^{K} S_k(A)$





(c) Representation of

...(iv) on a Different Segment of the Skeleton of A

k times, and K is the last iterative step before A another Maximum Disk which are given below where B represents a structuring element, and with $S_k(A) = (A \ominus kB) - (A \ominus kB) \ominus B$...(ii) erodes to an empty set. In other words - $(A \ominus kB) = ((....((A \ominus B) \ominus B) \ominus) \ominus B) ...(iii)$ (A ⊖ kB) represents k successive erosions of A,

$$K = \max\{k|(A \ominus kB) \neq \emptyset\}$$

these subsets by using the equationbe represented that A can be reconstructed from union of the skeleton subsets S_k(A). Also, it can (ii) represents that S(A) can be achieved as the The formulation provided in equations (i) and (d) Representation of

$$A = \bigcup_{k=0}^{K} (S_k(A) \oplus kB) \qquad \dots$$

<u>:</u> उ Complete Skeleton Fig. 1.29

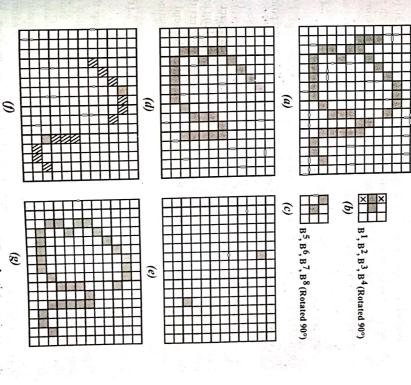
where $(S_k(A) \oplus kB) = ((.....((S_k(A) \oplus B) \oplus B) \oplus) \oplus B)$

...(vi)

Q.40. Explain about pruning in morphology.

skeletonizing algorithms due to these methods tend to leave parasitic components that require to be "eleaned up" by postprocessing. In the automated recognition Ans. Pruning procedures are an important complement to thinning and

parasitic branch. Of course, this also shortens other branches in the character character is illustrative of what we are interested in eliminating. By successively of an input set A with a order of structuring elements designed to detect only example is that any branch with three or less pixels is to be removed. Thinning removing end point of parasitic branch, the solution is based on suppressing a shown in fig. 1.30 (a). The parasitic component on the leftmost part of the Beginning with the assumption that the length of a parasitic component does characters. For handling this problem, a morphological method is developed but, in the absence of other structural information, the assumption in this not exceed a specified number of pixels. The skeleton of a hand printed "a" is



 $X_1 = A \otimes \{B\}$

where {B} represents the structuring element order which is represents in figs. 1.30 (b) and (c). The order of structuring elements comprises of two different structures, each of which is rotated 90° for a total of eight elements. The sign of × in fig. 1.30 (b) represents a "don't care" case, in the sense that it does not matter whether the pixel in that position has a value of 0 or 1 various results reported in the literature on morphology are based on the use of a single structuring element, just like to the one in fig. 1.30 (b), but having instance, this element would identify the point located in the eighth row, fourth column of fig. 1.30 (a) as an end point, hence, removing it and breaking connectivity in the stroke.

Performing equation (i) on A three times gives the set X_1 in fig. 1.30 (d). The next step is to "restore" the character to its original form, but with the parasitic branches eliminated. To do so first needs forming a set X_2 containing all end points in X_1 as given below –

$$X_2 = \bigcup_{k=1}^{k} (X_1 \otimes B^k)$$

..(ii)

where B^k represents the same end-point detectors as represented in figs. 1.30 (b) and (c). The next step using set A as a delimiter, is dilation of the end points three times –

$$X_3 = (X_2 \oplus H) \cap A$$

where, H represents a 3×3 structuring element of 1s and the intersection with A is performed after each step. Like in the condition of region filling and extraction of connected components, such conditional dilation prevents the creation of 1-valued elements outside the region of interest, like evidenced by the result represented in fig. 1.30 (f). Finally, the desired result can be obtained by the union of X_1 and X_3 ,

$$X_4 = X_1 \cup X_3$$

in fig. 1.30 (g)

In more complex scenarios, equation (iii) use sometimes picks up the "tips" of some parasitic branches. This case can occur when the end points of these branches are near the skeleton. However, equation (i) may remove them due to they are valid points in A, they can be picked up again during dilation Unless whole parasitic elements are picked up again, detecting and eliminating them is simple due to they are disconnected regions. At this juncture, a natural thought is that there must be simpler methods to solve this problem. For instance, we could just keep track of all deleted points and easily reconnected regions.

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the appropriate points to all end points remain after application of equation. This option is not invalid, but the advantage of the formulation just shown is that the use of easy morphological constructs solved the whole problem. In practical conditions, if a set of this type of tools is available, the advantage is that no new algorithm have to be written. The important morphological functions into a order of operations are easily combined.

Q.41. Explain the region growing technique.

Ans. A technique which groups pixels or subregions into larger regions based on predefined criteria for growth is known as region growing technique. The basic technique is to begin with a set of "seed" points and from these grow regions by appending to each seed those neighbouring pixels that have predefined properties similar to the seed. Choosing a set of one or more beginning points can be based on the problem nature. If a priori information is not available, the technique is to compute at every pixel the same set of properties which ultimately will be used to assign pixels to regions during the growing process. When the result of these computations represents values clusters, the pixels whose properties place them near the centroid of these clusters may be used as seeds.

The selection of similarity criteria depends not only on the problem under consideration, but also on the type of image data available. For example, the analysis of land-use satellite imagery depends heavily on the use of colour. To solve without the inherent information available in colour images, this problem would be significantly more difficult or even not possible. Region analysis must be carried out with a set of descriptors based on intensity levels and spatial properties, if the images are monochrome. When connectivity properties are not employed in the region-growing process, descriptors alone may yield misleading results. For example, a random arrangement of pixels is visualized with only three distinct intensity values. With the same intensity level, grouping pixels to form a "region" without paying attention to connectivity would yield a segmentation result which is meaningless.

The formulation of a stopping rule is the other problem in region growing. If no more pixels satisfy the criteria, region growth should stop for inclusion in that region. Criteria like intensity values, texture, and color are local in nature and do not take into account the history of region growth. Additional criteria which increase the power of region-growing algorithm utilize the concept of size, likeness between a candidate pixel and the pixels grown so far, and the shape of the region being grown. The use of these types of descriptors is based on the assumption that a model of expected results is at least partially

-

Q.42. Write a basic region-growing algorithm based on 8-connectivity.

Ans. Assume that f(x, y) represents an input image array. S(x, y) represents a seed array containing 1s at the locations of seed points and 0s elsewhere and Q represents a predicate to be applied at each location (x, y). Assume that an arrays f and S are of the same size. A basic region-growing algorithm based on 8-connectivity is given below —

-) Start
- (ii) Search all connected components in S(x, y).
- (iii) Erode each connected component to one pixel. Label all this type of pixels found as 1. All other pixels in S are labeled 0.
- (iv) Form an image f_Q such that, at a pair of coordinates (x, y), let $f_Q(x, y) = 1$ if the input image satisfies the given predicate, Q, at those coordinates and otherwise, let $f_Q(x, y) = 0$.
- (v) Let g be an image formed by appending to each seed point in S all the 1-valued points in f_Q which are 8-connected to that seed point.

 (vi) I ahel each connected component in the connected to the connecte
- (vi) Label each connected component in g with a different region label. This is the segmented image achieved by region growing.

Q.43. What do you mean by zooming and shrinking of digital images? (R.GP.V., Nov. 2019)

Ans. Image zooming is an important process in image processing. Basically zooming require two steps – the creation of new pixels locations and the assignment of gray level to those new locations. Suppose that we have an image of size 500*500 pixels and we want to enlarge it 1.5 times to 750*750 pixels. The spacing in the grid will be less than one pixel because we are fitting it over a small image. In order to perform gray level assignment for any point gray level to the new pixels in the grid. This method gray level assignment is called nearest neighbout interpolation.

Image shrinking is done in similar manner as described for zooming. The equivalent process of pixel replication is row and column deletion. For example, we want to shrink an image by one-half; we delete every row and column. How to present information effectively on small devices? This is a main challenge for small-screen interface developers because viewing on a small screen is becoming more difficult in our daily lives. We must find effective ways to organize, show, and search data or results on small screen. One of the methods is to build zoom able users, and all need tools to enable them to control the zooming purposes.



IMAGE REPRESENTATION AND DESCRIPTION – REPRESENTATION SCHEMES, BOUNDARY DESCRIPTORS, REGION DESCRIPTORS

Q.1. Write the various methods of representation. Discuss any one.

Ans. There are following methods of representation as given below -

- Boundary (border) following
-) Chain codes
- (iii) Polygonal approximations using minimum perimeter polygons (MPP)
- (iv) Signature
- (v) Skeletons.

Boundary (Border) Following – By introducing a boundary following algorithms whose output is an ordered sequence of points. We consider –

- (i) We are working with binary images where background and object points are labeled 0 and 1.
- (ii) That images are padded with a border of 0s to avoid the possibility of an object merging with the image border.

The method is extended to multiple, disjoint regions by processing the regions individually.

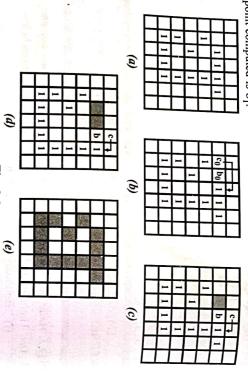
Given a binary region R, the given boundary consists of the following steps—

(i) Consider the initial point b₀, be the uppermost, leftmost in the image which is labeled 1. Indicate by c₀ the west neighbour of b₀, c₀ is always a background point. Consider b₁ represent the first neighbour encountered whose value is 1 and c₁ is the point immediately proceeding b₁ in the sequence. Check the 8 neighbours of b₀, beginning at c₀ and proceeding in a clockwise direction. Store the locations of b₀ and b₁ for use in step (v).

- (ii) Consider $b = b_1$ and $c = c_1$ as shown in fig. 2.1 (c).
- (iii) Consider the 8-neighbours of b, beginning at c and proceeding in a clockwise direction, be represented by n_1, n_2, \dots, n_8 . Determine the first n_k labeled 1.
- (iv) Consider $b = n_k$ and $c = n_{k-1}$.

The chain code representation is constructed in following steps -

point computed is b₁. (v) Repeat steps (iii) and (iv) until $b=b_0$ and the next $bounda_{D_y}$



called the Moore boundary tracking algorithm after move. is always a background point in step (iv). Sometimes, this algorithm is also Because nk is the first 1-valued point determined in the clockwise scan, c

Q.2. Write short note on chain code representation method. Ans. The chain code

as a Freeman chain code. The directional numbers is referred to formed as a sequence of such shown in fig. 2.2. A boundary code each segment direction is encoded connectivity of the segments. The by using a numbering method as representation is based on 4 or 8 direction. Typically, chain code segments of specified length and connected sequence of straight-line represent a boundary by a This representation is used to introduced in 1961 by Freeman (a) 4-directional Fig. 2.2 Chain Codes

representation method was (b) 8-directional

in fig. 2.3.

differential chain codes is shown

(a) 4-directional

Fig. 2.3 Differential Chain Codes

(b) 8-directional

its absolute coordinates in the image. Step (ii) - Every consecutive point is represented by a chain code Step (i) - Choose a initial point of the curve. This point is represented by

showing the transition need to go from the present point to the next point on the curve. Step (iii) - If the next point is the initial point then store the lengths of the

curves into the file.

 $c_i - c_{i-1}$) There are two types of chain code – code is denoted by Ki. Each differential chain code Ki is represented by the difference of the current chain code c_i and the preceding code c_{i-1} (i.e, K_i = A variation of chain code is differential chain codes and differential chain

(i) 4-directional chain code

(ii) 8-directional chain code.

be related to the principal shape features of the boundary. due to noise or imperfect segmentation cause change in the code that may not Drawbacks of Chain Code - Any small disturbances along the boundary

polygons. Q.3. Describe the polygonal approximations using minimum perimeter

Write short note on polynomial approximation. (R.G.P.V., Nov. 2018)

approximation gives a simple representation of the planar object boundary. shape in a given boundary using a fewest possible number of segments. This The objective of a polygonal approximation is to capture the quality of the boundary. Thus each pair of adjacent point defines a segment of the polygon. of the polygon is equal to the number of points in the boundary for a closed approximation. The approximation becomes exact if the number of segments Ans. A closed curve is approximated as a 2D polygon in case of polygonal

sequence. Polygonal approximation is obtained by minimization of an objective, λ_k such that each of the subsets may be approximated using a linear of the set into N mutually exclusive and collectively exhaustive subsets λ_1, λ_2 , planar object to be approximated using a polygon. It is defined as a partitioning function in the form. Consider $X = \{x_1, x_2, ..., x_n\}$ is a set of points on the boundary of a

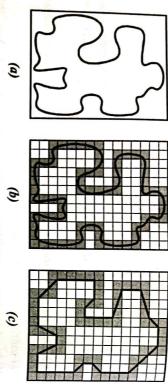
$$J = \sum_{i=1}^{n} d(x_i, l_j), x_i \in \lambda_j \qquad \dots(i)$$

approximation methods of modest complexity are well suited. One of the most powerful is representing a boundary by a minimum-perimeter polygons represents a measure of deviation. For image processing operations, where l_j represents linear structure that approximates the points λ_j and d

(MPP). It is explained in the following discussion -

(i) Foundation (ii) MPP algorithm.

MPP coincide with comers of either the inner and/or the outer walls. by the cell strip as shown in fig. 2.4 (c). In fig. 2.4 (c), all the vertices of the line segments from the polygon vertices. Disadvantage of this method is that perimeter is produced by this shrinking which circumscribes the region enclosed point are merged, after all point has been merged, the intersections of adjacent bounding region defined by the cells. The shape of a polygon of minimum is set to zero, line parameters are collected and repeats the process, other shrink, the rubber band will be constrained by the inner and outer walls of the used to merge points along a boundary. If this situation takes place, the error of concatenated cells as illustrated in fig. 2.4 (b). Because it is permitted to fine fit of the points merged so far exceeds a preset threshold, this method is algorithm to calculate MPPs is to enclose a boundary [see fig. 2.4 (a)] by a seq to solve the problem of polygonal approximation. Until the least square error (i) Foundation - An automatic appealing method for producing a



are not self intersecting, that leads to easily connected cellular complexes. is known as cellular complex. Consider the boundaries under consideration (iii) MPP Algorithm - The set of cells enclosing a digital boundar

vertices, respectively. The following observations are -Letting write (W) and black (B) denote convex and mirrored concave

- connected cellular complex, but it is not self intersecting. (a) The minimum perimeter polygon (MPP) bounded by a simply
- a vertex of the minimum perimeter polygon. polygon is a black (B) vertex, but not every black (B) vertex of a boundary is (b) Each mirrored concave vertex of the minimum perimeter
- is a vertex of the minimum perimeter polygon. polygon is a white (W) vertex, but not every white (W) vertex of a boundar, (c) Each and every convex vertex of the minimum perimeter
- vertices are outside the MPP. (d) All white (W) vertices are inside the MPP and all black (B)
- contained in a cellular complex, but it is always a white (W) vertex of the explain than the original two dimensional boundary function. Method is used minimum perimeter polygon.

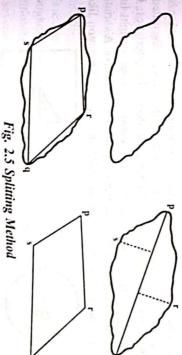
polygonal approximation. Q.4. Explain how merging scheme is used to solve the problem of

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not begin. corners to corners, because until the error threshold is increased, a next line is vertices in the final approximation do not always equivalent to inflections like Ans. Merging schemes depend on average error or other criteria is used

Q.5. Explain in brief about splitting methods of polygonal approximation.

of this method is seeking prominent inflection points. The best initial points does, the point containing greatest length from the line becomes a vertex. joining its two end points should not more than a preset threshold. When it are the two farthest points in the boundary for the closed region boundary. hence subdividing the initial segment into two different subsegments. Advantage that the maximum perpendicular length from a boundary segment to the line until a particular criterion is satisfied. For instance, a requirement might be Ans. Splitting methods are used to subdivide a segment into two sections



Q.6. Explain about signatures.

(e) The uppermost, leftmost vertex in a sequence of vertices the boundary representation to a one dimension function which is simpler to a cellular complex, but it is always a little of vertices the boundary representation to a one dimension function which is simpler to to plot the distance from the centroid to the boundary as a function of angle. to generate the signatures are invariant to translation, but they do depend on a signature. There are multiple methods to generate signature. The first one is It does not matter that how a signature is generated. The objective is to minimize Ans. A one-dimensional functional representation of a boundary is called

rotation and scaling. With respect to rotation, normalization may be obtained by searching a task to choice the same starting point to generate the signature. This function is referred to as a histogram of tangent angle values.

There are several task to choice the signature of tangent angle values.

The slope density function boundary sections which generating very quickly and reacts on strongly to the boundary sections with constant without pased on constant same starting point. The first one is to choice the starting point as the point changing angles and reacts on strongly to the boundary sections with constant same starting point. The first one is to choice the point on the size point and secause a histogram is a measure of values concentration. same statutes from the centroid. The second is to choice the point on the eigen and tangent angle because a histogram is a measure of values concentration.

of this technique is to employ the so called slope density function like size and works just like done by automatic gain control. Whatever the technique boundary may be partitioned by zero or so small which it generates computational difficulties. Variance us two object appearing in fig. 2.7 (a). The first one represents sets and its dependence may be a cause of significant error from object to object when the smallest convex set having s. The set difference H-s is known as the of the whole function depends on maximum and minimum values. This for robust boundary decomposition. The convex hull H of an arbitrary set s is along the boundary equivalent to horizontal segments in the curve. A variation orientation. angle between a line tangent to the boundary at that point and a reference line of this method is appearing in traverse the boundary and, equivalent to each point on the boundary, plot the convex deficiency. The output to generate a signature. The other method for generate the signature is to into or out of a object of the employed, the objective is to eliminate dependency on size while saving the the contour of s and marking the provides a variable scaling factor which is a inversely proportional to varies a convex deficiency. The second one represent s boundary after partition. The merit of this technique is simplicity. The disadvantage of this method is scaling a case, the convex hull of the region enclosed by the boundary is very useful is to scale all functions so that they span the same range of values. The nai concavities which carry details of shape, this technique is attractive. For such instance, because the tangent angle would be constant causes straight line dependent of boundary size and fig. 2.6, would hold detail, about fundamental shape characteristics. For principle, this method is not Although the output signature different from the $r(\theta)$ curves as illustrated in fig. 2.7 (b) in this case. In basic shape of the waveforms. Distance versus angle is not the only method transition points which is meet the signature variance, let us assume that the value of variance is not equal in the shapes are noisy. A more rugged method is to divide each sample through convex deficiency D of the set s. shape output in varies in the equivalent signature values. To normalize for the description process is simplified. If the boundary has one or more significant description process is simplified. If the boundary has one or more significant for such and which sampling is considered at equal intervals of θ , varies in Size of The boundary's complexity is reduced by decomposition and therefore,

With respect to both axes, depend on the uniformity assumptions in scaling

Q.7. Discuss boundary segments.

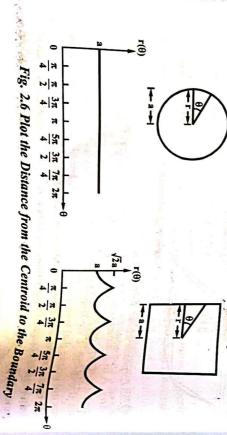
(a) Set s (b) Boundary after

Fig. 2.7 Boundary Segments

small, it can be insufficient in some boundary segments while if value of k is but it is not easy to control and take more time to process. If value of k is neighbours along the boundary. This method works for small irregularities, the coordinates of each pixel through the average coordinates of k of its are several methods for this. The first one is traverse the boundary and change partitioning as compare to sort out these irregularities by postprocessing. There throughout the boundary. A general method is to smooth a boundary prior to deficiencies which include small, meaningless components scattered randomly boundaries can be irregular. These effects appear in the form of convex large, it can provide extra smoothness. In real life, due to noise, variations in segmentation and digitization, digital

Q.8. Write the algorithm to obtain the skeleton of the region.

given below -Ans. There are two algorithms to obtain the skeleton of the region as



into a graph by obtaining the skeleton of the region via a thinning algorithm for Thinning Algorithm - Structural shape of a plane region can be reduce

Thinning algorithm is as follows —

(i) If the given below condition are satisfied, then flags a contou called Skelectonization.

(a)
$$2 \le NZ(P1) \le 6$$
 (b) $Z0(P1) = 1$

(c)
$$P2.P4.P6 = 0$$
 (d) $P4.P6.P8 = 0$

number of non-zero neighbours of P1.

	P-8	3
	Ы	P2
I	74	Ed

Fig. 2.8 (b) NZ(PI) = 4 and Z0(PI) = 3

transitions in the ordered sequence P2, P3, P4,, **P8, P9, P2.** For example, Z0(P1) = 3 and NZ(P1) = 4 in

Here Pi value is either 1 or 0 and is the number of zero to non-zer

while conditions (c) and (d) are changed into (c') (ii) Conditions (a) and (b) are not changed,



Original

(d') P2.P6.P8 = 0. (c') P2.P4.P8 = 0

Fig. 2.9 Thinning

boundary is locally maximum known as skeleton.

(ii) Transform of distance

 $u_k(m,n) = u_0(m,n) + \min_{\Delta(m,n;i,j)} \{u_{k-1}(i,j); (i,j); \Delta(m,n;i,j) \le 1\},$

here k = 1, 2,

 $\Delta(m, n; i, j) = Distance between (m, n) and (i, j)$

(iii) The skeleton is the set of points -

(iv) End. $\{(m,n): u_k(m,n) \geq u_k(i,j), \Delta(m,n;i,j) \leq 1\}$

> obtaining the skeleton of the region via a thinning algorithm. A skeleton also plane region is to reduce it to a graph. This reduction may be accomplished by Ans. An important approach of representing the structural shape of a Q.9. What do you mean by the term skeleton? (R.G.P.V., Nov. 2019)

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Here, NZ(PI) = P2 + P3 + + P7 + P8 + P9 and NZ(PI) represents the a specified subset of the transformed image is a distance skeleton. The original noise at the frontier. component into an image showing essential characteristics can eliminate local of data or to simplify the shape of an object in order to find features for interest in skeletonization algorithms are the need to compute a reduced amount algorithms should be a connected set of digital curves or arcs. Motivations for recognition algorithms and classifications. Additionally the transformation of a component can be reconstructed from the distance skeleton. Another category a subset of the original component. There are different categories of is defined by thinning approaches; and the result of skeletonization using thinning skeletonization methods - one category is based on distance transforms, and Skeletonization is a transformation of a component of a digital image into

Q.10. Explain some simple descriptors in boundary descriptors.

number of diagonal components provides its exact length for a chain coded The number of pixels along a boundary provides a rough approximation of its curve with unit spacing in both directions. length. The number of vertical and horizontal components plus $\sqrt{2}$ times the Ans. The length of a boundary represents one of its simplest descriptors.

The diameter of a boundary B is specified as given below

$$Diam(B) = \max_{i,j} [D(p_i, p_j)]$$

Skeleton Algorithms - The set of points whose distance from the neare. The value of the diameter and the orientation of a line segment connecting the u₀(m, n) ≜u(m, n of the major to the minor axis is known as the eccentricity of the boundary.

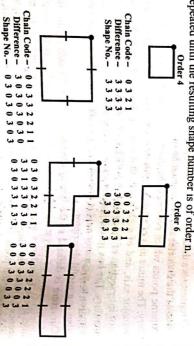
This also is a useful descriptor. the boundary. The box just defined is known as the basic rectangle. The ratio Points of intersection of the boundary with the two axes completely encloses to the major axis, and of such length that a box passing via the outer four boundary. The minor axis of a boundary is described as the line perpendicular two extreme points which comprise the diameter are useful descriptors of a

k = Maximum thickness of the region, the transform is computed because these boundaries tend to be locally "ragged". Although, using the useful. Since the boundary is traversed in the clockwise direction, a vertex of curvature at the point of intersection of the segments sometimes proves difference between the slopes of adjacent boundary segments as a descriptor

order n of a shape number is expressed as the number of digits in a not a shape number is expressed as the number of digits in the boundary itself can be represented as the and value of n limits the number of possible different shapes. fig. 2.2 (a), is expressed as the first difference of smallest magnitude. The $x(k) = x_k$ and $y(k) = y_k$. With this notation, Ans. The shape number of boundary, based on the 4-directional code coordinates may be expressed in the form

orientation is by aligning the chain-code grid with the sides of the basic rectangle and the y-axis as the imaginary axis of a sequence of complex numbers. boundary depends on the orientation of the grid. One method to normalize the gn the first difference of a chain-code is not dependent of rotation, usually the code the chain-code as a circular sequence, the first difference is calculated. Howew representations, first differences, and corresponding shape numbers. By treating Fig. 2.10 shows all the shapes of order 4, 6 and 8 along with their chain-cod hence,

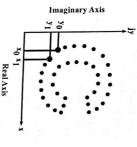
condition, a rectangle of order lower than n is specified and procedure for $u = 0, 1, 2, \dots, K - 1$. The complex coefficients a(u) are known as the repeated until the resulting shape number is of order n. this spacing sometimes yield shape numbers of order greater than n. In the way the grid spacing was chosen, boundaries with depressions comparable code. However, the order of the resulting shape number equals n due to the the chain code. The shape number follows from the first difference of the rectangle is used to establish the size of grid and procedure is used to achieve that it decreases a 2-D to a 1-D problem. whose eccentricity best approximates that of the basic rectangle. This nee boundary itself was not changed. This representation has one great advantage



Q.12. Explain Fourier descriptors in boundary descriptors.

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Q.11. Explain in brief about shape numbers in boundary descripton in the counter-clockwise direction. These pair may be treated as a complex number, for $k = 0, 1, 2, \dots, K - 1$. Each coordinate sequence of coordinates s(k) = [x(k), y(k)], $(x_0, y_0), (x_1, y_1), (x_2, y_2), \dots, (x_{K-1}, y_{K-1})$



and its Representation Like a Fig. 2.11 A Digital Boundary Complex Sequence

Practically, for a desired shape order, the rectangle of order n is determine However, the interpretation of the sequence was recast, the nature of the For $k = 0, 1, 2, \dots, K - 1$. That is, the x-axis is treated as the real axis s(k) = x(k) + jy(k)

The discrete Fourier transform of s(k) is given below -

$$a(u) = \sum_{k=0}^{K-1} s(k)e^{-j2\pi uk/K} \qquad ...(ii)$$

coefficients restores s(k) which is given below -Fourier descriptors of the boundary. The inverse Fourier transform of these

$$s(k) = \frac{1}{K} \sum_{u=0}^{K-1} a(u)e^{j2\pi uk/K} \qquad ...(iii)$$

P-1 in equation (iii). The following approximation to s(k) is given below the first P coefficients are employed. This is equivalent to setting a(u) = 0 for u > for $k = 0, 1, 2, \dots, K - 1$. Assume that instead of all the Fourier coefficients, only

$$\hat{s}(k) = \frac{1}{P} \sum_{n=0}^{P-1} a(n)e^{j2\pi nk/P} \qquad(iv)$$

of points exists in the approximate boundary, but not as many terms are P terms are employed, k still ranges from 0 to K-1. That is, the same number for $k = 0, 1, 2, \dots, K - 1$. However, to achieve each component of $\hat{s}(k)$, only

Fig. 2.10 Representation of all Shapes of Order 4, 6 and 8

be used as the basis for differentiating between distinct boundary shapes. coefficients keep shape information, this property is valuable. Hence, they can be employed to capture the gross essence of a boundary. Due to these the more detail which is lost on the boundary. A few Fourier descriptors can determined by low-frequency components. Hence, the smaller P becomes high-frequency components account for fine detail and global shape is employed in the reconstruction of each point. From the Fourier transform, the

origin. The rotated sequence is $s(k) e^{i\theta}$, whose Fourier descriptors are givetabout the origin of the complex plane is accomplished by multiplying the point points of the segment and rotating the line segment until it is horizontal. The recall from basic mathematical analysis that rotation of a point by an angle of an arbitrary variable r. This function is achieved by connecting the two end to easy transformations on the descriptors. For example, assume rotation, and and fig. 2.12 (b), which represents the segment shown as a 1-D function g(r) to these geometrical changes, but changes in these parameters can be related insensitive to the starting point. Fourier descriptors are not directly insensitive the mean, variance, and higher order moments. To see how this can be points are processed, an additional constraint is that descriptors should by and scale changes. In conditions where results depend on the order in whichThe descriptors should be as insensitive as possible to translation, rotation

$$a_{\mathbf{f}}(\mathbf{u}) = \sum_{\mathbf{k}=0}^{K-1} s(\mathbf{k}) e^{\mathbf{j}\theta} e^{-\mathbf{j}2\pi\mathbf{u}\mathbf{k}/K}$$

rotation simply affects all coefficients equally. for u = 0, 1, 2,, K - 1. Hence, by a multiplicative constant term $e^{i\theta}$ = a(u) e

point. The symbol Δ_{xy} is described as $\Delta_{xy} = \Delta x + j\Delta y$, hence, the notation form an amplitude histogram $p(v_i)$, i = 0, 1, 2,, A - I, where A represents $s_t(k) = s(k) + \Delta_{xy}$ denotes redefining the sequence as given below – s(k) which undergoes rotation, translation, scaling, and changes in starting Table 2.1 represents the Fourier descriptors for a boundary sequence

Table 2.1 Some basic Properties of Fourier Descriptors $s_t(k) = [x(k) + \Delta x] + j[y(k) + \Delta y]$

Transformation
Identity
Rotation
Translation $s_t(k) = s(k) + \Delta_{xy}$ $a_t(u) = a(u)e^{-x}$
Scaling
Starting point $s_p(k) = s(k-k_0)$ $a_p(u) = a(u) - \frac{2\pi k_0}{3}$

to all coordinates in the boundary. Translation has no effect on the descriptor histogram. In other words, g(r_i) is treated as the probability of value r_i occurring. In other words, translation comprises of adding a constant displacement. An alternative method is to normalize g(r) to unit area and treat it as a

means redefining the sequence as given below except for u=0, which include the impulse $\delta(u)$. Expression $s_p(k)=s(k-k_0)$

 $s_p = x(k - k_0) + jy(k - k_0)$

descriptors in a different way, in the sense that the term multiplying a(u) which simply changes the starting point of the sequence to $k=k_0$ from k=0. The last entry in table 2.1 represents that a change in starting point affects all

coordinates of the points are rotated by the same angle. Q.13. Explain in brief about statistical moments in boundary descriptors.



(a) Boundary Segment

Fig. 2.12 (b) Representation as a I-D Function

...(vi Then, keeping in mind that $p(v_i)$ is an estimate of the probability of value v_i occurring, the nth moment of v about its mean is given below the number of discrete amplitude increments in which amplitude scale is divided.

$$\mu_{\mathbf{n}}(\mathbf{v}) = \sum_{i=0}^{N-1} (\mathbf{v}_i + \mathbf{m})^{\mathbf{n}} \mathbf{p}(\mathbf{v}_i) \qquad \dots$$

recognized as its variance. Normally, only the first few moments are needed The quantity m is recognized as the mean or average value of v and μ_2 is ...(II)

In this condition, r is treated as the random variable and the moments are

$$\begin{split} \mu_n(r) &= \sum_{i=0}^{K-1} (r_i - m)^n \, g(r_i) & ...(ii) \\ e &\qquad m = \sum_{i=0}^{K-1} r_i \, g(r_i) & ...(iv) \end{split}$$

In this notation, K is the number of points on the boundary and $\mu_n(r)$ is directly related to the shape of g(r). For example, the spread of the curve about the mean value of r is measured by the second moment $\mu_2(r)$ and third moment $\mu_3(r)$ measures its symmetry with reference to the mean.

Generally, what we have accomplished is to decrease the description task to that of describing 1-D functions. However moments are by far the most popular procedure, they are not the only descriptors employed for this purpose. For instance, another procedure involves computing the 1-D discrete Fourier transform, achieving its spectrum and using the first q components of the spectrum to define g(r). The advantage of moments as compared to other method is that implementation of moments is straightforward. They also keep a physical interpretation of boundary shape. From fig. 2.12, the insensitivity of this method to rotation is clear. Size normalization, if desired, can be obtained by scaling the range of values of g and r.

Q.14. Explain in brief about shape descriptors.

Ans. Shape descriptors are a powerful tool used in wide spectrum of computer vision and image processing tasks like object matching, classification, recognition and identification. Many approaches have been developed. There are a number of generic shape descriptors that are capable of providing a high dimensionality feature vector that accurately describes specific shapes (for example, Fourier descriptors and moment invariants). Alternatively, other descriptors describe some single characteristic that is present over a variety of shapes, like circularity, ellipticity, rectangularity, triangularity, rectilinearity, complexity, mean curvature, symmetry, etc. Even for a single characteristic of shapes there often exist many alternative measures which are sensitive to different aspects of the shape. Very likely, the shape convexity is a shape property with the largest number of different methods defined for its evaluation. The need for alternative measures is caused by the fact that there is no a single shape descriptor which is expected to perform efficiently in all possible applications.

Generally speaking, there are two approaches to analyze shapes – boundary based (which use the information from boundary points only) and area based ones (which use all the shape points). It could be said that, in the past, more attention has been given to the area based methods. The area based methods are more robust (e.g. with respect to noise). Although not mentioned often, and are more robust (e.g. with respect to noise).

additional reason for a larger number of methods that are based on 'interior' shape points, rather than methods based on boundary points, is that area based methods are usually simpler to compute. For example, to estimate accurately the area of a given shape, it is sufficient to enumerate the number of pixels inside the shape, while the perimeter estimation is not a straightforward task. Depending on particular situation and conditions assumed different methods

have to be used. easily and accurately computable from the corresponding object image, while a very popular shape measure, the shape compactness classified either as boundary based or volume (area) based ones. For example image technology, high quality data can be provided, and the use of boundary Robustness is a very desirable property when we work with low quality data objects with partially extracted boundaries or with partially occluded objects. boundary based methods are more suitable for a high precision computer image processing and computer vision applications. On the other side, the are not simple to be estimated from discrete data, which are mainly used in shape boundaries are represented by a significantly smaller number of pixels boundary based methods could have a much lower time complexity because based methods becomes highly acceptable in many applications. In addition, (e.g., noisy images or low resolution images), but recently, due to progress in vision and image processing tasks. They are able to cope much easier with their boundary based analogues involve computation of path integrals, which than complete shapes are. Of course, there are methods which cannot be Another example would be geometric (area) moment invariants, these are

$$C_{st}(S) = \frac{4.\pi.\text{Area of } S}{(\text{Perimeter of } S)^2}$$

obviously uses both boundary and interior information. This quantity indicates how much a given shape differs from a perfect circular disc, which is understood as the most compact shape. Accordingly, the highest possible compactness (equal to 1) is assigned to circular disc. Finally, there are methods which use only information from specific points or specific boundary parts belonging to the convex hull of the shape considered).

Here, we focus on shape analysis techniques based on the use of a set of suitably selected shape descriptors/measures. Generally speaking, a shape measure is a quantity which relates to a particular shape characteristic. More maps a given planar shape measure D(S) (related to a certain shape descriptor) object classification, recognition or identification task, any shape measure is rotation, and scaling). Also, shape measures are preferred to be given in a normalized form. An easiest way to achieve a normalized form is to apply a

interval [0, 1] [or even better through the interval (0, 1)] while S varies through transformation. The folded, then the interval [0, 1] are region is turn or folded, then the contract planar regions. scaling transformation which would preserve that D(S) varies through the transformation. Usually, when the scaling transformation which would preserve that D(S) varies through the transformation. Usually, when the

Thus, common desirable properties of a given shape measure D(S) are

- (ii) D(S) =

for which, actually, the shape measure D(S) is designed. if S satisfies a certain property (here called a shape descripto properties implicitly based on the

- (iii) D(S) is invariant with respect to the similarity transformation
- the best possible lower bound for D(S)). (iv) For any $\delta > 0$ there is a shape S such that D(S) $< \delta$ (e.g., 0)

Q.15. Explain in brief about some simple descriptors in regional descripton

the circularity ratio R_c is obtained by the equation, which is given below the same perimeter. $P^2/4\pi$ is the area of a circle with perimeter length P. Hence ratio, described as the ratio of the area of a region to the area of a circle having in which the size of the regions of interest is invariant. A more frequent use can be used to describe the Euler (perimeter)²/area. A slightly different descriptor of compactness is the circulari these two descriptors is in measuring compactness of a region, described and area are sometimes employed as descriptors, they apply primarily to condition perimeter of a region represents the length of its boundary. However, perimeter Ans. A region area is described as the number of pixels in the region η

of the intensity levels, the minimum and maximum intensity values, and the number of pixels with values above and below the mean. easy measures employed like region descriptors include the mean and media errors which can be introduced in resizing and rotating a digital region. Another changes; it is insensitive also to orientation, ignoring, of course, computations dimensionless measure. Hence, compactness is insensitive to uniform scale for square region, the value of this measure is $\pi/4$. Compactness is length of its perimeter. For a circular region, the value of this measure is I am where, A represents the area of the region in question and P represents the

Q. 16. Explain in brief about topological descriptors in regional descriptors A COUNTY OF THE PARTY OF THE PA

region, this property obviously will not be affected by a stretching or rotation when a topological descriptor is described by the number of holes in the figure. For example, a region with two holes is shown in fig. 2.13. Hence unaffected by any deformation, as long as there is no tearing or joining of the in the image plane. Topology is the study of properties of a figure, which are Ans. Topological properties are useful for global descriptions of regions following relationship, known as number of faces by F gives the number of edges by "Q", and the number of vertices by "V", the network into faces and holes is often Important. Representating the

stretching affects distance, number of holes will change. As concept of a distance measure. on the notion of distance or any topological properties do not depend

topological property useful is the region with three connected components is represented in fig. 2.14. number of connected components. A For region description, another

number E nents C and the number of holes H In a figure, connected compo-



have Euler numbers equal to 0 and shown by straight-line segments component but two holes. Regions hole and the "B" one connected one connected component and one topological property. Fig. 2.15 interior regions of this type of represented by fig. 2.16. Classifying number. A polygonal network is interpretation in terms of the Euler include a particularly easy (known as polygonal networks), l, respectively, due to the "A" has represents the regions, for example, The Euler number is also a

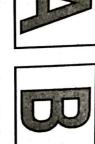


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Fig. 2.13 Representation of a Region with Two Holes



Fig. 2.14 Representation of a Region with Three Connected Components



with Euler Numbers Equal to 0 and -i Fig. 2.15 Representation of Regions

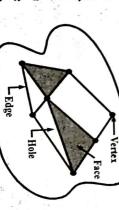


Fig. 2.16 A Polygonal Network is

Contained by Region

Euler formula which is given below -

$$V-Q+F=C-H$$

which, in view of equation (i), is equal to the Euler number -

$$V-Q+F=C-H=E$$

vertices, eleven edges, two faces. Hence, the Euler number is -2. The network in fig. 2.16 has one connected region, three holes, Selection of the Fuler number is _2

$$7 - 11 + 2 = 1 - 3 = -2$$

is given by topological descriptors. An additional feature which is useful in characterizing regions in a scen

Q.17. Write short note on texture in regional descriptors.

identifying high-energy, narrow peaks in the spectrum. Spectral methods are used primarily to detect global periodicity in an image h spaced parallel lines. Spectral methods are based on properties of the Fourier spectrum arrangement of image primitives like the description of texture based on regulation textures like smooth, coarse, grainy, and so on. Structural methods deal with & to describe the texture of a region. Statistical methods yield characterizations structural and spectral are the three principal methods employed in image processing measures of properties like smoothness, coarseness, and regularity. Statistical However no formal definition of texture presents, intuitively this descriptor provide Ans. An important method to region description is to quantify its texture content

Q.18. Derive the expression of moment invariants in regional descripton

M × N is given below -Ans. The 2-D moment of order (p + q) of a digital image f(x, y) of sin

$$m_{pq} = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} x^p y^q f(x, y)$$

where, $p = 0, 1, 2, \dots$ and $q = 0, 1, 2, \dots$ are integers. The corresponding central moment of order (p+q) is given below –

$$\mu_{pq} = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} (x - \bar{x})^{p} (y - \bar{y})^{q} f(x, y)$$

for $p = 0, 1, 2, \dots$ and $q = 0, 1, 2, \dots$

 $\overline{x} = \frac{m_{10}}{m_{00}}$ and $\overline{y} = \frac{m_{01}}{m_{00}}$

The normalized central moments, denoted npq, are given below -

$$\gamma = \frac{\mu_{00}^{\gamma}}{2} + 1$$

for $p + q = 2, 3, \dots$

can be derived -From the second and third moments, a set of seven invariant moments

$$\phi_1 = \eta_{20} + \eta_{02}$$

 $\phi_2 = (\eta_{20} - \eta_{02})^2 + 4\eta_{11}^2$...(vi)

$$\begin{aligned} & \phi_2 = (\eta_{20} - \eta_{02})^2 + 4\eta_{11}^2 & ...(vi) \\ & \phi_3 = (\eta_{30} - 3\eta_{12})^2 + (3\eta_{21} - \eta_{03})^2 & ...(vii) \\ & \phi_4 = (\eta_{30} + \eta_{12})^2 + (\eta_{21} + \eta_{03})^2 & ...(viii) \\ & \phi_5 = (\eta_{30} - 3\eta_{12}) (\eta_{30} + \eta_{12}) [(\eta_{30} + \eta_{12})^2 - 3(\eta_{21} + \eta_{03})^2] \\ & + \eta_{03})^2] + (3\eta_{21} - \eta_{03}) (\eta_{21} + \eta_{02})^{12} (\eta_{22} - 3(\eta_{21} + \eta_{03})) \\ \end{aligned}$$

$$\begin{aligned} &+\eta_{03})^{2}] + (3\eta_{21} - \eta_{03}) (\eta_{30} + \eta_{12})^{2} - 3(\eta_{21} + \eta_{03})) \\ &+(\eta_{13} - \eta_{03}) (\eta_{21} + \eta_{03}) [3(\eta_{30} + \eta_{12})^{2} - 3(\eta_{21} + \eta_{03})) [3(\eta_{30} + \eta_{12})^{2} - (\eta_{21} + \eta_{03})^{2}] ...(x) \end{aligned}$$

$$&+ (\eta_{12} - \eta_{02}) [(\eta_{30} + \eta_{12})^{2} - (\eta_{21} + \eta_{03})^{2}] ...(x)$$

$$&+ (\eta_{11} - \eta_{130} + \eta_{12})^{2} - (\eta_{21} + \eta_{03})^{2}]$$

 $\phi_7 = (3\eta_{21} - \eta_{03}) (\eta_{30} + \eta_{12}) [(\eta_{30} + \eta_{12})^2]$ $-3(\eta_{21}+\eta_{03})^2]+(3\eta_{12}-\eta_{30})(\eta_{21}+\eta_{03})$ $^{+}4\eta_{11}(\eta_{30}+\eta_{12})(\eta_{21}+\eta_{03})...(xi)$

and rotation. Q.19. Explain the use of principal components for description. This set of moments is invariant to translation, scale change, mirroring $[3(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2]$...(xii)

group of three corresponding pixels as a vector. colour image. The three image can be treated as a unit by expressing each Ans. Assume that we are given the three component images of such a

...(i in the form of a 3-D column vector, a where of the three RGB component images. These three elements can be expressed For example, let a₁, a₂ and a₃ respectively, be the values of pixel in each

vectors will be n-dimensional the pixels are represented in this manner. If we have n registered images, the images are of size $M \times N$, there will be a total of K = MN 3D vectors after all Here, this vector represents one common pixel in all three images. If the

$$\mathbf{a} = \begin{bmatrix} \mathbf{a}_1 \\ \mathbf{a}_2 \\ \vdots \\ \mathbf{a} \end{bmatrix} \dots (i)$$

m(v) order $n \times 1$). We can write them on a line of text simply by expressing them as $a = (a_1, a_2, ..., a_n)^T$, where "T" is transpose. The assumption is that all vectors are column vectors (i.e. matrices of

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element. The covariance matrix of the vector population is defined as value of a vector or matrix is obtained by taking the expected value of a that M is associated with the population of a vectors. Recall the expension of the expensio Here, E{.} is the expected value of the argument, and the subscript delay where for a darker object on a lighter background for if GIx vi<T

$$\mathbf{Q_a} = \mathbf{E}\{(\mathbf{a} - \mathbf{M_a})(\mathbf{a} - \mathbf{M_a})^{\mathrm{T}}\}\$$

Here, a is n dimensional, Q_a and $(a - M_a)(a - M_a)^T$ are matrices of q_i n × n. Element q_{ii} of Q_a is the variance of a_i , the i^{th} component of i_{th} $=q_{ji}=0$ all these definitions reduce to their familiar one dimensional counterpa elements a; and a; are uncorrelated, their covariance is zero and, therefore, may come from several disjoint intervals may be represented as element a_i and a_j of these vectors. The matrix $\mathbf{Q_a}$ is real and symmetric vectors in the population, and element q_{ij} of Q_a is the convariance between we may use

HIERARCHICAL SEGMENTATION, SPATIAL CLUSTERING SEGMENTATION, CONNECTED COMPONENT LABELING SPLIT & MERGE, RULE BASED SEGMENTATION, BINARY MACHINE VISION - THRESHOLDING, MOTION-BASED SEGMENTATION

Q.20. What do you mean by thresholding?

a gray-scale image and the binary image is obtained using thresholding. such a camera is a binary image. In most applications, however, cameras given predefined parameter To repeat steps from (iii) to (v). a gray-scale image and the binary image is obtained main the cameras given predefined parameter To repeat steps from (iii) to (v). designed to perform this thresholding operation in hardware. The output segmentation and thresholding are synonymous. Many cameras have be that interval to 1 and points outside that range to 0. Thus, for binary vision image can be obtained using a thresholding operation that sets the points intensity values of the backgrounds pixels are outside this interval, a bing level values μ_1 and μ_2 . gray-scale image. If the intensity values of an object are in an interval and Ans. A binary image is obtained using an appropriate segmentation of second one is G_2 which holds pixels with values $\leq T$. scale image. If the intensity values $= C_2$ and $= C_3$ and $= C_4$ scale image. If the intensity values $= C_4$ and $= C_4$ and

that the objects and background have sufficient contrast and that we knownsed of all possible segmentation techniques. In this method, a threshold value image so that objects of interest are separated from the background. For thresholding to be effective in object-background separation, it is necessar Thresholding is a method to convert a gray-scale image into a bing

Let us assume that a binary image B[x, y] is the same as a thresholded

gray image G[x, y]. Thus gray image $G_T[x, y]$ which is obtained using a threshold T for the original

 $G_{T}[x, y] =$ if $G[x, y] \le T$

If it is known that the object intensity values are in a range [T1, T2], then

 $G_T[i, j] = \begin{cases} 1 & \text{if } T_1 \le G[x, y] \le T_2 \end{cases}$

A general thresholding scheme in which the intensity levels for an object

 $G_{T}[i,j] = \langle$ 1 if $G[x, y] \in X$

where X is a set of intensity values for object components

Q.21. Write the algorithm to estimate the thresholding values. (R.GP.V., June 2015)

Ans. The algorithm to estimate the thresholding values is as follows -

Select an initial estimate for T(threshold)

the first one is G_1 which holds all pixels with gray level values > T and the (iii) Segment the image using T. This will generate two sets of pixels

(iv) For the pixels in regions G1 and G2, calculate the average gray

(v) Calculate a new threshold value -

Until the difference in T in successive iterations is smaller than $T = \frac{\mu_1 + \mu_2}{2}$

yar (vii) End. A see service or is a second

Q.22. Explain global and adaptive thresholding techniques. (R.GP.V., June 2015)

Ans. Global Thresholding Technique - It is simplest and most widely

of θ is selected and given condition is imposed –

$$\mathbf{x}(\mathbf{k}, h) = \begin{cases} 1 & \text{if } \mathbf{x}(\mathbf{k}, h) \ge 0 \\ 0 & \text{else} \end{cases}$$

local segmentation. illumination across the image. Hence, this may be considered as a form of Variable thresholding can be used when the overlap is due to variation is determined by accuracy of segmentation. Considerable care is therefore, thresholds to minimize the classification error when error is due to noise difficult task. The eventual success or failure of computerized analysis methods minimum-error may estimate the underlying cluster parameters and select the in their use of intensities global thresholding will be affected. A method like components. There is no need to carry segmentation past the level of detail has to be chosen in an optimal way. If pixels from different segments overla does not define that how to choose the threshold parameter 0. The value of assemblies interest lies in analyzing products' images to find the presence or

threshold values are indicated by one and remaining are indicated by zero. transformed into a binary image. All pixels values are greater than the glob

operations are based on local image features. In the condition of poor Illuminated images, local thresholding is more useful as compared to global detection and recognition tasks, automatic traffic control systems and video Adaptive Thresholding Technique - In this method, the thresholding

threshold. Two problems associated with this approach are as follows - th uneven illumination. This problem can be solved by dividing the original image consisting of large number of pixels). The image segmentation approaches which cannot be partitioned effectively through a single global threshold by and global segmentation (concerned with segmenting the whole image, of thresholding is known as adaptive thresholding. each pixel depends on the pixel position with respect to subimages, this typ to intensity discontinuity are detected and linked to form boundaries of regions. the threshold for each resulting subimage. Because the threshold used for detection based segmentation falls in this category in which edges formed due into subimages. After that, to segment each subimage utilize a difference can be categorized into two types based on properties of image. first one is how to subdivide the image and the second one is how to estimation which an image is segmented into regions based on discontinuity. The edge A perfectly segmentable histogram can be converted into a histogram

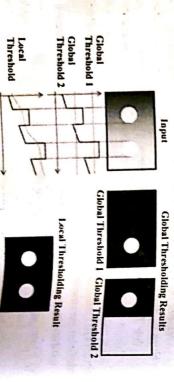


Fig. 2.17 Representation of Global and Local (Adaptive) Thresholding

Q.23. What is image segmentation? Explain.

In this method, using image intensity value, a gray scale image, manner to develop objects of interest. Analysis and interpretation can be Equation (i) represents a full description of a binarisation algorithm. have been isolated. For instance, in the automated analysis of electronic absence of specific anomalies like broken connection paths or missing required to identify those elements. Segmentation of nontrivial images is very performed these objects. required to improve the probability of rugged segmentation. Image segmentation The level to which the subdivision is carried depends on the problem to be solved, i.e. segmentation should stop if the objects of interest in an application is used to extract multiple features of the image that may split or merged in Ans. Image segmentation subdivides an image into its constituent objects.

segmentation are - Content-based image retrieval, medical imaging, object segments having similar features or attributes. The basic applications of image types - Local segmentation (concerned with specific part or region of image) surveillance, etc. The image segmentation can be classified into two basic The goal of image segmentation is to divide an image into several parts

(i) Discontinuity Detection Based Approach - This is the approach

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methodology. These divide the image into set of clusters having similar features regions having similar set of pixels. The clustering techniques also use this techniques and region splitting and merging. These all divide the image into that falls under this approach are - thresholding techniques, region growing which an image is segmented into regions based on similarity. The techniques based on some predefined criteria. (ii) Similarity Detection Based Approach - This is the approach in

data clustering. The region approach falls under similarity detection and edge approached from three perspectives - Region approach, edge approach and detection and boundary detection falls under discontinuity detection. Clustering rechniques are also under similarity detection. In other words, also we can say that image segmentation can be

from each other with respect to the method used by these for segmentation. and artificial neural network based techniques etc. These all techniques are different based techniques, watershed based techniques, partial differential equation based method, edge detection based techniques, region based techniques, clustering method, edge detection based techniques narrial differential entractions. Q.24. Explan in detail the classification of image segmentation technique Ans. The popular techniques used for image segmentation are – thresholding the popular techniques used for image segmentation are – thresholding the popular techniques of the popular techniques of the popular techniques of the popular techniques of the popular techniques used for image segmentation are – thresholding techniques of the popular techniques used for image segmentation are – thresholding techniques of the popular techniques used for image segmentation are – thresholding techniques used techniques of the popular techniq

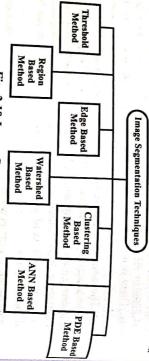


Fig. 2.18 Image Segmentation Techniques

are basically three types of thresholding i.e., can be based on prior knowledge or information of image features. Then than background. The selection of these methods can be manual or automati their intensity level. These methods are used over images having lighter object image segmentation. These methods divide the image pixels with respect Thresholding Methods - These are the simplest methods for are two basic techniques based on this method -

original image p(x, y) as image. On the basis of T the output image q(x, y) can be obtained from appropriate threshold value/T. This value of T will be constant for whole (a) Global Thresholding - This is done by using an

$$q(x, y) = \begin{cases} 1, & \text{if } p(x, y) > T \\ 0, & \text{if } p(x, y) \le T \end{cases}$$

upon the neighbourhood of x and y. value of T can vary over the image. This can further be of two types -(b) Variable Thresholding - In this type of thresholding, the (1) Local Threshold - In this case the value of T depend

(2) Adaptive Threshold - The value of T is a function of T(x, y) = True.

x and y.

are multiple threshold values like T0 and T1. By using these output image car $q(x, y) = \{n,$ m, if p(x, y) > T1if $p(x, y) \le T1$

$$q(x, y) = \begin{cases} n, & \text{if } p(x, y) \le T1 \\ 0, & \text{if } p(x, y) \le T0 \end{cases}$$

image histograms. Simple algorithms can also be generated to compute these, The values of thresholds can be computed with the help of the peaks of the

operator, canny operator and Robert's operator etc. can be used. Result of based on discontinuity detection. these methods is basically a binary image. These are the structural techniques To detect the edges one of the basic edge detection techniques like sobel segmentation methods are - Gray histograms and Gradient based methods. the edges are detected and then are connected together to form the object edges. Edge detection techniques locate the edges where either the first segmentation methods are based on the rapid change of intensity value in an well developed techniques of image processing on their own. The edge based boundaries to segment the required regions. The basic two edge based derivative has zero crossings. In edge based segmentation methods, first of all derivative of intensity is greater than a particular threshold or the second image because a single intensity value does not provide good information about (ii) Edge Based Segmentation Methods - These techniques are

segments the image into various regions having similar characteristics. There (iii) Region Based Segmentation Methods - These methods

8-connectivity) steps for region growing method are which is to be tested for each (x, y) location. Then basic algorithm (based on is the binary image where the seeds are located. Also let, 'T' be any predicate between pixels and with the help of the prior knowledge of problem, this can be stopped. Let p(x, y) be the original image that is to be segmented and s(x, y)particular application). Then the growing of seeds is controlled by connectivity selected manually (based on prior knowledge) or automatically (based on segmentation methods are the methods that segments the image into various regions based on the growing of seeds (initial pixels). These seeds can be (a) Region Growing Methods - The region growing based

(1) First of all, all the connected components of 's' are

eroded

(2) Compute a binary image P_T , where $P_T(x, y) = 1$, if

(c) Multiple Thresholding - In this type of thresholding, then = 1 and (x, y) is 8-connected to seed in 's'. (3) Compute a binary image 'q', where q(x, y) = 1, if $P_T(x, y)$

1.e., splitting and merging for segmenting an image into various regions. Splitting splitting and merging based segmentation methods use two basic techniques These connected components in 'q' are segmented regions (b) Region Splitting and Merging Methods - The region

maximizing the intra cluster similarity and also minimizing the inter cluster

and merging contributes to combining the adjacent similar regions. Following based technique known as ricivi. In this technique, first of all the centers are diagram shows the division based on quad tree. The basic algorithm steps to computed then each pixel is assigned to nearest center. It emphasizes on the intra cluster similarity and also minimizing the intra cluster similarity and also minimizing the intra cluster. stands for iteratively dividing an image into regions having similar characteristic based technique known as HCM. In this technique, first of all the centers are on the content of the center of the

- (1) First of all the R₁ is equal to P.
- (2) Each region is divided into quadrants for which $T(R_{ij})$

False.

- regions R_i and R_j such that $T(R_i \cup R_j) = True$. (3) If for every region, $T(R_i) = \text{True}$, then merge adjac_{Q_i}
- (4) Repeat step 3 until merging is impossible.
- where 'p' be the original image and 'T' be the particular predicate.

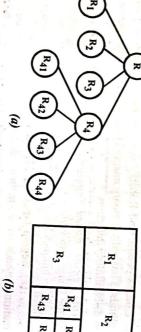


Fig. 2.19 Division of Regions Based on Quad Tree

algorithms to find clusters. There are basic two types of clustering an objective function. In between these two methods there are various side the partition based methods use optimization methods iteratively to minimiz the whole database and the internal nodes represent the clusters. On the other methods are based on the concept of trees. In this the root of the tree represent methods - hierarchical method and partition based method. The hierarchical similar to each other than others. There are two basic categories of clustering pixels with similar characteristics. Data clustering is the method that divide techniques are the techniques, which segment the image into clusters having the data elements into clusters such that elements in same cluster are mon (iv) Clustering Based Segmentation Method - The clustering base

An example of a hard clustering based technique is one k-means clustering either I or 0 i.e., one either certain pixel can belong to particular cluster or not exactly one cluster. These methods use membership functions having value to only one cluster. In other words it can be said that each pixel can belong that divides the image into set of clusters such that one pixel can only below (a) Hard Clustering - This is a simple clustering technique

> on partial membership i.e., one pixel can belong to more than one clusters and Thus soft clustering techniques are most useful for image segmentation in more flexible than other techniques. this degree of belonging is described by membership values. This technique is which division is not strict. The example of such type of technique is fuzzy cbecause in real life exact division is not possible due to the presence of noise. means clustering. In this technique pixels are partitioned into clusters based (b) Soft Clustering - This is more natural type of clustering

are represented as boundaries which are continuous. of basin the adjacent basins are merged together. To maintain separation of topological interpretation. In this the intensity represents the basins having the gradient of image as topographic surface. The pixels having more gradient These dams are constructed using dilation. The watershed methods consider between basins dams are required and are the borders of region of segmentation. hole in its minima from where the water spills. When water reaches the border (v) Watershed Based Methods - These methods uses the concept

noise). The results of the PDE method is blurred edges and boundaries that to reduce the noise from image and the second other PDE method is used to can be shifted by using close operators. The fourth order PDE method is used better detect the edges and boundaries. the edges) and convex non-quadratic variation restoration (used to remove segmentation. These are appropriate for time critical applications. There are basic two PDE methods - non-linear isotropic diffusion filter (used to enhance The partial differential equation based methods are the fast methods of (vi) Partial Differential Equation Based Segmentation Method –

leatures and segmentation by neural network. e. solved using neural network. This method has basic two steps - extracting independent of PDE. In this method the problem is converted to issues which connected nodes and each connection has a particular weight. This method is image from background. A neural network is made of large number of brain for the purpose of decision making. At present this method is mostly ANN based segmentation methods simulate the learning strategies of human used for the segmentation of medical images. It is used to separate the required (vii) Artificial Neural Network Based Segmentation Method - The

Q.25. Give comparison of various segmentation techniques,

Ans. The comparison of various segmentation techniques is given in take

Table 2.2 Comparison of Various Segmentation Techniques

Fig.			THE PERSON NAMED IN CO.		
F:-			decision making	The state of the s	1
	0	163, 1700	learning process for	50 BC 10 BC	
	in training.	plex programs.	on the simulation of	method	_
	More wastage of tim	No need to write com-	This method is based	(VII) ANN based	(<u>I</u>
		cations.	erential equations.		
	complexity.	for time critical appli- complexity.	on the working of diff-	method	
	More computation	Fastest method, best	This method is based	sed	(IA)
		are continuous.	tation.		;
	gradients.	detected boundaries	on topological interpre-	method	v _
	Complex calculation	Results are more stable,	This method is based	ed	3
	2000	real problems.			
	easy.	fore more useful for	geneous clusters.		11
	ship function is no	membership there-	division into homo-	method	
	Determining member	Fuzzy uses partial	This method is based on	ng	(3
		similarity criteria.	gions.	,	
	mory.		into homogeneous re-		3,
e_/	terms of time and me	noise, useful when it	on partitioning image	method	y- 1
	Expensive method	More immune to	This method is based	Region based	(III)
interi	edges.	between objects.	tion.		
Shoul	detected or too man	ing better contrast	on discontinuity detec-	method	
	Not suitable for wrom,	Good for images hav-	This method is based	Edge based	Ξ
and I	Acres 1		values.		
	considered		particular threshold		.:
wher	spatial details are no	method	of the image to find		
Total C	dependent on peak	information, simplest	on the histogram peaks	method	
	This method, high	No need of previous	This method is based	Thresholding	Θ
Junio	Disadvantages	Advantages	Description	Technique	ı.
				Segmentation	S

Q.26. Discuss about the connected components.

Ans. A set of pixels in which each pixel is connected to all other pixels called a connected component.

The set of all connected components of \overline{A} (the complement of A) that have points on the border of an image is called the background. All other components \overline{A} are called holes. Let us consider the simple picture shown below —

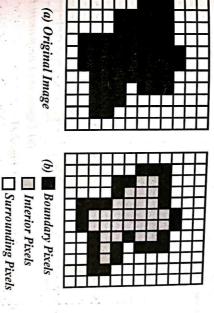


If we consider 4-connectedness for both foreground and background, there are four objects that are 1 pixel in size and there is one hole. If we use 8-connectedness, then there is one object and no hole. Intuitively, in both cases we have an ambiguous situation. A similar ambiguous situation arises in a simple case like —

0 1 0

re if the 1s are connected, then the 0s should not be

To avoid this situation, different connectedness should be used for objects background. If we use 8-connectedness for A, then 4-connectedness ld be used for \overline{A} . An example of a simple binary image with its boundary, ior and surrounding is shown in fig. 2.20.



g. 2.20 A Binary Image with its Boundary, Interior, and Surroundings

The boundary of A is the set of pixels of A that have 4-neighbours in A. The boundary is usually denoted by A'. The interior is the set of pixels of A that are not in its boundary. The interior of A is (A - A'). Region \mathbb{T} surrounds region A (or A is inside T), if any 4-path from any point of A to the border of the picture must intersect T.

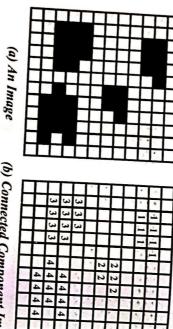
Q.27. Explain the term connected components labeling.

Ans. "A connected components labeling of a binary image B is a labeled image LI in which the value of each pixel is the label of its connected component".

One of the most common operations in machine vision is finding the connected components in an image. The points in a connected component form a candidate region for representing an object. As mentioned earlier, in computer

components must be determined. image and the object properties and locations need to be found, then the connections for finding the connected compoents; however, if there are many objects in the found then the operation. If there is only one object in an image, then there may not be any in nature, because the operation of finding connected components is a blue in a chief in an image, then there may not to be a blue in an image. usually form a bottleneck in a binary vision system. The algorithm is sequentially form a bottleneck in a binary vision system. The algorithm is sequent spatially crose pourses...... components in digital images. However, the connected component algorithm is a binary vision system. The algorithm is a solution by the connected component algorithm is a binary vision system. spatially close points. The notion of "spatially close" is captured by connected component of the connected conn vision most objects have surfaces. Points belonging to a surface project of "spatially close" is captured by a surface project of the notion of "spatially close" is captured by a surface of the notion of th

orientation, and bounding rectangle of the components while lebeling the applications, it is desirable to compute characteristics such as size, postion (a) and (b) shows an image and its labeled connected components. In me image and assigns a unique label to all points in the same component. Fig. 23 A component labeling algorithm finds all connected components h



(b) Connected Component Image

Q.28. Explain the recursive connected component algorithm.

component at a time, but can move all over the image while doing so. can fit in memory and employ a simple, recursive algorithm that works on one component labeling operation. Some algorithms assume that the entire image Ans. There are a number of different algorithms for the connected

become the labeled image. Then the process of finding the connected inputs the binary image B and outputs the negated image Ll, which will component label 1. This can be done using a function called negate that This is needed to distinguish unprocessed pixels (- 1) from those of of its connected component. The strategy, adapted from the Tanimoto Al text, is to first negate the binary image, so that all the 1-pixels become -1's produce a labeled output image LI in which every pixel is assigned the label + 1 columns. We wish to find the connected components of the 1-pixels and Suppose that B is a binary image with MaxRow + 1 rows and MaxCol

components becomes one of finding a pixel whose value is -1 in Ll, assigning value 1 and recursively repeat the process for these neighbours. The utility it a new label, and calling procedure search to find its neighbours that have neighbourhood or 8-neighbourhood definition. Only neighbours that represent returns the set of pixel positions of all of its neighbours, using either the 4 function neighbours (L, N) is given a pixel position defined by L and N. II in scan-line order as shown in fig. 2.22. legal positions on the binary image are returned. The neighbours are returned

	2	
4	*	_
	w	

(a) Four-neighbourhood (b) Eight-neighbourhood

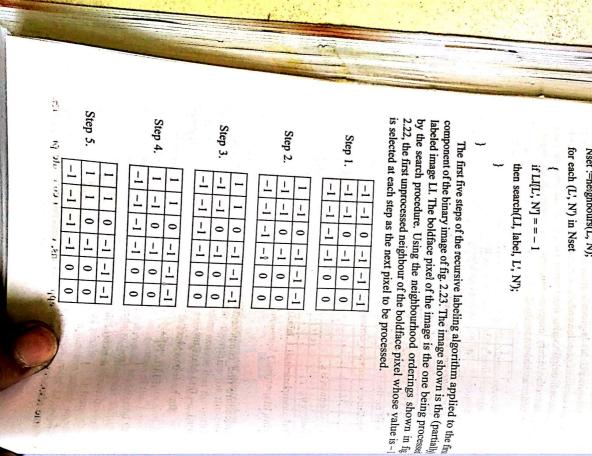
Fig. 2.22 Scan-line Order for Returning the Neighbours of a Pixel

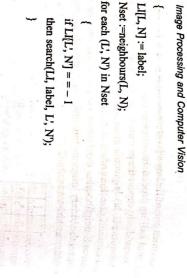
connected components of a binary image. Here, B is the original binary image and LI will be the labeled connected component image Algorithm for Recursive Connected Components - Compute the

procedure recursive_connected_components (B, LI);

```
print(LI);
                                                                                                                                                                                                                                                                                                                                LI := negate(B);
                                                                                                                                                                                                                                                                          find_components(LI, label);
                                                                                                                                                                                                                                                                                                       label := 0;
                                                                                                                                                                                             procedure find_components(LI, label);
                                                                                                                                          for L := 0 to MaxRow
                                                                                                               for N := 0 to MaxCol
                                                                                  if LI[L, N] = -1 then
search(LI, label, L, N);
                              label := label + 1;
```

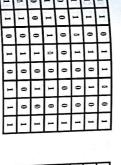
procedure search(LI, label, L, N);





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(a) Binary Image

(b) Connected Components Labeling



(c) Binary Image and Labeling, Expanded for Viewing

Fig. 2.23 A Binary Image with Five Connected Components of the Value I

Q.29. Write short note on row-by-row labeling algorithm.

connected components algorithm for graphs, was described in Rosenfeld and equivalences are found, has been widely used in computer science applications. each temporary label by the label of its equivalence class. In between the two to determine the equivalence classes of the relation. Since that time, the unionrecord equivalences and assign temporary labels and the second to replace Pfaltz in 1966. The algorithm makes two passes over the image - one pass to structure is a useful improvement to the classical algorithm. of equivalence classes represented by tree structures. The addition of this data find algorithm, which dynamically constructs the equivalence classes as the passes, the recorded set of equivalence, stored as a binary relation, is processed The union-find data structure allows efficient construction and manipulation Ans. The classical algorithm, deemed so because it is based on the classical

Q.30. Discuss about the hierarchical image representation.

multiple resolutions. In many applications, one can compute properties of array, some data is lost, making it more difficult to recover information. requirements. Hierarchical representation of images allows representation at However, reduction in resolution results in reduced memory and computing resolutions. By reducing an image's resolution, i.e. reducing the size of the Ans. In segmentation an image can be represented at many different

Unit - 11 83

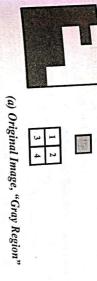
a selected area of the image at a higher resolution. Hierarchical representation as elected area of the image at a higher resolution. Hierarchical representation as elected area of the images. Two commonly used forms of him. representations are pyramids and quad trees. a selected at the sure of his selected at the sure also used for browsing in images. Two commonly used forms of his are also used for browsing in images. Two commonly used forms of his are also used for browsing in images. Two commonly used forms of his are also used for browsing in images. images first at a low resolution and then perform additional computations on the first at a low resolution and then perform additional computations on the first at a low resolution and then perform additional computations on the first at a low resolution and then perform additional computations of the first at a low resolution and then perform additional computations of the first at a low resolution and then perform additional computations of the first at a low resolution and then perform additional computations of the first at a low resolution and then perform additional computations of the first at a low resolution and then perform additional computations of the first at a low resolution and then perform additional computations of the first at a low resolution and the first at a low resolution at a low

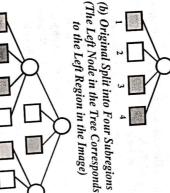
possible to taper the pyramid in nonlinear ways. devise other strategies to form reduced-resolution versions. Similarly, it is single pixel at the top level, level 0, and the bottom level is the origin several pixels in the image at level l+1. The whole image is represented as of an image, the pixel at level *l* is obtained by combining information from averaging the gray values in 2×2 neighbourhoods. It is possible however, in a pyramid is shown in fig. 2.24. Here the pyramid is obtained by simply represented by several pixels at the next level. An image and its reduced version (unreduced) image. A pixel at a level represents aggregate information the other images are n/2 × n/2, n/4 × n/4, 1 × 1. In a pyramid representation the image and k reduced versions of the image. Usually n is a power of 2 and world 1 x 1. In a novramid representation Pyramids - A pyramid representation of an n × n image contain

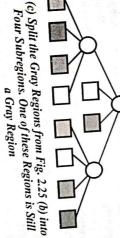
of size 2(2^{2×level}). An implementational point is that the entire pyramid fits into a linear array

Level 3 Level (log2n) Level 2

fig. 2.25. For each subregion, if all points in the region are either white or A region in an image is split into four subregions of identical size, as shown in is represented in a tree structure. The splitting process is repeated until there contains pixels of both kinds, it is considered to be a "gray region" and is black, then this region is no longer considered as a candidate for splitting, if it further split into four subregions. An image obtained using this recursive splitting







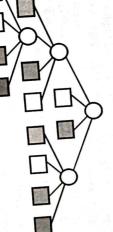


Fig. 2.25 The Building of a Quad Tree (d) Splitting of the Last Gray Region and the Final Quad Tree

black and gray. A quad tree is obtained by requ

pyramids for binary images. A quad tree contains three types of nodes - white,

itting of an image

(ii) Quad Trees - A quad tree may be considered as an extension of

Fig. 2.24

or has four children - thus the name quad tree. are no gray regions in the tree. Each node in this structure is either a leaf not Quad trees are finding increasing application in spatial databases. Several

properties have also been developed. and a quad tree to a raster array. Algorithms for computing several pictorial algorithms have been developed for converting a raster array to a quad to

versions are successively obtained by averaging four points. Fig. 2.24 the original image is a 512 × 512 image, its reduced-resolution

Q.31. Write short note on spatial clustering.

a technique is called spatial clustering. In essence, spatial clustering scheme spatial linkage technique. combine the histogram mode seeking technique with a region growing or combining clustering in measurement space with spatial region growing. Such Ans. It is possible to determine the image segments by simultaneous

probability is not larger than the probability of the value of the pixel we are is close enough in measurement space to the value of the pixel and if its growing from) if the value of a neighbour (an N-tuple for an N band image a neighbour of this pixel (in general, the neighbours of the pixel we are value is on the current peak. Consider for possible inclusion into this segment performed in the following manner. Initially, each segment is the pixel whose both spatial and measurement space region growing are simultaneous determining all pixel locations having a measurement on the peak. Next beginning with a pixel corresponding to the highest peak not yet processed locating, in turn, all the peaks in the measurement space histogram, and the According to Haralick and Kelly, segmentation can be done by first

of these 4 great-grandparents then there are at most 4 segments which are the respective great-grandchildren converge. If the top layer of the pyramid is a 2 × 2 block of great-grandparents. converge reasonably quickly and for the same reason the ISODATA iterations new value is the average of the children to which it is linked, etc. The iterations each of its parent's values and links itself to its closest parent. Each parent's the average of its child pixels. Then each child pixel compares its value with block of parent pixels. The iterations proceed by assigning to each parent pixel parent pixels has 8 child pixels in common. Each child pixel is linked to a 2 × 2 spatially corresponding 4 × 4 block of child pixels. Each pair of adjacent it. Initial links between layers are established by linking each parent pixel to the the number of pixels per row and half the number of rows of the image below image. Each successively higher layer of the pyramid is an image having half ISODATA kind of clustering. The bottom layer of the pyramid is the original Another spatial clustering scheme is a spatial pyramid constrained

Q.32. Explain the method of region splitting and merging for region

smaller quadrant regions so that, for any region R_i, Q(R_i) = TRUE. We begin Q is FALSE for any quadrant, the quadrant is subdivided into subquadrants, and with the whole region. If Q(R) = FALSE, the image is divided into quadrants. If One method for segmenting R is to subdivide it successively into smaller and of quadtrees. Quadtrees represent trees in which each node includes exactly so on. This specific splitting method has a convenient representation in the form only splitting is employed, the final partition includes adjacent regions with identical into four descendant nodes. In this situation, only R4 was subdivided further. If to the whole image, and that each node corresponds to the subdivision of a node properties. By permitting merging as well as splitting, this disadvantage can be four descendants as shown in fig. 2.19. Note that the root of the tree corresponds adjacent regions R_j and R_k are merged only if $Q\ (R_j \cup R_k)$ = TRUE. adjacent regions whose combined pixels satisfy the predicate Q. That is, two remedied. Satisfying the constraints of segmentation requires merging only Ans. Assume that, R is the whole image region and choose a predicate Q

the predicate individually. This results in a much simpler way due to testing of further splitting is carried out. Numerous variations of the preceding the predicate is limited to individual quadregions. This simplification is still fundamental theme are possible. For example, a significant simplification results capable of yielding good segmentation results. if we permit merging of any two adjacent regions Ri and Ri if each one satisfies It is customary to satisfy a minimum quadregion size beyond which no

Q.33. Write down the split and merge algorithm for region segmentation.

are useful for segmenting complex scenes. Domain knowledge may be may be applied to refine the segmentation. Combined split and merge algorithms introduced to guide the split and merge operations. presegmentation based on thresholding, a succession of splits and merges Ans. Split and merge operations may be used together. After a

property defined by a predicate A applied to the region. The predicate represents the similarity between the pixels in a region. For example, the predicate could 2,, m. All of the pixels in a region will be homogeneous according to some be defined using the variance in gray values within a region -Suppose that an image is partitioned into a set of regions, $\{R_n\}$, for n=1,

A(R) =1 if the variance is small

Algorithm for Split and Merge Region Segmentation -

Step 2 - Pick a region R. If A(R) is false, then split the region into four Step 1 - Start with the entire image as a single region.

Scanned with CamScanner

...., R_n in the image. If $A(R_1 \cup R_2 \cup \cup R_n)$ is true, merge the n regions Step 4 - Repeat these steps until no further splits or merges take place Step 3 – Consider any two or more neighbouring subregions, R. R. is true. meron that R. is true.

rules - knowledge rules, the control rule and the highest rules. According to this approach, the model stored in the LTM has three levels $_{
m 0f}$ the rule fires, and an action, usually involving data modification is performed rules in the LTM against the data stored in the STM. When a match occurs about low-level segmentation and control strategies. A system process matches output. Other hand, LTM contains the model representing the system knowledge i.e., the long term memories (LTM) and short term memories (STM). The short term memories holds the input image, the segmentation data and the analyzer, the focus of attention, the scheduler, and two associate memories (CTAA) processes such as the line analyzer, the initializer, the region analyzer, the area ochadular and two accordate more the area. and Levine in 1984. According to this approach, system contains a Set of Ans. A rule based expert system for segmentation introduced by Near Q.34. Discuss about the rule based segmentation in image segmentation

extending a line, merging two lines, and modifying focus of attention area. actions include splitting a region, merging two regions, adding, deleting or regions, lines, and area in the form of situation-action pairs. The specific Knowledge Rules - Encode information about the properties of

they alter the matching order of different knowledge rule sets. that their actions don't modify the data in the short term memory. Instead, control the focus-of-attention strategy. The inference rules are metarules in data entry to be considered, a region, a line, or an entire area. These rules focus-of-attention and inference rules. Focus-of-attention rules find the next (iii) Highest Rule Level - These rules are strategy rules that select (ii) Control Rules - These rules are divided into two categories -

a given set of data. the set of control rules that executes the most appropriate control strategy for

allow more specific strategies to be incorporated without changing the code. feature values. Rule based segmentation is useful because it is general but optional DIFFERENCE qualifier that applies the operation to differences in feature of this data entry, fourth, an optional NOT qualifier, and last fifth, an denoting the data entry on which the condition is to be matched. Third, a depicting a logical operation to be performed on the data, second, a symbol Q.35. Describe the motion based segmentation. The conditions of the rules base are made up of first, a symbolic qualifier

animals to extract objects or regions of interest from a background of irrelevant Ans. Motion is a very powerful cue used by humans and many other

> mage components. elements, leaving only nonzero entries that correspond to the non stationary procedure for doing this is to form a difference image. Assume that we have times of and of respectively, is to compare the two images pixel by pixel. One segmentation, we used spatial techniques. One of the simplest approaches for the sensus navigation and dynamic scene analysis. The use of motion in autonomous new used spatial techniques. One of the simplest and the sensular techniques. bject results in the difference of the two images canceling the stationary mage against a subsequent image of the same scene, but including a moving a reference image containing only stationary components. Comparing this described a respectively, is to compare the two images.

A difference image between two images taken at times c; and c; may be

$$D_{ij}(a, b) = \begin{cases} 1, & \text{if } |f(a, b, c_i) - f(a, b, c_j)| > T \\ 0, & \text{otherwise} \end{cases}$$
...(i)

mages in the sequence. these images, so that the difference image $D_{ij}(a, b)$ is of the same size as the that the values of the coordinates (a, b) in equation (i) span the dimensions of threshold T. It is assumed that all images are of the same size finally we note appreciably different at those coordinates, as determined by the specified coordinates (a, b) only if the intensity difference between two images is Here, T is a specified threshold. D_{ij}(a, b) has a value of 1 at spatial

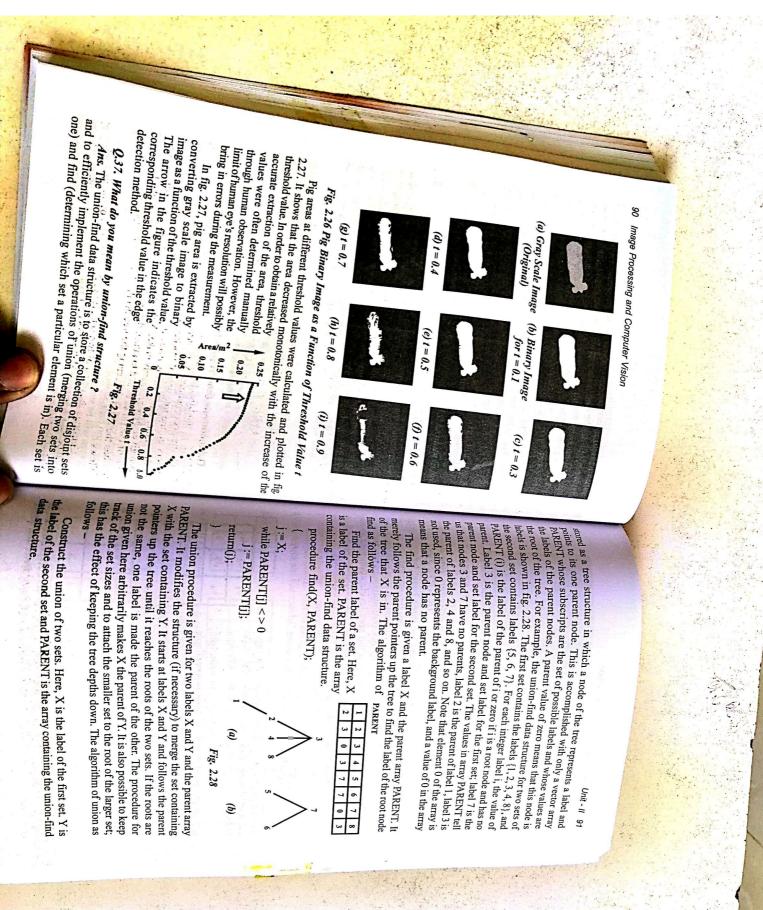
REA EXTRACTION — CONCEPTS, DATA STRUCTURES, EDGE NE LINKING, HOUGH TRANSFORM, LINE FITTING, CURVE FITTING (LEAST-SQUARE FITTING)

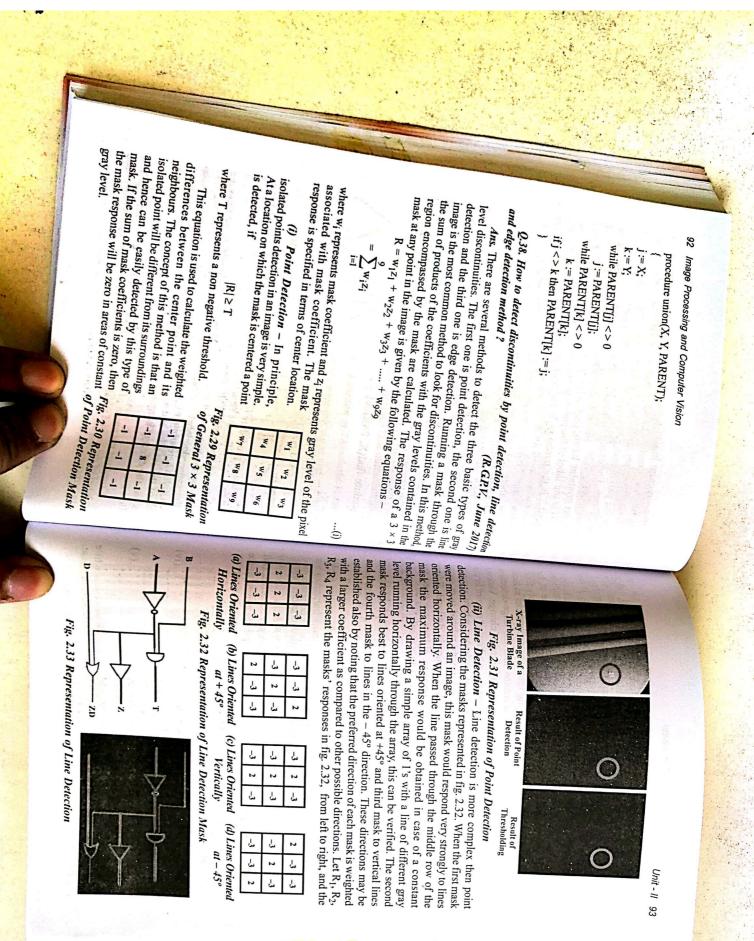
Q.36. How do threshold values affect conventional area extraction?

causing the calculated pig area to be larger than the actual area. Fig. 2.26 shows the binary images of a pig corresponding to different threshold values. some brighter parts of the environment could be counted as part of the pig. Pig area will be smaller than the actual area. If the threshold value is too low, Value is too high, some darker parts of the pig will be missing, so the calculated o convert the gray scale image to binary image by setting a threshold value. neshold value is critical in determining the area of the pig area. If the threshold ne shape of the animal on a black background. However, the selection of the man it, the result would be an image showing a white blob corresponding to With pixel values greater than the threshold value separated from those lower Ans. In image processing, the conventional method for extracting area is

deball. In imaging application motion arises from a relative displacement between

deall. In system and the scene being viewed such as in robotic applications the sensing system and dynamic scene analysis. The manifer pavigation and dynamic scene analysis.





points correspond nearest to the direction specified by the mask. The remaining points are strongest responses for one pixel thick line. They direction, the mask attached with that direction is used and its output is threshold the direction is used and its output is threshold the direction is used and its output is threshold the direction is used and its output is threshold the direction. certain point in the image the point is said to be more likely associated with four masks are run individually through an image. If $|R_i| > |R_j|$, for all j * iline in the direction of mask i. Alternatively, for detecting lines in a particular to the direction is used and its outnotice that the direction is used to the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice that the direction is used to the direction its outnotice th

characterise object boundaries typically in images. Edges are used for edge detectors work based on calculating the intensity gradient at a point in the identification, segmentation and registration of objects in a scene. change in intensity encounters. These changes are mostly related with some physical boundary in the scene from which the image is derived. Edge image. Edge detection is used to recognize areas of an image where a major the border between different objects. Determining intensity differences in logical transferences central tasks of the lower level. Points where brightness changes sharply form algorithm should look for a neighbourhood with strong signs of change. Various image regions such points can be detected. It means that the edge-detection in an image is known as edge detection. In image processing, it is one of the (iii) Edge Detection - The process of obtaining meaningful transition

The methods of edge detection are as follows -

difference. Assume the pixels arrangement with respect to the central pixel (a) Prewitt Mask - It uses the basic concept of central

a₇ [i, j] a₃ a₁ a₂

The Prewitt edge detector partial derivatives are computed as given below- $G_X = (a_2 + Ca_3 + a_4) - (a_0 + Ca_7 + a_6)$

centre of mask. G_X and G_Y represents the approximations at [i, j]. The constant C represents the emphasis provided to pixels nearer to the $G_Y = (a_6 + Ca_5 + a_4) - (a_0 + Ca_1 + a_2)$

Putting C = 1, the Prewitt edge detector mask becomes

...(17)

averages in other direction. Hence, edge detector is less vulnerable to noise. The Prewitt edge detector masks have longer support The Prewitt edge detector mask differentiates in one direction while

...(v)

approximations to first derivatives of Gaussian kernels. basic during averaging. The Sobel mask can be considered as 3 × 3 basic concept of central differences but gives greater weight to the central For the pixels arrangement shown in equation (i), Sobel edge detector (b) Sobel Mask - It was developed by Irwin Sobel. It uses the

artial derivatives are computed as given below -

The Sobel edge detector mask is as follows - $G_Y = (a_6 + 2a_5 + a_4) - (a_0 + 2a_1 + a_2)$ $G_X = (a_2 + 2a_3 + a_4) - (a_0 + 2a_7 + a_6)$...(vi)

...(viii)

...(ix)

the Prewitt mask The noise suppression feature of a Sobel mask is better as compared to

Q.39. Explain the difference between edge and line with graph (R.G.P.V., May 2019)

Ans. Refer to Q.38.

in the image. These features are usually termed as local features, since they two plots of agricultural land, bearing the same vegetation. A point is embedded are extracted from the local property alone. Though the edges and lines are single uniformly homogeneous region. For example, a thin line may run between wo different regions. A line, on the other hand, may be embedded inside a both detected from the abrupt change in the gray level, yet there is an important ustnetly different regions, which means that an edge is the border between ifference between the two. An edge essentially demarcates between two Edges, lines, and points carry a lot of information about the various regions

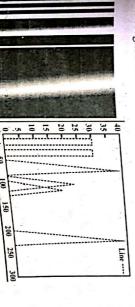
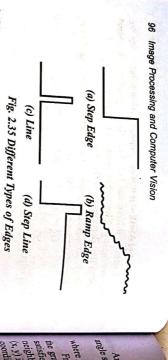


Fig. 2.34 Edge Profile of One Ross of a Synthetic Image



step line, are shown in fig. 2.35. forms and nature of ideal edges and lines, such as step edge, ramp edge, line ramp edge are shown in the form of an edge profile in fig. 2.34. The diverge a spike. The changes in the gray levels in case of a perfect step edge, line average gray value of the region in which it is embedded. This is analogous to inside a uniformly homogeneous region and its gray value is different from the

Q.40. Explain local analysis method of edge linking and boundary detection

detection algorithms are followed by edge linking methods. discontinuities. Hence, to assemble edge pixels into meaningful edges, edge nonuniform illumination and other effects which result in spurious intensiv seldom characterizes an edge completely due to noise, breaks in the edge from Ans. Ideally, pixels lie only on edges but in actual practice, set of pixels

properties for establishing similarity of edge pixels in this analysis all similar points are linked, developing an edge. There are following two simple method for linking edge points. According to a set of predefined critera, of pixels in a small neighbourhood about every point (x, y) in an image is the Local Processing Method of Edge Linking - Analyze the characteristics

The strength of the gradient operator response is used to generate

(ii) Gradient vector direction.

An edge pixel with coordinates (x_0, y_0) in a predefined neighbourhood of The value of ∇x provides first property as given below - $\nabla x \approx |G_X| + |G_Y|$

(x, y), is similar in magnitude to the pixel at (x, y), if $|\nabla x(x, y) - \nabla x(x_0, y_0)| \le E$

:.(ii)

where E represents non-negative threshold

Following expression represents the direction of the gradient vector

 $\alpha(x, y) = \tan^{-}$

angle same as to the pixel at (x, y), if where A is a non-negative angle threshold. An edge pixel at (x_0, y_0) in the predefined neighbourhood of (x, y) has an $|\alpha(x, y) - \alpha(x_0, y_0)| < A$ Unit - 11 97 :. (¥)

the image, this procedure is the linked points as the center of repeated. To maintain a record of hbourhood of coordinates is linked to the pixel at that ed, a point in the predefined inates. At every position in com equation (iii), we can see the direction of the edge is perpendicular to dient vector direction at (x, y). If direction and magnitude criteria are



one pixel to another pixel assign ghbourhood is shifted from Fig. 2.36 Representation of Edge Linking

a different gray level to each set

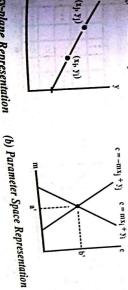
of linked edge pixels.

eoretic techniques. Q.41. Discuss global processing via Hough transforms and graph (R.G.P.V., June 2017,

Ans. Global Processing via Hough Transform – This method was developed by Hough in 1962. At a point (x_p, y_i) the general equation of a straight line in slope-intercept form is given below $y_i = mx_i + c$

nd c, they all satisfy the equation (i). Equation (i) can also be written as Generally, infinite lines may pass via point (xi yi). For varying values of m $c = y_i - mx_i$

(x, y). In addition, a second point (xj, yj) also has a line in parameter space with (x, y). Where a' represents the slope and b' represents intercept of the Assume that mc-plane provides equation of a single line for a fixed pair ected with it. And at a point (a', b') this line intersects the line associated $c = -mx_i + y_i$..(II)



:. (iii)

from 0 to n plus an estimate of cost of that path from n to a goal node i.e. from the start node o to a goal node, where the path is constrained to go via node or the cost of a minimum of via node or the cost of the cost of the cost of a minimum of via node or the cost of the co of finding. Let, r(n) represents an estimate of the cost of a minimum cost line of the cost line of the cost of the cost line of the cost of the cost line shows a class of method which use heuristics in manner to decrease the esting the cost of a minimum control of the cost of a minimum This cost may be defined as an estimate of the cost of a minimum Cost May the method has to sacrifice optimally for the sake of speed. Following algorithms heuristics in manner to decrease the Generally, problem of obtaining a minimum cost path is not trivial. Typically

uses r(n) as the basis for performing a graph search using any available heuristic information we can obtain h(n). Following algoritm Here g(n) represents the lowest cost path from o to n found so far, and

Indicate the start node open and set g(0) = 0.

n is smallest. (iv) Indicate closed the open node n IF estimate r(n) of open nodeExit with failure if no node is open else continue.

pointers IF n is a goal node ELSE continue. (v) Exit with the solution path achieved by tracing back through the

successors then (GoTo) step (iii). (vi) Expand node n, producing all of its successors. IF there are no

(vii) IF a successor n; is not indicated, set

and indicate it open, and direct pointers from it back to n. $r(n_i) = g(n) + c(n, n_i)$

(viii) IF a successor n; is indicated closed or open, update its value by-

Indicate open those closed successors whose g'values were thus lowered $g'(n_i) = \min[g(n_i), g(n) + c(n, n_i)]$

and redirect to n the pointers from all nodes whose g' values were lowered

This algorithm does not provide guarantee that a path find by it is minimum-

cost path.

y = mx + c

Q.42. Explain the term line fitting.

for all points on the curve is to perform a least-squares fit of a line to the points error with respect to the fit. A popular way to achieve the lowest average error corner. However, this may result in some portions of the curve having large intersection of them was taken as the corner location. This yields a sharper 2.41 (c), a least squares fit was performed to two sets of points, and the to connect, but the corner angle is not as sharp as intended in the original. In fig. (b), the fit is made exactly on data points. Because of this, the endpoints are sure in fig. 2.41 (a) and two corner fits are shown in fig. 2.41(b) and (c). In fig. 2.41 endpoints of the curve as the straight line endpoints. On-valued pixels are shown Ans. A simple way to fit a straight line to a curve is just to specify the

C = - m + 1

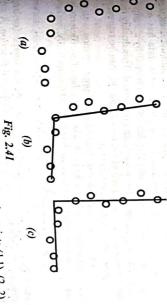
1 = m + c For (1, 1) y = mx + cStep 1 -

(m, c) = (1, 1)

on the current so determine of the form the data points, (x_i, y_i) . The least square fit is made by minimizing of errors, $\Sigma(y - y_i)^2$ over all data points, i = 1of the curve. For a line fit of equation, y = mx + c, the objective is to determine the data points, (x_i, y_i) . The least square fit is made to mand of errors, $\Sigma(y-y_i)^2$ over all data points, i=1,...,n. The solution is the simultaneous equations. be sum v. solving the simultaneous equations, $\Sigma y_i = m\Sigma x_i + cn$, and found by solving the simultaneous equations, $\Sigma y_i = m\Sigma x_i + cn$, and

found by $\frac{1}{2} + c\Sigma x_i$, for all data points, i, to obtain m and c.

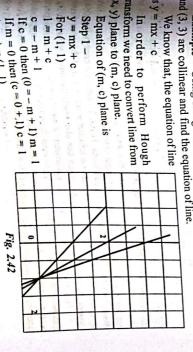
If there can be a problem in blindly applying the least-squares method just there can be a problem and continuous analysis and the continuous analysis analysis analysis and the continuous analysis analysis analysis analysis. perpendicular distance to the line in any orientation. This can be done by a line-fiting method called principal axis determination or eigenvector line fitting. approach is to minimize error not with respect to x or y, but with respect to the refor for slopes expected to be ± 45 degrees around the vertical. A more general only for slopes expected to be ±45 degrees around the horizontal and to minimize of orientation, and as the true slope of the line approaches vertical, this method of described to document analysis applications. That is, the method is not independent ming y-error becomes inappropriate. One approach is to minimize y-error



0 0

0

Example - Using Hough transform show that the points (1,1), (2, 2),



can be generalized for higher-order polynomials. A related quad tree approach system. In fact, the selection of the origin can also affect the range values of c. by quantizing a and b, the block center was selected as the origin of the coordinate describing the sizes of the compressed blocks. To reduce the error energy imposed resulting error was less than a prescribed threshold. A PSNR of 32 dB was reported for 16:1 compression (0.5 bpp) with high complexity in building the quad tree the minimization procedure, usually 8×8 or 16×16 , were retained whenever the N counterparts and were assumed uniformly distributed. The resulting values of derivation of first order (plane) fitting was proposed as component) and z(x, y) is the value from the suggested function. A simplified where g(x, y) is the original intensity value of the image (or any color to represent all pixels in the block of the image. Mathematically, we have The computation of $2N \times 2N$ parameters from their $N \times N$ counterparts as an optimization algorithm where only a small number of coefficients is enough 2D mathematical expression (z(x, y)). the image or block (small part) of the image (g(x, y)) can be represented as a such as the digital image that is saved and processed. This duality means that dimensions. The 2-dimensional (2D) data is represented by a matrix of datarepresent gathered random data into a group. This data has one or t_{W0} The coefficients a, b and c of a $2n \times 2N$ block are computed from their $N \times 2N$ points (1,1), (2,2), and (3,3) are collinear. (y = mx + c) put the value of m and c on this To achieve data compression, least squares approximation was presented If (x,y) = (3,3) then (m, c) = (1,3)If (x,y) = (2,2) then (m, c) = (1,2)Ans. Curve-fitting refers to the use of a mathematical expression to 102 Image Processing and Computer Vision Q.43. Describe the curve fitting of image. Step 3 - The original equation of line is Plot a graph for (m, c) = (1, 1), (1, 2)Step 2 -Similarly for $\min_{\mathbf{a},\mathbf{b},c} \sum \sum [ax + by + c - g(x,y)]^2$ $\min \sum \sum [z(x,y) - g(x,y)]^2$ Fig. 2.43 set of properties for each region. The in the property of the

EGION ANALYSIS - REGION PROPERTIES, EXTREMAL POINTS, SPATIAL MOMENTS, MIXED SPATIAL **GRAY-LEVEL MOMENTS**

Q.1. Write down some basic properties of region.

procedures that perform decision-making tasks such as recognition or inspection. Most image processing packages have operators that can produce Ans. The properties of the regions become the input to higher level

Some basic properties of regions are as follows -

centroid denoted by (r_e, c_e) . The area of region defined as -The simplest geometric properties are the region's area denoted by A and the (1) Area of Region - We denote the set of pixels in a region by RE.

$$A = \sum_{(r_e, c_e) \in R_E}$$

It means the area is just a count of the pixels in the region Re-

average' location of the pixels in the set Rg. The centroid is defined as (ii) Centroid of Region - The centroid of region (re, ce) is thus the

The solution of the second contains
$$\frac{A}{(c_{c},c_{c})}$$
 and $\frac{A}{(c_{c},c_{c})}$ and $\frac{A}{($

generally not a pair of integers, often a precision of tenths of a pixel is justifiable for the centroid. Note that, even though (re, ce) \(\in \text{RE} is a pair of integers (re, ce) is

corners were used in the decoder to find the coefficients of (dxy+ax+by+c). was proposed to predict block corners from the upper left one. These four

4-connectivity is used to determine whether a pixel inside the region is Similarly, the resulting set of perimeter pixels well be 8-connected, what whether a pixel inside the region is connected to a pixel outside the region is connected to a pixel outside the region. perimeter pixels will be 4-connected, when 8-connectivity is used to determine connected to a nixel outside to neighbouring pixel that is outside the region. For example, the resulting sequence of the result is denoted by PE, and a pixel of a region is a border pixel if it has some is denoted by PE, and a pixel of a region. For example, the results some region without holes is the set of its interior border pixels. Perimeter of legion is a border pixel if it has been decided by the set of the s (iii) Perimeter of Region - A simple definition of the perimeter of the interior border pixels. Perimeter of

The 4-connected perimeter P_{E_4} and the 8-connected perimeter $P_{E_8 \mid a_e|}$

$$P_{E_4} = \{(r_e, c_e) \in R_E | N_8 (r_e, c_e) - R_E \neq \emptyset\}$$
 $P_{E_8} = \{(r_e, c_e) \in R_F | N_F (r_e, c_e) - R_E \neq \emptyset\}$

Here N is the number of connections. $P_{E_8} = \{(r_e, c_e) \in R_E | N_4 (r_e, c_e) - R_E \neq \emptyset \}$

neighbours, including the first and last pixels. Then the perimeter length $|P_E|$ is perimeter P_E , the pixels in P_E must be ordered in a sequence $P_E = <$ (r_{c_0} , c_{c_0}). "", (fem-1, cem-1) >, each pair of successive pixels in the sequence being (iv) The Perimeter Length of Region – To compute length $|P_E|_{0}$

$$\begin{split} |P_{E}| &= |\{m \,|\, (r_{e_{m+1}}, c_{e_{m+1}}) \in N_{4}(r_{e_{m}}, c_{e_{m}})\}| \\ &+ \sqrt{2} \,|\, \{m \,|\, (r_{e_{m+1}}, c_{e_{m+1}}) \in N_{8}(r_{e_{m}}, c_{e_{m}}) \\ &- N_{4}(r_{e_{m}}, c_{e_{m}})\}| \end{split}$$

of circularity of the region is the length of the perimeter squared divided by the Here, m+1 is computed modulo M, the length of the pixel sequence. (v) The First Circularity Measure of Region - A common measure

$$C_1 = \frac{|P_E|^2}{A}$$

for vertical or horizontal moves and $\sqrt{2}$ for diagonal moves of its 4-neighbouring border pixels or as the length of the border, counting or diamonds depending on whether the perimeter is computed as the number digital circles, as it would for continuous planar shapes, but for digital octagons However, for digital shapes, |PE|²/A assumes its smallest value not for

> replacify measure in 1974 to overcome the first circularity measure as defined as – assuments. The second circularity is defined as -(vi) The Second Circularity Measure of Region – Haralick proposed

 $C_2 = \frac{\mu_{R_E}}{\sigma_{R_E}}$

from the centroid of the shape to the shape boundary. Circularity measure can be computed by mean radial distance and standard deviation of radial distance formulae. They are defined below -Here, μ_{RE} , σ_{RE} are the mean and standard deviation of the distance

Mean Radial Distance - The mean radial distance is defined as -

$$\mu_{R_{\rm E}} = \frac{1}{M} \sum_{m=0}^{M-1} \lVert (r_{e_m}, c_{e_m}) - (\overline{r_e} - \overline{c_e}) \rVert$$

Standard Deviation of Radial Distance - The standard deviation of

radial distance is defined as - $\sigma_{R_E} = \sqrt{\frac{1}{M} \sum_{m=0}^{M-1} [|| (r_{e_m}, c_{e_m}) - (\overline{r_e} - \overline{c_e}) || - \mu_{R_E} ||^2}$

as the digital shape becomes more circular and is similar for digital and $P_{\rm E}$ of the region. The second circularity measure C_2 increases monotonically continuous shapes. Here, the set of pixels (r_{e_m}, c_{e_m}) , m = 0, M - 1 lie on the perimeter

Q.2. Explain the term extremal points in region properties.

digitization or quantization, the standard Euclidean distance formula will provide length and orientation. Because the extremal points come from a spatial extremal points defines an axis. Useful properties of the axis include its axis (BR), bottommost left (BL), leftmost bottom (LB), leftmost top (LT) and right (TR), rightmost top (RT), rightmost bottom (RB), bottommost right there can be as many as eight distinct extremal pixels to a region - topmost touches its topmost, bottommost, leftmost, and rightmost points. In fig. 3.1, a rectangle with horizontal and vertical sides that encloses the region and ustances that are biased slightly low. L with BR, TR with BL, RT with LB and RB with LT. Each pair of opposite ounding box of the region. Extremal points occur in opposite pairs such as pmost left (TL). Each extremal point has a extremal coordinate value in ner its row or column coordinate position. Each extremal point lies on the Ans. Extremal points is the main properties of region. A bounding box is

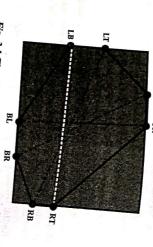


Fig. 3.1 The Eight Extremal Points of Region

account for this. The increment depends on the orientation angle θ of the a_{Ris} calculation for distance adds a small increment to the Euclidean distance $\mathfrak{h}^{\,l}$ a length of 2 but the distance between the pixel centers is only 1. The appropriate adjacent. From the left edge of the left pixel to the right edge of the right pixels For example, let consider the length covered by two pixels horizontally

$$X(\theta) = \begin{cases} \frac{1}{|\cos \theta|} & : |\theta| < 45^{\circ} \\ \frac{1}{|\sin \theta|} & : |\theta| > 45^{\circ} \end{cases}$$

to extremal point (r_{e_2}, c_{e_2}) is defined as – with this increment, the length of the extremal axis from extremal point (r_{e_1} , c_{e_1}) r_{e_2}

Extremal axis length -

 $\mu_{(c_e,c_e)}$, where $\mu_{(t_e,r_e)}$ measures row variation from the row mean, order spatial moments of a region. They are denoted by $\mu_{(t_e,t_e)}, \mu_{(t_e,e_e)}$ and moments are often used to describe the shape of a region. There are three 2nd Ans. Another important region property is spatial moments. Spatial Q3. Write short note on spatial moments region properties. $Y = \left[(r_{e_2} - r_{e_1})^2 + (c_{e_2} - c_{e_1})^2 \right]^{1/2} + X(\theta)$

> The 2nd order row column (mixed) moment is defined as $\mu(r_e, c_e) = \frac{1}{A} \sum_{(r_e, c_e) \in R_E} (r_e - r_e)(c_e - c_e)$

Q.4. Discuss about the mixed spatial gray level moments region

$$\mu_{(r_e,g)} = \frac{1}{A} \sum_{(r_e,c_e) \in R_E} (r_e - r_e) [I(r_e - c_e) - \mu]$$

9

are two 2nd order mixed gray level spatial moments which are defined as -Other gray level properties consist the mixed spatial gray level moments. There

Ans. A simple gray level properties consist gray level mean and variance

 $\mu_{(c_e,g)} = \frac{1}{A} \sum_{(t_e,c_e) \in R_E} [c_e - \overline{c_e}] [I(t_e - c_e) - \mu]$

E

that minimizes, defined by region R_E. The least-squares fit to the observed $I(r_e, c_e)$ is the gray level It gray level intensity planes to the observed gray level spatial pattern of the utensity plane $X(r_e - r_e) + Y(c_e - c_e) + Z$ determined from the X, Y and Z These spatial moments can be used to determine the least squares, best

$$\frac{1}{2} = \sum_{(\mathbf{r}_{e}, \mathbf{c}_{e}) \in R_{E}} \left[X(\mathbf{r}_{e} - \overline{\mathbf{r}_{e}}) + Y(\mathbf{c}_{e} - \overline{\mathbf{c}_{e}}) + Z - I(\mathbf{r}_{e}, \mathbf{c}_{e}) \right]^{2}$$

these partial derivatives to zero leads to the normal regression equation that in Taking partial derivatives of \in^2 with respect to X, Y and Z and setting

measures row and column variation from the centroid

 $\mu_{(e_e,e_e)}$ measures column variation from the column mean and $\mu_{(e_e,e_e)}$

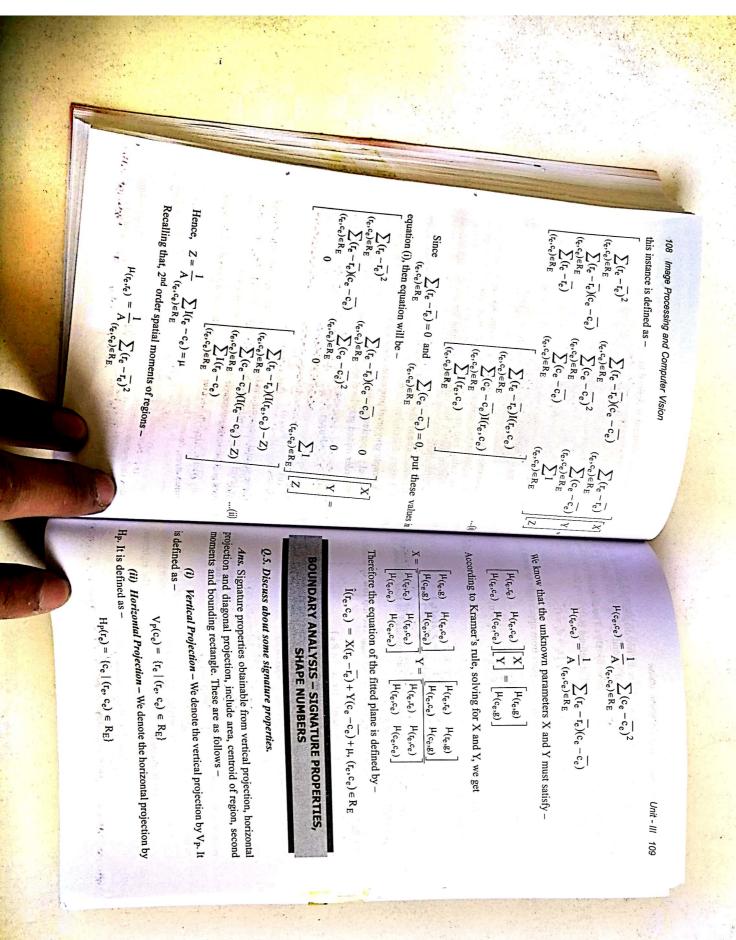
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The 2nd order row moment is defined as - $\mu_{(t_e,c_e)} = \frac{1}{A}\sum_{(t_e,c_e)\in R_E} \iota_e$ $\frac{1}{\Delta} = \sum_{\mathbf{r}_e} (\mathbf{r}_e - \overline{\mathbf{r}_e})^2$

The 2nd order column moment is defined as -

 $\mu(c_e,c_e) = \frac{1}{A} \sum_{(f_e,c_e) \in R_E} (c_e - \overline{c_e})^2$

moments have value and meaning for a region of any shape, the same way invariant to translation and scale change of a 2D shape. The 2nd order spatial probability distribution. that the covariance matrix has value and meaning for any two-dimensional These quantities are often used as simple shape descriptors, as they are





lower right. We denote diagonal projection by D_P : The diagonal $p_{TO[e_0]}$ going from lower left to upper right and second, going from upper left D_{P_L} goes from lower left to upper right, is defined by (iii) Diagonal Projection - There are two diagonal projections For projection, vertical projection, diagonal projection. These are as follows -

$$D_{P_L}(l) = \#\{(r_e, c_e) \in R_E \mid r_e + c_e = l\}$$

is defined by The second diagonal projection D_{P_U} goes from upper right to $\mathsf{low}_{\mathsf{er}_{[t]}}$

(iv) Area of Region - The area A can be obtained from any projection $D_{P_U}(u) = \#\{(r_e, c_e) \in R_E | r_e - c_e = u\}$

row, bottom row, leftmost and rightmost. (v) Bounding Rectangle - They are divided in four sections, to $\sum_{(f_e, e_e) \in R_E} 1 = \sum_{f_e} \sum_{\{e_e \mid (f_e, e_e) \in R_E\}} 1 = \sum_{f_e} H_P(f_e)$

(a) Top Row - It is denoted by rmin. The top row of bounding

$$r_{\min} = \min\{r_e \mid (r_e, c_e) \in R_E\}$$

 $= \min\{\mathbf{r}_{\mathbf{e}} \mid \mathbf{H}_{\mathbf{P}}(\mathbf{r}_{\mathbf{e}}) \neq 0\}$

row of the bounding rectangle rectangle is given by (b) Bottom Row - This can be denoted by r_{max}. The bottom $I_{\text{max}} = \max\{r_e \mid (r_e, c_e) \in R_E\}$

=
$$\max\{r_e(H_P(r_e) \neq 0\}$$

nost - This can be denoted rectangle is given by

column of the bounding rectangle is given by (c) Leftmost - This can be denoted by cmin. The leftmost

$$c_{\min} = \min\{c_e | (r_e, c_e) \in R_E\}$$
$$= \min\{c_e | V_P(c_e) \neq 0\}$$

column of the bounding rectangle is given by (d) Rightmost - This can be denoted by cmax. The rightmost

$$c_{\max} = \max\{c_e \mid (r_e, c_e) \in R_E\}$$

 $\max_{c_e \mid V_P(c_e) \neq 0}$

the horizontal projection Hp, as defined below -

(vi) Centroid of Region - The centroid of region include horizontal

(a) Row Centroid - The row centroid Ie can be obtained from

$$\begin{aligned} & = \frac{1}{A} \sum_{(\mathbf{f_c}, \mathbf{c_c}) \in R_E} \mathbf{r_c} \\ & = \frac{1}{A} \sum_{\mathbf{f_c}} \sum_{\{c_e | (\mathbf{f_c}, c_e) \in R_E\}} \mathbf{r_c} \\ & = \frac{1}{A} \sum_{\mathbf{f_c}} \mathbf{r_c} \sum_{\{c_e | (\mathbf{f_c}, c_e) \in R_E\}} \mathbf{r_c} \\ & = \frac{1}{A} \sum_{\mathbf{f_c}} \mathbf{r_c} \mathbf{H_P}(\mathbf{f_c}) \end{aligned}$$

obtained from the vertical projection V_P as follows – (b) Column Centroid - The column centroid $\overline{c_e}$ can be

$$c_{e} = \frac{1}{A} \sum_{(f_{e}, c_{e}) \in R_{E}} c_{e}$$

$$= \frac{1}{A} \sum_{c_{e}} \sum_{\{f_{e} | (f_{e}, c_{e}) \in R_{E}\}} c_{e}$$

$$= \frac{1}{A} \sum_{c_{e}} c_{e} \sum_{\{c_{e} | (f_{e}, c_{e}) \in R_{E}\}} 1$$

$$= \frac{1}{A} \sum_{c_{e}} c_{e} V_{p}(c_{e})$$

(c) Diagonal Centroid (Lower Left to Upper Right) - The

diagonal centroid $ar{l}$ can be obtained from the diagonal projection $D_{
m P_L}$. $\bar{l} = \frac{1}{A} \sum_{l} l D_{P_L}(l)$

The diagonal centroid \bar{l} is related to the row and column centroid in

following manner -

$$\begin{split} \overline{l} &= \frac{1}{A} \sum_{I} I \\ &= \frac{1}{A} \sum_{I} \{ (r_{e}, c_{e}) \in R_{E} | l_{e} + c_{e} = I \} \\ &= \frac{1}{A} \sum_{I} \{ (r_{e}, c_{e}) \in R_{E} | l_{e} + c_{e} = I \} \end{split}$$

$$= \frac{1}{A} \sum_{l' \{(t_e, c_e) \in R_E | t_e + c_e = l\}} \sum_{f_e} t_e$$

$$+ \frac{1}{A} \sum_{l' \{(t_e, c_e) \in R_E | t_e + c_e = l\}} \sum_{f_e + f_e + c_e = l\}} t_e$$

$$= \frac{1}{A} \sum_{(t_e, c_e) \in R_E} t_e + \frac{1}{A} \sum_{(t_e, c_e) \in R_E} t_e$$

$$= \frac{1}{t_e + c_e}$$

diagonal centroid $\overline{\,U\,}$ can be obtained from the diagonal projection $\,D_{ extst{P}_{\overline{\!U\,}}}$. (d) Diagonal Centroid (Upper Left to Lower Right) - The

$$\overline{U} = \frac{1}{A} \sum_{\mathbf{u}} \mathbf{u} D_{\mathbf{P}_{\mathbf{U}}}(\mathbf{u}) \qquad \text{and a } \mathbf{0}$$

Similarly, the diagonal centroid u is related to the row and column centroid

$$\overline{u} = \overline{t_e} - \overline{c_e}$$

projection, vertical projection, diagonal projection. (vii) Second Moments - Second moments also include horizontal (a) Row Moment – The second row moment $\mu_{(f_e, r_e)}$ can be

obtained from the horizontal projection Hp, defined as _____

$$\begin{split} \mu_{(\mathbf{r}_{e},\mathbf{r}_{e})} &= \frac{1}{A} \sum_{(\mathbf{r}_{e},\mathbf{c}_{e}) \in R_{E}} (\mathbf{r}_{e} - \mathbf{r}_{e})^{2} \\ &= \frac{1}{A} \sum_{\mathbf{r}_{e}} \sum_{\{c_{e} \mid (\mathbf{r}_{e},\mathbf{c}_{e}) \in R_{E}\}} (\mathbf{r}_{e} - \mathbf{r}_{e})^{2} \\ &= \frac{1}{A} \sum_{\mathbf{r}_{e}} (\mathbf{r}_{e} - \mathbf{r}_{e})^{2} \sum_{\{c_{e} \mid (\mathbf{r}_{e},\mathbf{c}_{e}) \in R_{E}\}} 1 \\ &= \frac{1}{A} \sum_{\mathbf{r}_{e}} (\mathbf{r}_{e} - \mathbf{r}_{e})^{2} H_{P}(\mathbf{r}_{e}) \end{split}$$

can be obtained from the vertical projection VP, defined as -(b) Column Moment – The second column moment $\mu_{(c_e,c_e)}$

$$\begin{split} \mu(c_e,c_e) &= \frac{1}{A} \sum_{(\tau_e,\,c_e) \in R_E} (c_e - \overline{c_e})^2 \\ &= \frac{1}{A} \sum_{c_e} \sum_{\{t_e \mid (\tau_e,c_e) \in R_E\}} (c_e - \overline{c_e})^2 \\ &= \frac{1}{A} \sum_{c_e} (c_e - \overline{c_e})^2 \sum_{\{t_e \mid (\tau_e,c_e) \in R_E\}} 1 \\ &= \frac{1}{A} \sum_{c_e} (c_e - \overline{c_e})^2 V_P(c_e) \end{split}$$
 Diagonal Moment (Lower Left to Upper Right)

DPL, defined as second diagonal moment $\mu_{(l,l)}$ can be obtained from the diagonal projection (c) Diagonal Moment (Lower Left to Upper Right) - The

$$\mu_{(l,l)} = \frac{1}{A} \sum_{l} (l - \bar{l})^2 D_{P_L}(l)$$

The second diagonal moment $\mu_{(l,l)}$ is related to $\mu_{(t_e,c_e)},\mu_{(t_e,t_e)}$ and

$$\begin{split} \mu_{(c_e,c_e)} \text{ in following way} \\ \mu_{(I,I)} &= \frac{1}{A} \sum_{l} \sum_{\{(t_e,c_e) \in \mathbb{R}_E | t_e + c_e = d\}} (r_e + c_e - \overline{r_e} - \overline{c_e})^2 \end{split}$$

$$= \frac{1}{A} \sum_{(r_e, c_e) \in R_E} [(r_e - \overline{r_e}) - (c_e - \overline{c_e})]^2$$

$$= \frac{1}{A} \sum_{(r_e, c_e) \in R_E} (r_e - \overline{r_e})^2 + 2(r_e - \overline{r_e})(c_e - \overline{c_e}) + (c_e - \overline{c_e})^2$$

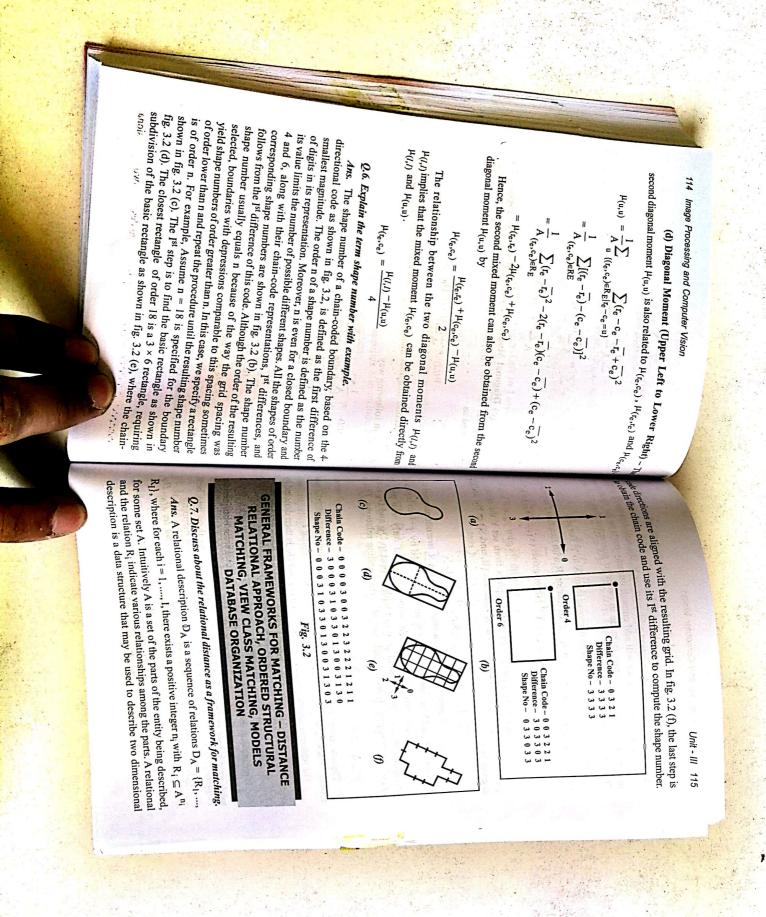
$$= \mu_{(r_e, r_e)} + 2\mu_{(r_e, c_e)} + \mu_{(c_e, c_e)}$$

Hence, the second mixed moment can be obtained from the second

diagonal moment $\mu(l,l)$ by

$$\mu_{(t_{c},c_{c})} = \frac{\mu_{(l,l)} - \mu_{(t_{c},t_{c})} - \mu_{(c_{c},c_{c})}}{2}$$

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(Y); if this is not use the assumption is made in order to guarantee that relating shape models, where $X = \{R_1, ..., R_I\}$ be a relational description with part set X. We will assume X and X and X are alternative X and X are alternative X. on. Let $D_X = \{K_1, ..., x_1\}$ a relational description with part set Y. We will assume that $\{S_1, ..., S_l\}$ a relational description with part set Y. We will assume that $\{S_l, ..., S_l\}$ on the case, we will add enough dummy parts to the $\{S_l, ..., S_l\}$ of the $\{$ shape models, three dimensional object models, regions on an image, and relational description with part set V.

Ans. (i) $R_D(D_X, D_Y) = 0$

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a positive integer, the composition $R \circ f$ of relation R with function f is g iven by Assume, f be any one-one, onto mapping from X to Y. For any $\mathbb{R} \subseteq X^N$.

 $R \circ f = \{(y_1, \dots, y_N) \in Y^N \mid \text{there exists } (x_1, \dots, x_N) \in \mathbb{R} \}$

error of f for the i^{th} pair of corresponding relations $(R_i \text{ and } S_i)$ in D_X and D_Y The function f maps parts from set X to parts from set Y the structual with $f(x_n) = y_n, n = 1,...,N$

$$E_s^{I}(f) = |R_i \circ f - S_i| + |S_i \circ f^{-1} - R_i|$$

sum of the structural errors for each pair of corresponding relations. That is corresponding relations. The total error of f with respect to D_X and D_Y is the Ri. The structural error is expressed with respect to only one pair of to tuples in S_i and how many tuples in S_i are not mapped by f^{-1} to tuples The structural error indicates how many tuples in R_i are not mapped by

$$E(f) = \sum_{i=1}^{r} E_s^i(f)$$

relational descriptions D_X and D_Y with respect to the mapping f. The total error gives a quantitative idea of the difference between the two

The relational distance $R_D(D_X, D_Y)$ between D_X and D_Y is then denoted by $R_D(D_X,D_Y) = \min_{f \in \mathcal{F}} E(f)$

mapping, one can be arbitrarily selected as the designated best mapping. mapping one can be st mapping from Dx to Dy. If there is more than one best any one-one, onto mapping f from X to Y. We call a mapping f that minimize total error a hart It means that, the relational distance is the minimal total error obtained for

180 and D_Z be arbitrary relational descriptions, then prove that Q.8. Suppose R_D be the relational-distance measure, and let D_X D_1 $(iii) \mathcal{R}_D (D_{X'} D_{D'}) = \mathcal{R}_D (D_{X'} D_{D'}) + \mathcal{R}_D (D_{D'} D_{D'}).$ (ii) $R_D(D_X, D_Y) = R_D(D_Y, D_X)$ $R_D(D_X, D_Y) = 0$, if and only if D_X and D_Y are isomorphic

 $y=x\circ f_2^{-1}\in R_i\circ f_1-T_i$, we have

 $|R_i \circ f_1 \circ f_2 - S_i| \le |R_i \circ f_1 - T_i| + |T_i \circ f_2 - S_i|$

between Dx and Dy. If f is an isomorphism between D_X and D_Y , then E(f) = 0. If $R_D(D_X, D_Y)$ then there exists one-one, onto f with E(f) = 0. Thus f is an isomorphism (ii) $R_D (D_X, D_Y) = R_D (D_Y, D_X)$ $LH.S. = R_D (D_X, D_Y)$

 $= \min_{\mathbf{f}^{-1}} \sum_{i=1}^{l} |R_i \circ \mathbf{f}^{-1} - S_i| + |S_i \circ (\mathbf{f}^{-1}) - R_i|$ $= \min_{f} \sum_{i=1} |R_i \circ f - S_i| + |S_i \circ f^{-1} - R_i|$

 $= \min_{\mathbf{f}^{-1}} \sum_{i=1}^{l} |S_i \circ \mathbf{f} - R_i| + |R_i \circ \mathbf{f}^{-1} - S_i|$

 $= \min_{f} \sum_{i=1}^{l} |S_i \circ f - R_i| + |R_i \circ f^{-l} - S_i|$

 $R_D(D_Y, D_X) = R.H.S.$

where for each i=1,...,I, $R_i\subseteq X^{n_i}$, $S_i\subseteq Y^{n_i}$ and $T_i\subseteq Z^{n_i}$. Let $f_1\subseteq X\times Z$ Assume $D_X = \{R_1, ..., R_I\}, D_Y = \{S_1, ..., S_I\}$ and $D_Z = \{T_1, ..., T_I\},$ (iii) $R_D(D_{X'}, D_{Y'}) \leq R_D(D_{X'}, D_{Z'}) + R_D(D_{Z'}, D_{Y'})$

be one-one, onto and the f_1 that minimizes R_D (D_X, D_Z) . Let $f_2 \subseteq Z \times Y$, be

If $y \in T_i$, then $y \in R_i \circ f_i - T_i$. If $y \in T_i$, then $\{x\} = \{y\} \circ f_2$ is an element of $T_i \circ f_2$. Hence $x \in T_i \circ f_2 - S_i$ There exists a unique $y \in R_i \circ f_1$ such that $\{y\} = \{x\} \circ f_2^{-1}$ and $\{x\} = \{y\} \circ f_2$. error E(f) with respect to D_X and D_Y . Assume $x \in R_i \circ f_1 \circ f_2 - S_i$. Then one-one, single valued and the f_2 that minimizes $R_D(D_Z, D_Y)$. $\in R_1 \circ f_1 \circ f_2$ and $x \notin S_i$. Since $x \in R_i \circ f_1 \circ f_2$ and f_2 is one-one and onto, Since for each $x \in R_i \circ f_1 \circ f_2 - S_i$ either $x \in T_i \circ f_1 \circ f_2 - S_i$ or Let $f: X \to Y = f_1 \circ f_2$. Then f is one-one and onto and produces some

of yj+1. yj+2,..... yj+k-1.

(iii) x_{i+1} maps to no primitive of Oy.

$$\begin{split} \sum_{i=1}^{L} |R_i \circ f_1 \circ f_2 - S_i| &\leq \sum_{i=1}^{L} |R_i \circ f_1 - T_i| + \sum_{i=1}^{L} |T_i \circ f_2 - S_i| \\ \text{Similarly, we can show that} \\ \sum_{i=1}^{L} |S_i \circ f_2^{-1} \circ f_1^{-1} - S_i| &\leq \sum_{i=1}^{L} |T_i \circ f_1^{-1} - R_i| + \sum_{i=1}^{L} |S_i \circ f_2^{-1} - T_i| \\ \text{Adding, we get} \\ 1 \end{split}$$

 $\sum_{i=1}^{n} |R_i \circ f_1 \circ f_2 - S_i| + |S_i \circ f_2^{-1} \circ f_1^{-1} - S_i|$

 $\leq \sum_{i=1}^{l} |R_{i} \circ f_{i} - T_{i}| + |T_{i} \circ f_{i}^{-1} - R_{i}| + \sum_{i=1}^{l} |T_{i} \circ f_{2} - S_{i}| + |S_{i} \circ f_{2}^{-1} - T_{i}|^{l}$

E(f) wrt D_X and $D_Y \le R_D(D_X, D_Z) + R_D(D_Z, D_Y)$ $R_D(D_X, D_Y) \le E(f)$

Thus the relational distance of two relation description is a metric up \mathfrak{g} $R_D(D_X,D_Y) \le R_D(D_X,D_Z) + R_D(D_Z,D_Y)$

Q.9. Write short note on ordered structural matching.

symbols and that parse the string according to the grammar. represent object models by grammars, that convert an object to a string of ordered structural matching are syntactic pattern recognition algorithms that extracted by operations of mathematical morphology. Another example of MacDonald and Sternberg, for 2-D shape matching using shape primitives In many two-dimensional computer vision problems, the spatial Ans. In 1987, ordered structural matching was used by Shapiro,

primitives that greatly reduces the complexity of the search. arrangement of the primitives allows the definition of an ordering on the

one of the following conditions holds hypothesized that primitive x_i maps to primitive y_i. The ordering tells us that ordering < y₁, y₂,, y₁ >. Suppose that during the matching process it is set X has the ordering $\langle x_1, x_2, ..., x_s \rangle$ and that the primitive set Y has the OX to another object represented by description Oy. Suppose that the primitive Assume that we wish to compare an object represented by description

> here, x_{i+1} is the next primitive after x_i in the ordering. Thus, once x_i is mapped to y_i , the ordering can be used to find the correspondences between all the other primitives in polynomial time. 0.10. Explain various stages of view class matching Ans. A view class matching can be divided into two stages, when a 3-D

represents relationships among entities from lower levels. The full relational If the relational pyramid has a relation R with c tuples given by pose of the object after the view class is identified. For rapid view class in which primitives appear on the lowest level and each of the other levels pyramid structure is for use in detailed matching for determining the exact dentification, relational summaries were derived from the relational pyramids. represented by a hierarchical relational structure called the relational pyramid, object is represented by a view-class model. These stages are as follows -(i) Determining View Class of the Object - A view class is

 $\{[(N_1,t_{1,j}),....,(N_n,t_{n,j})] | j=1,...,c\}$

the relation that tuple tij comes from. Here, ti, is a tuple from a lower level of the pyramid and Ni is the name of

line drawing of this view class relation has four types of the form [ROCK, r), (BRAVO, b)], then the collinear summary relation has one tuple [(ROCK, BRAVO), 4], indicating that there are four collinearity relationships between a rock junction and bravo junction in [(N₁,....,N_n),c] representing those c tuples. For example, if the collinear The summary has a corresponding relation PL with a single tuple

for k = 0,, K, where K is the maximum amount of deviation allowed. view classes on list attached to $[(N_1,...,N_n),c+k]$ and $[(N_1,...,N_n),c-k]$ $[(N_1,, N_n), c]$, the system adds $e^{-k^2/2}$ to the accumulators of those evidence are selected. For inexact matching, when considering summary tuple attached to that tuple in the index. The view class or classes with maximal structure, it adds one to the accumulators of all the view classes on the list initialized to zero. For exact matching, the system traverses the summary The online system keeps an evidence accumulator for each view class,

matching procedure for each view class, with the particular relationships and pose. There are two possible approaches. First is to use a general purpose been determined, feature correspondences must be found the determine the (il) Pose Determination with View Class - Once the view class has

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procedure for each view class. A preprocessing program analyzes each view use higher level features first and propagate the results to lower levels of pyran relational pyramic A strategy that the feature matching at each possible level of the pyramid. A strategy that this the feature matching at each possible level of the pyramid. A strategy that this the feature matching at each possible level of the pyramid. A strategy that the feature matching at each possible level of the pyramid. A strategy that the feature matching at each possible level of the pyramid. A strategy that the feature matching at each possible level of the pyramid. A strategy that the feature matching at each possible level of the pyramid. A strategy that the feature matching at each possible level of the pyramid. A strategy that the feature matching at each possible level of the pyramid. features, and then selects a sequence of features to look for in the matching class, possibly using training data or theoretical analysis to determine reliable to the for in the reliable to the form of features to look for in the reliable to the features to look for in the reliable to the features to look for in the reliable to the features to look for in the reliable to the features to look for in the reliable to the features to look for in the reliable to the features to look for in the reliable to th can result in a fast match. The second possibility is to develop a customia relational pyramid structure is a hierarchical, relational structure that can only constraints of that view class used to prune the search for a solution.

Q.11. Write brief note on model database organization.

an average of y interest points, then total number of such pairs stored in the all possible models in its hash table structure. If there are x models, each with the original affine-invariant matching technique stores (model, basis) pairs in candidate models, several approaches to this problem are available. For example database of models in a way that system allows rapid access to the most like Ans. An important problem for robot vision system is to organize the

$$(y)$$
 $\frac{1}{|x-4|}$

syntactic classifier. Such classification may be very simple, but very useful classes can be chosen by some type of decision tree or other statistical $_{
m 0T}$ global attributes, then, like the view-class determination approach, the object which can grow quite large. If the object models can be characterized by their

relational description within the cluster that somehow best represents that cluster i.e., as opposed to points in n-dimensional space. The representative should be be done by any clustering algorithm that can work with distance between object and then with the models in those clusters deemed similar enough. Clustering can each cluster. An unknown object would be compared with the cluster representatives is to group similar relational models into clusters and to select a representative for metric was developed in 1982 by Sharpiro and Haravick. The idea of this approach A scheme for organizing relational models based on the relational-distance

 D_x in A, define the total distance of D_x with respect to A is given by, Assume that a cluster A has been constructed. For any relational description

$$T(D_x, A) = \sum_{D \in A} R_D(D_x, D).$$

The relational description D_y that satisfies $T(D_y, A) = \min_{D \in A} T(D, A)$ is used

can be repeated to create a hierarchical structure of clusters and representatives. as the representative of the clusters. If the clusters are large, this entire process

0

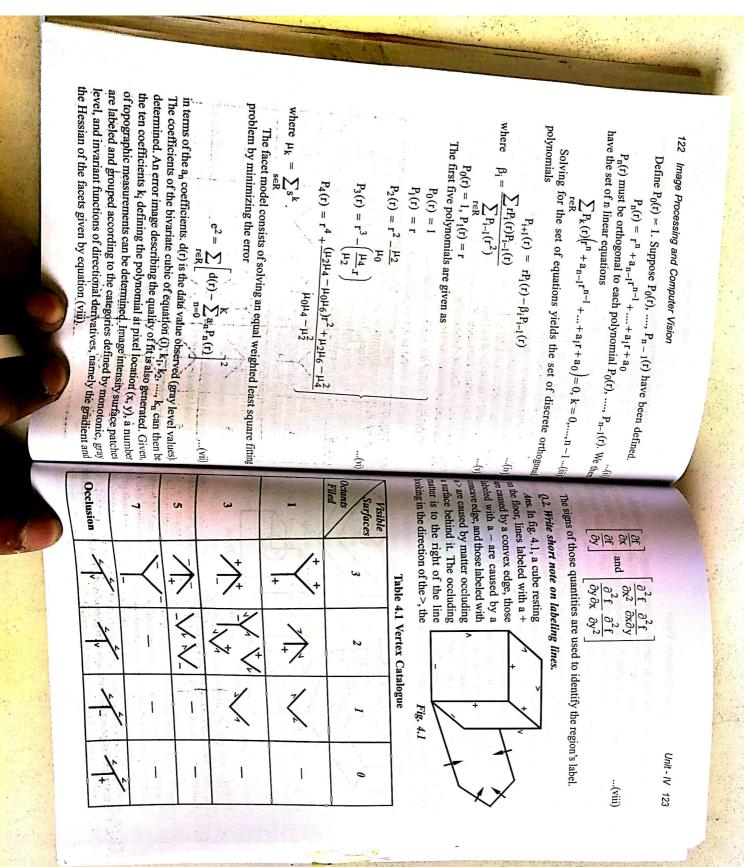
are iteratively constructed as follows -

OF SHAPES BY LABELING OF EDGES, RECOGNITION NDERSTANDING LINE DRAWINGS, CLASSIFICATION OF SHAPES, CONSISTING LABELING PROBLEM, ACET MODEL RECOGNITION - LABELING LINES, BACK-TRACKING ALGORITHM

range from edge detection, background normalization, shape and surface curves, valleys, and ridges. The facet model principle is based on the were. The image is considered as a noisy discretized sampling of the surface. wography, to image segmentation procedures involving detection of comers, region in the image has a constant gray level. In the sloped model, each region linear, piecewise quadratic, and piecewise cubic. In the constant model, each The general forms of the facet model include piecewise constant, piecewise as a gray level surface that is a sloped plane. The model used in this work is Q.1. Discuss about the facet model in details. timous gray level intensity surface and the observed data from the physical mization of the error between the image thought of as a piecewise Ans. The facet model is a powerful tool in image processing. Its uses

sto be fitted. A local vector of the ten coefficients, computed as weighted sums where f(x, y) is the gray level value at pixel location (x, y) whose neighbourhood the cubic polynominal defined by equation (i), orthogonal polynomial basis permits independent estimation of each coefficient of the values in the local neighbourhood, is found for each pixel (x, y). A discrete olynomials are given by equation (ii) for the 1-D case. The 2-D polynomials are a linear combination of the data values in the neighbourhood of (x, y). Those $f(x, y) = k_1 + k_2x + k_3y + k_4x^2 + k_5xy + k_6y^2 + k_7x^3$ $+ k_8 x^2 y + k_9 x y^2 + k_{10} y^3$

implies \vdash $r \in R$. Let $P_n(r)$ be the n^{th} order polynomial. The discrete polynomials brained by taking the tensor product of the 2 sets of 1-D polynomials. Let the discrete integer index set R be symmetric in the sense that $r \in R$



in this restricted world of trihedral polyhedra. It is easy to imagine extending the state of th which is a catalogue of all possible vertices, including those arising from occlusion for these comer types. The vertices appear in the first two rows of table 4. views of one- and three-octant corners which give rise to all possible vertions. the possible labelings of lines meeting at a vertex can occur. Fig. 4.2 towo all possible universe. Clowes found that without occlusion, just four vertex types and Only a long at a vertex can occur rich a long a long a long at the long at all possible trihedral corners as seen from all possible viewpoints, Huffman inst four vertex types and a liftman and the second for the comer of a cube, seven for the inside comer of a room etc.). By consider the inside comer of a room etc.). By consider to consider the consideration of the comercial transfer to the consideration of the constant classified by how many octants of space are filled by matter around them (a) types of lines possibly seen around a trihedral corner, such corners and find the corners of space are filled by matter around a trihedral corners. occluded suriace to the control of with - . A systematic investigation can have lowest lines with / instead of with - . A systematic investigation can have lowest lines with corner, such corner, such corner, such corner, such corner. occluded surface is to the left. If the cube were floating, one would label Aline Projection specifications, a wire-frame object may be constructed with selections given the N projections. However, for a given 1 way server to given the N projections. However, for a given object, there is 4.3 whice wing nevertheless does convey three-dimensional information.

4.4 Integration specifications, a wire-frame object manufacture.

the possible labels actually occur. Thus only a small fraction of possible labels cell. In the catalog, however, only 3/64, 3/64, 4/64, and 6/16, respectively, = 64 possible labels for the fork, arrow, and T and 16 possible labels for the Note that there are four possible labels for each line (+-><), and thus

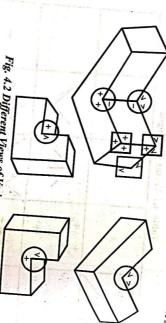


Fig. 4.2 Different Views of Various Corner Types

Q.3. What do you understand by line drawings?

supplied" by our model-driven perception. polyhedra are often so easy to supply as to pass unnoticed, or be "automatically understood and interpreted as they were meant. Missing lines in drawings of interpretation means that even drawings that are strictly nonsense can be knowledge of everyday physics, and can require training. Such informed human being about quantitative aspects of three dimensional object, Line drawings are often ambiguous; interpreting them sometimes takes Ans. Line drawings have been the main medium of communication between

not enough to make an unambiguous representation, as shown by Generalizing the line drawing to three dimensions as a list of lines or points

by is another of projections that can determine the object unambiguously.

Fig. 4.3 An Ambiguous Representation

Line drawings were a natural early target for computer vision for the

- goessing that may have affected the "line drawing extraction" can be modelled (i) They are related closely to surface features of polyhedral scenes.
 (ii) They may be represented exactly; the noise and incomplete visual
- sems approachable. at will or completely eliminated. (iii) They present an interpretation problem that is significant but

Q.4. Explain the shape recognition by moments.

ligital (j, k)th moment of S is given by represent a 2-D shape. For each pair of nonnegative integers (j, k), the Ans. Suppose f be a binary image function and suppose $S = \{(x, y) \mid f(x, y)\}$

$$M_{jk}(S) = \sum_{(x,y) \in S} x^{j}, y^{k}$$

exognition, we would like to have quantities that are moment invariants under noments that are invariant under certain shape transformation. For 2-D shape M₀₀(S) is then just #S. Moment invariants are function of the digital

uslation, rotation, scaling and some kind of skewing. The COG (center of gravity) $(\overline{x}, \overline{y})$ of S can be expressed in terms of

some moments are defined as -Using the COG, we can define the central (j, k)th moment of S by $\mu_{jk} = \sum_i (x - \overline{x})^j (y - \overline{y})^k$ $\bar{x} = \frac{M_{10}(S)}{M_{00}(S)}$ and $\bar{y} = \frac{M_{01}(S)}{M_{00}(S)}$

The central moments are translation invariant, since if $S^* = \{(x^*, y^*) \mid x^* = x + p, y^* = y + q, (x, y) \in S\}$

Then
$$\overline{x}(S^*) = \frac{\sum_{(x^*,y^*) \in S^*} x^*}{M_{00}(S)} = \frac{(x,y) \in S}{M_{00}(S)} = \frac{(x,y) \in S}{M_{00}(S)} = \overline{x}(S) + p$$

Similarly, $\overline{y}(S^*) = \overline{y}(S) + q$

$$\mu_{jk}(S^*) = \sum_{(x^*,y^*) \in S^*} [x^* - \overline{x}(S^*)]^j [y^* - \overline{y}(S^*)]^k$$
$$= \sum_{x^*} \{x + p - [\overline{x}(S) + p]^j (y^*) - \overline{y}(S^*)\}^{k}$$

and

 $= \sum (x - \overline{x})^{j} (y - \overline{y})^{k} = \mu_{jk}(S)$ $\sum_{(x,y) \in S} \{x + p - [\overline{x}(S) + p]^{j} (y + q - [\overline{y}(S) + q])^{k}$

The standard deviation (SD) can be expressed in terms of moments.

$$\sigma_{x} = \left[\frac{\mu_{20}}{M_{00}}\right]^{1/2}, \quad \sigma_{y} = \left[\frac{\mu_{02}}{M_{00}}\right]^{1/2}$$
the coordinates by the coordin

normalized coordinates Alt normalized the coordinates by their respective SD to obtain the

Thus the mean values of x' and y' are both 0, and variance are both $x' = \frac{(x-\overline{x})}{\pi}, \ y' = \frac{(y-\overline{y})}{\pi}$

Normalizing by area, the normalized moments defined by $m_{jk} = \sum (x')^{j} (y')^{k}$

and "squeezing" transformation), since if transformations of the form $x^* = px + q$, $y^* = ry + t$ (referred to as "stretching" These moments are invariant under translation, scale and in general, affind

then we have $S^* = \{(x^*, y^*) \mid x^* = px + q, y^* = ry + t, (x, y) \in S\},\$

 $\sum p^{j}[x-\overline{x}(S)]^{j} r^{k}[y-\overline{y}(S)]^{k}$

when \hat{U} of the units is consistent if whenever u_1,u_2 and u_N are in \hat{U} and the Number $(u_1, u_2, ..., u_N)$ is in T, then $[(u_1, f(u_1)), (u_2, f(u_2)), ..., (u_N, f(u_N))]$ is are the N-tuples of T, the unit constraint relation. A labeling of subset $[:[u_1,u_2,....,u_N]]$ of U is a mapping $f:\hat{U}\to L$ from \hat{U} to L. A labeling f of a vay relation over the set $U \times L$ of unit-label pairs. If an N-tuple $[(u_1, l_1), (u_2, l_2), (u_3, l_3)]$ Nuple (u) u2,, uN) belongs to T, then we say that units u1, u2 ordered size N subsets of unit set U. The only groups of units that are constrained and countries on the set U of units. (IN, N)] belongs to R, then the units u₁, u₂,, u_N may be assigned the O.s. Discuss about the consisting labeling problem. ruple component, namely, U, L, T and R. The first component U of the 4-And in science and engineering in general. An N-ary CLP (caline ligence), and in science and engineering in general. An N-ary CLP and component L is the set of possible labels. The third component T is saset of M units U = {1, ..., M} which are the objects to be labeled. The 0.5 A consisting-labeling problem (CLP) arise in computer vision, in Al ups of parallel line segment can potentially mutually constrain one another. mally constrain one another. Groups of regions in an image that are adjacent conding labels $l_1, l_2, ..., l_N$. Thus the elements of R are allowable labeling the fourth component R is called the unit-label constraint relation. R is an

Q.6. Explain the following -

belings of the unit set U.

(i) The N-Queens problem (ii) The Latin-square puzzle.

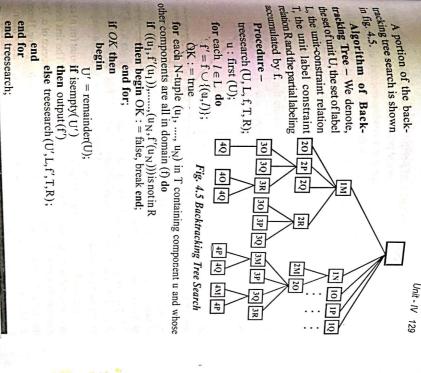
R. The goal of the consistent labeling problem is to find one or all consistent-

consistent labeling problems. The Latin-square puzzle is an $N \times N$ matrix with the chessboard on which two queen's can stand without capturing each other. and N queens. The queens must be placed on the chessboard in such a way set L = {1, 2, 3,, N} is the set of columns. Since there will be exactly one the same row, same column, or same diagonal of the chessboard. The Nthat no queen can capture any other queen. This means that no two may be in onstraint relation R = { [u_i, l_i), (u_i, l_j)] | (u_i, u_j) ∈ T, $l_i \neq l_j$, l_i , $l_j \in L_i | u_i - u_j | \neq l_j$ wit set U = {1, 2, 3, ..., N} is the set of rows on the chessboard and the label |- /|) includes these pairs of unit-label pairs that represent two squares on usen per row, a labeling will specify the column on which a queen is placed weens problem can be modeled as a consistent-labeling problem in which the each row. Every pair of rows will constrain one another, so the unit constraint onsistent-labeling problem. In this problem, we are given $N \times N$ chessboard ation T will be the set $T = \{(u_i, \mu_j) \mid u_j, u_j \in U \text{ and } u_i \neq u_j\}$. The unit-label ans. (i) The N-Queens Problem - This problem can be formulated as (ii) The Latin-square Puzzle - This problem is also an example of

 u_3, u_4) is in T. $(a_i b_i) \in L$ for i = 1,, 4 and when $i \neq j$, $a_i \neq a_j$ and $b_i \neq b_j$. form {[u₁, (a₁, b₁)][u₂, (a₂, b₂) [u₃, (a₃, b₃)], [u₄, (a₄, b₄)]} where (u₁, u₅) constraint relation R would then consist of quadruples of unit label pairs of the | u₁, u₂, u₃ and u₄ all lie in the same row, column or diagonal}. The unit-label product set $L = A \times B$. The constraints are along the rows, columns, and main $T = f_{fin}$. red rectangle, orange rectangle, and so on. We can represent Las the Carlesian squares of the flaced on the squares such as pink square, orange triangle, and so on. We can represent L as the contribute of the squares of matrix community with the matrix community of modeling the Latin-square puzzle is to let the left the left the left than the rest of unit $U = \{1, 2, ..., 16\}$. Then the rest of the left the left than the rest of the left than th matrix contains exactly one object of each color and exactly one object of each color and exactly one object of each color and exactly one object of the Latin-square puzzle is to law of the latin-square puzzle is to latin-squa such that each row, each column, and each of the two main diagonals objects that each row, each column, and each color and exactly one object of each color and exactly one objects. of four colours A = {pink, orange, blue, red} and has one of four shapes by shapes by shapes by the problem is to arrange the base of N^2 objects that must be consider a 4×4 puzzle for ease of illustration. In this case each object will $A \times A = A$ with orange, blue, red and has one of four share A = A and A = A and A = A or or or one of four share A = A one of four share A one of N² objects that must be arranged on the matrix, one per square. We will be a square of illustration. In this case each object will be a square. of four colours A — \(\text{\text{\$\sigma}}\) frectangle, triangle, square, circle}. The problem is to arrange the object of the two main diagonal.

Ans. A backtracking tree search starts with the first unit of U. This unit Q.7. Explain the backtracking tree search. Also write its algorithm.

outdegree $[f(u)] \ge outdegree(u)$ for all units u. a subgraph of graph G2, that is isomorphic to graph G1. The possible labels for each unit were chosen on the basis that indegree $[f(u)] \ge \text{indegree } (u)$ and consistent labelings. A simple digraph matching problem as shown in fig. 4.4, tree. The path from the root node to any successful nodes at level $|\mathbb{U}|$ are the because they violate the constraints. The process continues to level |U| of the to each possible label of L. At this level some of the nodes may be ruled out the children of the first node, which are nodes that map the second unit of U makes the assignment, selects the second unit of U, and begins to construct is a node at level one of the tree. The algorithm selects one of these nodes, can potentially match each label in set L. Each of these potential assignments



PERSPECTIVE PROJECTIVE GEOMETRY, INVERSE PERSPECTIVE PROJECTION, PHOTOGRAMMETRIC FROM 2D TO 3D

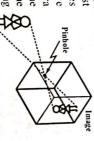
Unit

Possible Labels

called perspective projection. form the image of the object. Such a mapping from three dimensions onto two dimensions is intersection of the light rays with the image plane urough an infinitesimally small aperture. The projection. Rays of light enters the camera accurately the geometry of perspective maging device which, however captures Ans. A pinhole camera is the simplest Q.8. Write short note on perspective projection geometry. Fig. 4.6

M, O, P, Q M, O, P, Q, R M, O, P, Q, R M, N, O, P, Q

Fig. 4.4



constant. The position on the line is determined by where the line from $(m, n)_{ij}$ perspective projection has coordinates (md/ distance d directly in front of the lens. The distance d is known as the Camera point (m, n) onto the image line, which is a line parallel to the x-axis and at a According to the geometric ray optics model for the lens, the lens will focus a image behind the lens. The image line for this example is parallel to the x-axis projects forward to it. This eliminates the problems of left-right reversal in an that the image line is at a distance d in front of the camera lens and that the lens are the problems of left-right resources. shown in fig. 4.7. In order to keep the image in a positive orientation, we assume the first of the camera lens and those at the camera lens are the camera lens and the camera lens are the camera le Ans. The camera lens is at the origin and points directly down the yaxis, as Q.9. Explain the one-dimensional perspective projection.

computed by taking ratios of components of by an appropriate linear transformation, the I-D perspective coordinates could be numerator and denominator were computed are linear combinations of m and n. If the the numerator and the denominator of md/n line, the coordinate is md/n. Note that, both coordinate system. Relative to the onedimensional coordinate system of the image n, d) in the original two dimensional

XI Image x-axis

Fig. 4.7

the 1-D image line coordinates, for the point are then given by $x_1 = a/b = md/n$. second transformation takes the perspective transformation to the image line. Hence, transformation translates the point (m, n, 1) down the y-axis by a distance of d. The be represented as (m, n, 1) in the homogeneous coordinate system. The first linear This can be shown by using homogeneous coordinates. The point (m, n) can

$$\begin{bmatrix} \mathbf{a} \\ \mathbf{b} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1/d & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & -d \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{n} \\ \mathbf{n} \end{bmatrix}$$
Q.10. Discuss about the three dimension $\mathbf{J} = \mathbf{J} \begin{bmatrix} \mathbf{n} \\ \mathbf{n} \end{bmatrix}$

Q.10. Discuss about the three dimensional perspective projection.

space. Let (x_0, y_0, z_0) be the position of the lens, called the lens. Let (x, y, z) be the original coordinates of a point in three dimension using a homogeneous coordinate system that assumes an arbitrary position of take the perspective transformation. Perspective transformation is done by distance d to the desired location of the projection image plane, and finally we centered at the lens of the camera. Then we translate along the z-axis by a space, we first translate this point to a three dimension coordinate system To obtain the image frame coordinates for a given point in three dimension Ans. The optic axis of a camera lens lies along a line parallel to the z-axis the center of

> per projection plane. Then a = x*/t* and b = y*/t*, where (x, y, z) on the image projective xperspectivity, and let (a, b) be the coordinates of the perspective projection of

 $a = d \frac{x - x_0}{a}$ and $b = d \frac{y - y_0}{a}$

Q.11. Define the term inverse perspective projection.

of the camera lens has 3D coordinates (a, b, d). Since the camera lens is the rojection (a, b). We call the line L, multiples of (a, b, d). Furthermore, since the origin is the center of perspective coordinate system of the image projection plane that is at a distance d in front gin, a ray passing through the point (a, b, d) and the origin consists of all Ans. Consider, a point whose perspective projection is (a, b) in the

$$L = \left\{ \begin{bmatrix} x \\ y \\ y \\ z \end{bmatrix} \begin{bmatrix} x \\ a \\ b \\ d \end{bmatrix} \right\}$$

the inverse perspective projection of the point (a, b)

Q.12. Write short note on photogrammetric terminology.

Ans. Basic terminology used in photogrammetric is are as follows -

control points whose corresponding position on the image is known. respectivity and the direction of the optical axis. Specification of the exterior vorid reference frame. The parameters consist of the position of the center of pecified by all the parameters that determine the pose of the camera in the arameters and it is accomplished by obtaining the 3D coordinates of some tentation therefore requires three rotation angles and three translation Exterior Orientation - The exterior orientation of a camera is

specified by all the parameters that determine the geometry of a bundle of three dimension rays from the measured image coordinates. The parameters (ii) Interior Orientation - The integrior orientation of a camera is

Unit - IV 131

orientation of a camera is given by the interior and exterior orientations. of interior our managements include the camera constant, the principal physics of a camera. The parameters include the camera constant, the principal physics of a camera. The parameters include the camera constant, the principal physics of a camera. of interior orientation relate the geometry of ideal perspective projection to the marameters include the camera constant, the mineral constant of the mineral constant.

orientation of each camera is known. The process of determining relative orientation assumes that the interior three dimension space. The scale cannot be determined by relative orientation orientation, each pair of corresponding rays from the two cameras intersecting to the two cameras in the two cameras intersecting to the two cameras in the two c - three rotation angles and two translations. When two cameras are in relative relative to another constitutes a stereo model and is specified by five parameters are in the parameters. When two cameras are in the parameters are in the parameters are in the parameters are in the parameters. (iii) Relative Orientation - The relative orientation of one camera

by obtaining the three dimension coordinates of some central points whosetranslation parameters, and the three rotation parameters. It is accomplished position on the stereo image can be determined. requires the determination of seven parameters, such as the scale, the three orientation of a stereo model in a world reference frame. This orientation (iv) Absolute Orientation - The absolute orientation involves the

SIGNALS, MATCHING OF 2D IMAGE, HIERARCHICAL IMAGE MATCHING - INTENSITY MATCHING OF 1D IMAGE MATCHING

Q.13. Explain about the image matching.

errors in the matching results when dealing with poor textural images. photogrammetry systems require lots of human interactions to remove the matching is a difficult and challenging problem. Most of the traditional digital image texture conditions. However, on relatively poor textural image, image triangulation. Image matching is relatively easy when encountered with good corresponding pixels in a pair of image which allows 3D reconstruction by intelligent monitoring and motion analysis. Image matching is used for finding applications, such as camera calibration, three dimensional reconstruction, photogrammetry and computer vision. It is the foundation of computer vision Ans. Image matching is an essential and difficult task in digital

primitives. One is area-based matching and the other is feature-based matching. matching which can be generally divided into two classes based on the matching computer vision to improve the reliability, automation, and efficiency of image A lot of efforts have been devoted in the field of photogrammetry and

uses the grey value of the whole image to measure the similarity of two images directly on local image windows, and it can acquire dense correspondences. It (i) Area-based Matching - Area-based matching usually works

> measurazion of mutual information, correlating method, conditional entropy inint entropy method and so on Although area to conditional entropy long time of matching and sensitivity to rotating, scaling and distort. most widely used, there exists some shortcomings such as huge computation, nethod, joint entropy method and so on. Although area-based matching is the measurement is the biggest. There are many area-based matching methods such dreathy. And a certain method is employed to search the point where the similarity ment is the biggest. There are many area-based matching.

and the obtaining of feature points is a bit difficult. Besides, it is only suitable speed and high precise matching rate, but it also requires human intervention operator mainly through region segmentation. Generally speaking, feature one is point feature extraction operator such as Förstner operator, Harris By far, feature extraction algorithm can be divided into three main classes such as Canny operator, LoG operator), and the third is surface extraction operator and Susan operator, the second is linear feature extraction operator or simple images with significant geometric features. ased matching has the advantage of being simple to operate, rapid matching point feature, straight line, edge, shape, closed area, statistical moment, etc. (ii) Feature-based Matching - The common image feature includes

Ans. Intensity based matching techniques directly refer to the model equation Q.14. Discuss about the intensity based matching techniques in 1-D signal

procedure. The model then can be written as assumed to be perfectly known. This situation is relevant to an object location account, we restrict this discussion to the case in which one of the signals is this task is demanding when taking the statistical properties of the data into into the principles, we first develop methods for matching 1D signals. As even and aim at estimating and evaluating the parameters p_G and p_I. To give insight $g'(r',c') = T_I \{g''[T_G(r'',c'';p_G)];p_I\}$

 $g(x) = T_I\{f[T_G(y;p_g)];p_I\} + n(x)$..(II)

can be obtained analytically. This is just like the facet model. Because of the use a derived or estimated continuous f(y) from which the first derivatives gven by sampled data and a fitting or interpolation scheme that allows one to and the observational noise component n(x) is stated explicitly. Let f(y) is ighly nonlinear character of the estimation problem, we always, assume that Here, g', g", r' and r" have been replaced by g, f, x and y respectively,

nonlinear problem. We therefore always assume that second-order effects are problem by a linear substitute problem whose solution then gives rise to better prediction scheme. This initial approximation permits us to replace the nonlinear approximate values $p_I^{(0)}$ and $p_G^{(0)}$ are known from some prior information or

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sufficiently small specifically, (i) when interpolating for its derivate, (ii) when neglecting the random nature of f if it is derived from real data, or (iii) when

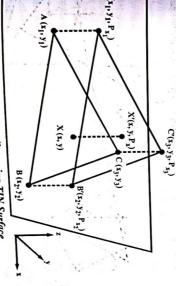
Q.15. Write short note on epipolar geometry.

which are the intersection of the baseline b intersects with the image planes μ' and μ'' , respectively Thus in general epipolar lines are not parallel. epipolar lines. All epipolar planes form a pencil of planes passing through the baseline b = (A'A''). The epipolar lines intersect in the epiploles F' and F'points P_1 not sitting in the same epipolar plane, we obtain different pairs of and μ'' result in the two epipolar lines e'(P) and e''(P) associated with P. For condition - the five points P,A',A",P' and P" lie in one plane, the so called epipolar plane \in (P) associated with P. The intersection lines of \in (P) with μ' geometric model of the perspective projection - specifically the collinearly P'(u', v') and P"(u", v") in the image planes μ' and μ". Because of the interior orientation. The object point P(x, y, z) then is mapped into (u",v") derived from the pixel coordinates (r',c') and (r',c') by using the are assumed to be the origin of the two image coordinate systems (u',v') and centers A' and A" form the baseline of length b, the principal points B and B image pair. The general setup of cameras is shown in fig. 4.8. The projection dimensional one by the so called epipolar geometry inherent in the oriented

Ans. Image matching can be tremendously simplified if the relative histogram. The matching is performed by measuring the similarity between the definerest point is characterized by a vector with 128 unsigned eight-bit numbers and interest point is characterized by a vector with 128 unsigned eight-bit numbers and incention, which defines the manual results are a local region, which defines the manual results are a local region. generated from a local region, which defines the multi-scale gradient orientation distributed matching points for the initial triangulation. In the SIFT descriptor, bortons, which is ideal for the purpose of generating a certain number of well

not fit for the final best model are considered as blunders and eliminated from process is repeated to find the best model. Those matched points which do nodel which has the largest number of correct corresponding points. This This model is evaluated by determining whether each pair of corresponding subset of the matched corresponding points. From the chosen matched points from the previous SIFT matching results. It starts by randomly selecting a we vectors associated with the two matching points. he initial matching point set. oints fit reasonably well to it. This is used as a criterion to determine the best fundamental matrix can be calculated based on which a model is then built. The RANSAC approach is used to detect and eliminate possible blunders

grid points is conducted at the top level again. can be constructed and an area-based image matching with feature points and After the seed points are extracted at the top level, an initial triangulation



2

on the lowest resolution. The matched points are then transferred to the next Subsequent level, points from upper level are matched again to achieve higher This process repeats until it reaches up to the original image level. At a level (of higher resolution) where additional feature points could be matched recision. A TIN (Triangulated Irregular Network) surface of parallaxes is In the process of hierarchical strategy, image matching is first conducted Fig. 4.9 Interpolation of x Parallax using TIN Surface

initial triangulation. The SIFT algorithm is proved to be able to produce robust

but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse corresponding points invariant to moderate scale changes or but relative sparse spars

Fig. 4.8

and RANSAC approach to obtain a few reliable correspondences, an Am. The hierarchical image matching method first uses a SIFT algorithm Q.16. Explain the hierarchical image matching

Onstruct

Scanned with CamScanner

TIN is used to estimate the correspondence of additional feature points. generated from these matched points using the Delaunay triangulation. This As shown in fig. 4.9, a point X(x,y) is inside of a Delaunay triangle formed

on the TIN surface formed by $A'(x_1, y_1, p_{x_1})$, $B'(x_2, y_2, p_{x_2})$, $C'(x_3, y_3, p_{x_3})$, by points $A(x_1,y_1)$, $B(x_2,y_2)$, $C(x_3,y_3)$, the x parallax is interpolated based

strategy, only using y parallax as z coordinates. Finally, the estimated parallel to z-axis. Parallax in y direction (p_x) can be calculated using the same corresponding point coordinate (x', y') is defined as which is the intersection between the 3-D plane A'B'C' and the line $\chi_{X'}$ The x parallax of point $X(p_x)$ is interpolated as the x coordinate of point χ_i

 $x' = x + p_x$

OBJECT MODELS AND MATCHING - 2D REPRESENTATION, GLOBAL VS LOCAL FEATURES

Q.17. Discuss about the two dimensional representation.

is boundary representation. In boundary representation, there are three main points, second, by its chain code and third, as a sequence of line segments. ways to represent the boundary of an object such as first, as a sequence of representation selected. The most common example of 2D object representation The method used for shape recognition often depends on the particular vision, including medical image analysis, aerial image analysis and manufacturing Ans. 2D shape analysis is useful in a number of applications of machine

some special property that makes them useful in a given matching algorithm. other two main boundary representation, or processed to produce a smaller list of interest points. Interest points are points on the boundary that have coordinates. The list can be maintained as a whole, converted into one of the performed on a digital image. The result of such an operation is a list of pixel boundary come from some kind of border-following or edge-tracking algorithm (i) A Sequence of Points Representation - The points of the

let M (A, C) be the maximum distance from A to all such arc length I and span the part of the curve containing A. Let d(A, C) be the perpendicular distance from a point A to a chord C whose span cons point A on the curve and a fixed arc length I, there is a set of chords that have of boundary points of the curve is the curve-partitioning algorithm. Given a One method of extracting these interest points from the original sequence , and

> this way it detects not only very sharp corners but also points of high curvature point of the curve if the value of M(A, C) is a local maximum and also exceeds this way that are part of a section of approximately constant curvature, slong the boundary that are part of a section of approximately constant curvature. a tree modified to select a point A that is the median point in a sequence of A_{-} for which $M(A_{-}, C)$, i = 1point of well-old t(f). This method finds points of high curvature along the boundary, wheels a point A that is the modifier and the boundary. goints <A),, An> for which M(Ai, C), i = 1, ..., n, are all local maxima. In (ii) The Chain-code Representation - Refer to Q.2, Unit-2.

function j', based on the difference between the segment lengths of BiBi and measure of the consistency of mapping junction i to junction i' and junction j to of A, based on the difference between the angles α_i and α_j . Let $S_{ij}(i',j')$ be a B. The goal is to find an association $E = \{1, 2, ..., m\} \Rightarrow \{1, 2, ..., n\} \cup \{mssmg\}$ that satisfies $i < j \Rightarrow E(i) < E(j)$ or either E(i) = missing or E(j) = missing. Davis used constraints on both sides (line segments) and angles to define what is be converted into a model of the shape that can be used in shape recognition or nction that measures the goodness of the match of junction i of A to junction neant by a best mapping for this problem. Let M(i, j) be a local evaluation $A_{\rm b,....,}A_{\rm n}$ of junction points representing the boundary of a model object A and coordinate location (X_i, Y_i) with angle magnitude α_i . Given a sequence $A = A_1$ by the sequence of junction points $\langle \mathrm{X_i}, \mathrm{Y_i}, lpha_i
angle$ where a pair of lines meet at segments was introduced by Davis. According to Davis, a line segment sequence other matching tasks. A model for representing the matching sequences of line Once the sequence of line segments has been computed by some method, it can into a set of line segments representing near-linear portions of the boundary common representation for the boundary of a 2D shape. This representation is gnerally used after the original sequence of boundary points has been segmented similar sequence $B = B_1, B_2 \dots B_m$ representing the boundary of a test objective. (iii) A Sequence of Line Segments Representation - This is a third

AiAj. The cost of a mapping E is given by -

$$C(E) = \sum_{i=1}^{m} M[i, E(i)] + \sum_{i=1}^{m} \sum_{j=1}^{m} S_{ij}[E(i), E(j)] + P(m_B) + P(m_A)$$

Q.18. Explain the following terms Here, P is a penalty function for missing angles

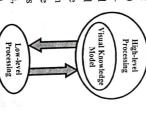
some of the same features we used to represent binary images. Commonly have value 0. Because of this relationship, it is natural to represent by using mage. The pixels of the object have value 1, and the pixels outside the object Ans. (i) Global Feature - A 2D object can be thought of as a binary Global feature (ii) Local feature.

(ii) Local Feature – A 2D object can also be characterized by local features, their attributes, and their interrelationships. The most commonly can be detected by a connected component procedure followed by boundary tracing or, if the shapes of the holes are known in advance, through the into some type of structure for matching. The most common type of structure for matching. The most common type of structure is a graph whose nodes represent local features and their properties of measurement and whose edges represent relationships among the features.

KNOWLEDGE BASED VISION – KNOWLEDGE REPRESENTATION, CONTROL STRATEGIES, INFORMATION INTEGRATION

Q.1. Explain the knowledge-based computer vision with suitable

Ars. Fig. 5.1 shows the typical architecture of a Knowledge-based Computer Vision (KBCV) a knowledge-based Computer Vision (KBCV) system structured in two different sub-systems – low-level and high-level processing. At low-level processing algorithms, usually generating feature descriptions, sets of symbolic descriptors which summarizes characteristics of data in a quantitative way. Examples of low-level processing algorithms are segmentation, color detection, texture detection, noise reduction, occlusion detection and so forth. These algorithms were the main focus of research in computer vision for a long time and had come a A long way in terms of performance.



Architecture of KBCV

1

On the other hand, high-level processing is related to the interpretation and reasoning with visual data. It is usually built on top of the low-level processing algorithms, taking features descriptors as input and generating processing algorithms, taking features descriptors as input and generating abstract, qualitative descriptions about the content of the visual data. This is abstract, qualitative descriptions, Ideally, the high-level processing can also act on called content descriptions, Ideally, the high-level processing adjusting its parameters to improved their performance the low-level processing adjusting its parameters to improved their performance based on generated content descriptions, creating a kind of feedback loop based on generated content descriptions, creating a kind of feedback loop based on generated content descriptions, creating a kind of feedback loop based on generated content descriptions, or an action of the content of the low-level processing has been implemented using the various forms of the low-level processing has been implemented using the various forms of

Each piece of knowledge can be expressed with a different rule. A

symbolic at university and the visual interpretation usually employ some sort of a priori knowledge about the visual interpretation symbolic artificial intelligence, from rule-based to probabilistic systems. They

Q.2. Explain in detail about knowledge representation.

explicit what is important and must be easy to handle. Two main knowledge representation schemes are presented in the following, production rules and representation schemes. A knowledge representation scheme must allow to bases the experts describe the contents of their knowledge using knowledge conventions to describe a piece of knowledge. In order to build knowledge Ans. A knowledge representation is a set of syntactic and semantic

production rules are as follows rule very generally expresses an "if-then" relationship. General syntax for predicate logic and the inference capabilities of modus ponens. A production Kule ruleX Production Rules - Production rules are directly inspired from

condition

comment: "a comment explaining the rule"

and/or ... condition

conclusion

can use the production rule R1bridge that during bidding one can open with a specific distribution. For example, we holds. For instance in the domain of the bridge game, if we want to express Which means that if a set of conditions are true then the conclusion

è

Rule R1bridge

comment: "bidding rule for opening"

balanced hand

12 to 15 head points

opening I no trump

head points then we can open at the level of 1 no trump. This rule means that if we have a balanced hand and between 12 and 15

pawer base can contain hundreds of production rules. It is very easy to moviledge base can production rule in a knowledge base. they are based. For rules based on propositional logic symbols represent all ges to structure the knowledge and help the reasoning. example for bidding rule R1 bridge. A usual kind of production rules are rules popositions or facts, everything is a constant. It was the case in the previous modify or remove a production rule in a knowledge base. This allows to add, modify a knowledge base. Production rules can be seen that allows to add, incomplate a knowledge base. Production rules can be grouped in different extend or update a knowledge and help the reserving not directly given in the rule but referenced through the attribute roomof 0+ order production rule, where the value of the temperature in the room is value) are used; the values can be referenced. The rule R2 shows an example based on 0+ order logic. The formalisms (object, attribute, value) or (attribute, The power of expression of production rules relies on the kind of logic

Example of 0+ order production rules are given below -

comment: "use the heater if the temperature is too low"

room-temperature < 19

change heating-status to on.

rule, where two variables M and N and one quantifier, 3, are used. variables can be used. The rule R3 shows an example of first-order production For rules based on first-order logic or predicate logic quantifiers and

example of first-order production rules are given as

comment: "track mobile regions which are possible human beings" if

3 mobile object M

shape of M = human

1.4 metres < size of M < 2 metres

the case of propositional logic; they are very modular and readable. They knowledge is fragmented, the uniform formalism for expressing the knowledge allow fast modifications of a knowledge base and explanations are easy to leads to a lack of efficiency for problem solving. provide to a user. On the contrary they have different drawbacks - the In conclusion we can say that production rules are simple, in particular in

comes from cognitive research on human reasoning. The hypothesis is that and compare them to objects or events corresponding to new situations. human beings refer when reasoning to prototypes already stored in memory (ii) Frames - A frame is a knowledge representation scheme which

well adapted for structured The concept of frames is a declarative knowledge representation scheme

Table 5.1 The General Frame Frame!

object descriptions.

Object describitoris.			
A frame is a set of	Attributes	Slots	Slot Values
attributes (or properties).	_	type	type-value
Each attribute has several		value	attribute-value
characteristics of the		default	default-value
attribute. The attributes are	2	type	type-value
very dependent on the nature	5	value	value
of object it represents. The		range-of-values	range-value
characteristics useful for any	3	type	type-value
kind of attribute; classical		value	attribute-value
slots are the type, the current	0.00	range-of-values	range-value
possible range of values.	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	default	default-value
Framel is an example of	The state of	200 OE - 1-1	200
frame with n attributes and	The state of	type	type-value
4 kind of slots. A frame is		value	attribute-value
concept, as the concept of a	The second second	range-of-value	default-value
chair.		default	default-value

Q.3. Describe various image control strategies.

Ans. Some control strategies in image processing are as follows -

description of the scene has been generated. successively manipulated and aggregated until a sufficiently high level interpreted and aggregated. The interpretations and aggregations are then only uses general knowledge about the world being sensed. In a computer solving that is data driven. It employs no object models in its early stages and vision system using a bottom-up control strategy, the observed image data is Bottom-up Control Strategy - This strategy is used for problem

generated or hypothesized. Assuming the hypothesis is true and using the solving that is goal-directed or expectation directed. A form of solution is information in the knowledge data base, the inference mechanism then infers, if (ii) Top-down Control Strategy - This strategy is used for problem

possible, some consistent set of values for the unknown variables or parameters. possible, when the problem has been solved. If a consistent set can be inferred, then a new form of colors and the inferred. If a construct set cannot be inferred, then a new form of solution is generated or bipourous of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of objects being sensed in the image is usually highly the number of types of the number of types of the number of types of the number of the number of types of the number of the number of types of types of the number of types of type byothesized. In a computer vision system using a top-down control structure, the minute and knowledge about the objects, relationships between objects, more and knowledge about the objects, relationships between objects, and the objects are the objects and the objects are the objects and the objects are the object the hypothesis is consistent with the observed data. bject parts are all known. The system hypothesizes that the image shows ar set of objects, infers values for parameters, and then tests to verify

led subproblems. The refinement continues until the most refined , in which the given problem is solved by dividing it up into a set of problem. Then each subproblem is successively divided into more dems, each of which encapsulates an important or major aspect of the (iii) Hierarchical Control Strategy - This strategy is used for problem

mponent of the inference mechanism to make a deduction, the inference led the blackboard. When the blackboard has sufficient data to permit one ving in which the various components of the inference mechanism comes available for the other components of the inference mechanism. In roblems can be solved directly. manner the inferred constraints are successively propagated and the required anism goes to work and writes its results on the blackboard where it unicate with one another through a common working data storage area (iv) Blackboard Control Strategy - This strategy is used for problem

arch is made more limited. Q.4. Which approach to the information integration problem has been

been used in computer vision. The Bayesian approach to information integration introduced by Pearl in 1987. Pearl defines a Bayesian belief network as a and A, has J possible values. For each pair of values (a; a;), the strength of the ares represent causal relationships. Assume that the nodes of the graph are value of A_j is a direct cause of the value of A_i. Assume A_i has I possible values, Variables A₁, A₂,, A_N. Each propositional variable A_i has a finite set of directed acyclic graph whose nodes represent propositional variables and whose causality is the conditional probability $P(a_i | a_j)$. These probabilities can be possible values {a_i}. An arc (A_j, A_i) from node A_j to node A_i indicates that the Ans. The Bayesian approach to the information integration problem has

that node Ai has support set Si. Then P(ai|si) denotes the joint conditional bought of as forming a $J \times I$ matrix associated with the arc. The support set of a node is the set of the node's predecessors. Assume

probability of $A_i = a_i$, given the set of value $\{s_i\}$ for the support variables, Π_{le} distribution corresponding to the entire network is then

$$P(a_1, a_2,a_n) = \prod_{i=1}^{n} P(a_i \mid s_i)$$

The matrices of strengths on each of the causal links are static input to

network to be used in image analysis is Fig. 5.2 Portion of a Belief Network = a, given all the evidence e received so B(a) denotes the probability P(a|e) of A far. The idea for a portion of a belief The dynamically changing belief value B(a) of each proposition A = a changes. through the network, the belief value the network. As information propagates

Push Buttons, Workstation **Key Board** Desk,

can be set of pushbuttons or keyboard, and object O can be a telephone or a computer terminal. Labels of "desk" for has two possible labels - object M can be a workstation or a desk, object N Where, nodes M, N and O represent objects to be identified. Each object

enters the system. The idea for a support the label of "telephone" for O, propagation of beliefs through a piece the network are updated as new evidence belief propagation defines how beliefs in label of "terminal" for O. The model of "keyboard" for N tend to support the and labels of workstation for M and M and "pushbuttons" for N tend to

of a belief network is shown in fig. 5.3. through Piece of a Belief Network Fig. 5.3 Propagation of Beliefs

are successors of node A. Here the nodes C and D are predecessors of node A and nodes W and X Let P(a | c, d) be the fixed conditional probability matrix that relates the

to their children, whereas diagnostic support represents feedback from children function but also its λ and π functions. The formula of belief updating is to their parents. Updating a node A thus involves updating not only its belief from A. Causal support represents evidence propagating forward from parents current strength of the diagnostic support contributed by an outgoing link of the causal support contributed by an incoming link to A. Let $\lambda_W(a)$ be the variable 'a' to its immediate parents c and d. Let $\pi_A(c)$ be the current strength

where α is a normalizing constant that makes $\sum B(a) = 1$. OBJECT RECOGNITION - HOUGH TRANSFORMS AND HER SIMPLE OBJECT RECOGNITION METHODS,

 $B(a) = \alpha \lambda_{W}(a) \lambda_{X}(a) \sum_{c,d} P(a \mid c,d) \pi_{A}(c) \pi_{A}(d)$

PE CORRESPONDENCE AND SHAPE MATCHING

the world, using object models which are known as priori. This task is An object recognition system finds objects in the real world from an image of suprisingly difficult. Humans perform object recognition effort lessly and introduce some techniques that have been used for object recognition in many applications. The architecture and main components of object recognition is achines has been very difficult. The different steps in object recognition and santaneously. Algorithm description of this task for implementation on Q.5. What is object recognition? And its main components. Ans. Object recognition is a technology in the field of computer vision.

Feature Detector Hypothesis Formation Candidate Objects Hypothesis Verification

recognition. It can vary from a qualitative or functional description to precise information in the model database depends on the approach used for the other objects. Size, colour, and shape are some commonly used features. considered important in describing and recognizing the object in relation to abstract feature vectors. A feature is some attribute of the object that is geometric surface information. In many cases, the models of objects are The model database contains all the models known to the system. The Fig. 5.4 Architecture of Object Recognition

of features that help in forming object hypotheses. The features used by a system depend on the types of objects to be recognized and the organization assigns likelihoods to objects present in the scene. This step is used to reduce of the model database. Using the detected features in the image, the hypothesizer organized using some type of indexing scheme to facilitate elimination of unlikely the search space for the recognizer using certain features. The model base is The feature detector applies operators to images and identifies locations

object candidates from possible consideration. The verifier then uses object to verify the hypotheses and refines the likelihood of objects the object with the highest likelihood, based on all the system then selects the object with the highest likelihood, based on all he

systems, on the other hand, rely little on the hypothesis formation and do not the classical approach. work in the verification phases. In fact, one of the classical approaches, template the classical approaches and vermination when systems use only hypothesis formation and then select object. Pattern of a state of the correct object. and verification components vary in their importance in different approaches to the second of the se All object recognitions based on these object models. The hypothesis formation their importance in different approximation approaches are a good example of this approach. Many artificial intelligence in the hypothesis formation and intelligence object recognition. Control object with highest likelihood as the correct object. Pattern classification of this approach. Many artificial install of the correct object. All object recognition systems use models either explicitly or implicitly or implicitly and a successive hased on these object models. The hypothesis form

Q.6. What are the challenges faced in object recognition?

Ans. The challenges faced in object recognition are as follows _

factors influencing the accuracy of the system. The accuracy of the modelChange in size, cropping out the background are some of the

difficult for the system to recognize the objects in the image. (ii) Adjusting brightness and contrast of the image may also make it

for the system to recognize it. The object recognition system must handle (iv) The system may fail in cases where similar objects occur in (iii) There may be cases when the object might not be visible enough

groups and are too small in size. (v) Various lightning conditions and shadows in the image may also

pose difficulty for the system to recognize the object.

Ans. The applications of object recognition are as follows – Q.7. Give some applications of object recognition.

and recognition system to identify pedestrians and cars on the roads and then make the suitable decision in accordance. Self-Driving Cars - Self driving cars may use object detection

recognition is face detection e.g. facebook recognizes people before they are (ii) Face Detection - Another application of object detection and

help medical science to detect diseases. For e.g. detecting tumors and various (iii) Medical Science - Object detection and recognition system may 319: SEC.

Trees of tra-siting

handwriting of a person. with recognition of hand poses, and sign languages letters/symbols, individual words and series of words. Ex- recognizing letters/symbols person. (v) Hand Gesture Recognition - Hand gesture recognition deals

Q.8. Explain Hough transform. Also write its advantages and disadvantages.

his method is finding imperfect instances of objects within a certain class of that can detect arbitrary shapes within a sample image. The main purpose of shapes by a voting procedure. The classical Hough transform was mainly be implemented successfully such as in medical visualization or in order to circles or ellipses. In that case appropriate parametric representation is needed introduced for the identification of lines in images, but later the Hough transform The aim of this technique is to produce a computer vision system gaine extraction method that can be used in image analysis and digital image approaches to these problems have been developed. The Hough transform has to the field of biomechanics for many years but now several automatic the vertebral bodies. The measurement of vertebral motion has been a challenge transform. In objective spinal motion imaging assessment system (OSMIA), and Iris under uncontrolled illumination can also be obtained by Hough circle Now-a-days there are a wide range of areas where the Hough transform can within an image, most commonly the extended version indulged itself in finding has been modified and extended to identify the positions of arbitrary shapes it is required to locate marker that can be used in determining the positions of achieve high accuracy in face recognition etc. The characteristics of Pupil also been introduced in morphological image processing to detect nad estimate Ans. Paul Hough patented the technique of Hough transform in 1962 is a

transform is considering the features of the straight line not as discrete image the slope-intercept model of a straight line. The main idea behind using Hough the line, and c represents the y-intercept. This form of representation is called the straight line y = mx + c can be denoted as a point (m, c) in the parameter points (x₁, y₁), (x₂, y₂), etc., but in terms of slope-intercept model. In general, line can be described as y = mx + c where the parameter m represents slope of ransform for detecting straight lines in an image. In the image space, the straight the number of red blood cells in the blood sample image. space where m represents the slope of the line and c represents the intercept. The most common application of using the Hough transform is the linear

can be exceptionally valuable when attempting to perceive lines with tiny breaks Is that the pixels present on one line need not be adjacent to one another which In them due to noise, or identification in partially occluded images. Advantages and Disadvantages - The major advantage of Hough transform

drawback that is the recognized lines are infinite lines defined by their (n, c) another termination points. With respect to minimum results when objects are associated by chance. This plainly indicates ambiguous the recognized lines are infinite lines defined by their countries. With respect to hindrances of Hough transform, then it may give ambiguous are associated by chance. This plainly indicates and the same of the same of

Q.9. Discuss about the line Hough transform.

Ans. A suitable equation for describing a set of lines in a parametric form is.

example and the fig. 5.6 shows the parametric representation of a line. presentation is described in the fig. 5.5 which shows an object taken as an orientation of r with respect to the X-axis. A suitable way of describing this where r is the length of the normal from the origin to this line and θ is the



Fig. 5.5 Gradients of the Example Fig. 5.6 Parametric Representation

known pixels that are selected for analyzing. The pair of θ and r used for parametric representation is inserted into an accumulator. When an image is analyzed the (x, y) parameters represents the well

corresponds to a set of sinusoid curves which intersects in some points. discrete in nature it only consists of a set of all possible lines in R2. It also accumulator corresponds to certain line in the image. As this accumulator is the relevant cell is increased by I. Each and every single point present in the through the point (x, y) are transformed into parametric space (θ, r) and then Another approach to think about this fact is that all the lines that go

applications such as in analyzing ultrasound images which contains some obvious noise that may causes problems in analyzing the features. gaps present in the input image. This technique can be useful in real life A very useful feature of this algorithm is its robustness against noise and

Q.10. Explain the circular Hough transform.

is used for detecting circles. It is a part of Hough transform. The reason for Ans. Feature extraction techniques, like, circle Hough transform (CHT)

> his strawer le candidates are created by "voting" and afterward nearby maxima space the circle candidates accumulator matrix. is discovering circles in blemished image. In the Hough parameter

space med in a so-called accumulator matrix. guce is characterized by space of the object of interest. A ware the basic behind the general Hough transform. The parameter A clarge of a point in the x-y plane to the parameter space may be

can be done easily. The equation of the circle is affelt, transformation of the parameter of the circle to the parameter space The line is difficult to represent in parameter space, contrasted with the

where, m, n and r are three parameters of circle, where (m, n) is centre of the $r^2 = (x - m)^2 + (y - n)^2$

circle in the direction (x, y) respectively and r is its radius. Circle can be represented in parametric form as -

$$x = m + r \cos \theta$$

 $y = n + r \sin \theta$

parametric representation of the circle, the range can be held constant or a parameter fitting in with two dimensional or at most three dimensional. The transform complexity too increases. Therefore straightforward shape with ixed number of radii can be set. the measurement of the parameter space expand, simultaneously the Hough quantity of parameter expected to portray the shape increment and in addition dimensional, though the line just had a place with two dimensional. As the Along these lines the circle's parameter space shall fit in with three

Hence the highest number relate to the centre of the circle in the image. urcles passing through the individual coordinate stored at the accumulator. edge-point and each preferred radius is utilized, then we can get the number of radii increasing and updating the value in our accumulator. Now, when each the information image drawing circle with the wanted circle with preferred craved range. The drawn circle attracts the parameter space, such that our xaccumulator matrix is incremented. Hence, we clear over vitality edge-point in accumulator matrix has identical size as parameter space. Value in our axis, y-axis, and z-axis are m-value, n-value, and the radii respectively. At every edge-point we draw a circle with centre in the point with the

Q.11. Explain in brief about the patterns and pattern classes.

recognition by machine involves techniques for assigning patterns to their respective classes automatically and with as little human intervention as classes are denoted p₁, p₂, ..., p_N, where N is the number of classes. Pattern class is a family of patterns that share a set of common properties. Pattern used often in the pattern recognition literature to denote a descriptor. A pattern Ans. A pattern is an arrangement of descriptors. The name feature is

(for quantitative upon the properties of the pro for quantitative descriptions) and strings (for structural description) and strings (for structural description) are vector like x, y and z, and b. allower letters like x, y and z, allower letters like x, y and z, and z, and z, and z, and z, and possible. The two principal pattern arrangements used in practice are vector of the five descriptions) and strings (for structural description), b...

$$\mathbf{x} = \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \\ \vdots \end{bmatrix}$$

computation to use row vector of dimension $1 \times n$, obtained simply by forming of such descriptors associated with the pattern. Sometimes it is necessary in where each component x, represents the ith descriptor and n is the total number

used to describe the physical pattern itself. The nature of the component of a pattern vector \mathbf{x} depends on the approach

Q.12. Discuss the recognition based on decision theoretic method.

the property that, if a pattern x belongs to class p_p then of decision function. Let $\mathbf{x} = (x_1, x_2, ..., x_n)^T$ represent an n-dimensional pattern theoretic recognition is to find N decision function $d_1(x), d_2(x), ..., d_N(x)$ with vector. For N pattern classes $p_1, p_2, ..., p_N$, the basic problem in decision Ans. The decision theoretic approaches to recognition are based on the $_{\rm lig}$ $d_i(x) > d_j(x)$ $J = 1, 2, ..., N j \neq i$

for which $d_i(x) = d_j(x)$ or, equivalently, by values of x for which The decision boundary separating class p_i from p_j is given by values of y $d_i(x) = d_i(x) = 0$

class p_i and $d_{ij}(x) < 0$ for patterns of class p_j . by the single function $d_{ij}(x) = d_i(x) - d_j(x) = 0$. Thus $d_{ij}(x) > 0$ for patterns of Common practice is to identify the decision boundary between two classes

Q.13. Discuss about the structural methods.

AT THE PROPERTY OF THE PARTY OF of matches between the two strings where a match occurs in the kth position if $x_k = y_k$. The number of symbols that do not match is denoted $x_1 \, x_2 \, ... \, x_n$ and $y_1 \, y_2 \, ... \, y_m$ respectively. Let α represent the number recognition. Suppose that two region boundaries x and y are coded into strings Ans. Strings are the most practical approach in structural pattern $\beta = \max(|x|, |y|) - \alpha$

> Here we still the shown that $\beta=0$ if and only if x and y are identical. of the argument are measure of similarity between x and x in all and y are identical. A simple measure of similarity between x and y is the ratio Here, |arg| is the length (number of symbols) in the string representation Here, |arg| is the length (number of symbols) in the string representation

$$= \frac{\alpha}{\beta} = \frac{\alpha}{\max(|x|, |y|) - \alpha} \dots$$

the amount of computation. by symbol the starting point on each boundary is important in terms reducing concesponding symbols in x and y match. Because matching is done symbol Hence R is infinite for a perfect match and 0 when none of the

of R gives the best match. which consists of starting at arbitrary points on each string and then shifting so long as it provides a computational advantage over brute force matching, one of the string and computing equation (ii) for each shift. The largest value Any method that normalizes to, or near, the same starting point is helpful,

Q.14. Discuss about the affine matching.

of quality of the transformation. Suppose an image I containing n feature transforming the model to image coordinates and determining the fraction of between an object and model basis and then verifies the hypothesis by computes an affine transformation based on an hypothesized correspondence 10 match objects. The first alignment, also called hypothesis and test. It points, alignment consists of the following stepsmodel and image points brought into correspondence. This is taken as a measure ans. In affine transformation, there are two main approaches proposed

for each model M. Let m be the number of model points

for each triple of model points do

for each triple of image points do hypothesize that they are in correspondence and

compute the affine transformation based on this correspondence.

for each of the remaining m - 3 model points do

apply that transformation

Find correspondences between the transformed model points and the image points

Measure the quality of the transformation (based on the number of model points that are paired with image points.)

It consists of representing each model object by storing information-invariant points, since it is known that they uniquely determine an affine transformation. These steps are repeated for all possible groups of three model and image The second method, geometric hashing or indexing is a table lookup method.

Scanned with CamScanner

noncollinear points are affine invariant. The algorithm consists of the consis to as geometric including the second in the second in the coordinates of a point into a reference frame consisting of the invariant. The algorithm consisting of the second interval in the second in the table to Ima pussion..... to as geometric hashing for point set matching is based on the following for point into a reference frame consisting of a point into a point in time, similar invariance of the model the indexing mechanism, recutoring is based on the fall. information about it in a hash. This table is compiled offline. At recognition

Algorithm of Preprocessing Phase _

for each model M. Let m be the number of model points for each triple of noncollinear model points do for each of the m-3 remaining model points do form a basis (reference frame) as an index to an entry in the hash table, Use the triplet of coordinates (after a proper quantization) determine the point coordinates in that basis.

Algorithm of Recognition Phase where the pair (M, basis) is stored.

for each entry of the hash table do set a counter to 0

Choose three noncollinear points of I as a basis. for each of the n-3 remaining image points do Use the triplet of coordinates (after a proper quantization) determine its coordinates in that basis.

Q.15. Describe the dynamic programming. Find the pair (M, basis) that achieved the maximum value of the counter when summed over the hash table. as an index to an entry in the hash table and increment the

Three types of edit operations, namely, insertion, detection, and change, are matching problem. The string matching algorithm is as follows or concavity are considered. The matching problem becomes then a string of the boundary into convex/concave parts, there might be just three symbols (for convex, concave, and straight) or more if different degrees of convexity boundary segments. For instance, if the segments result from the decomposition contours. A shape boundary is described by a string of symbols representing Let $X = a_0$ a_{n-1} and $Y = b_0$ b_{m-1} be two strings of symbols Ans. A number of approaches use dynamic programming to match shape

defined to transform X into Y.

where h is the null symbol (1) Insertion – Insert a symbol 'a' into a string, denoted as $\lambda \to a$

g(X, Y). Let E(0, 0) = 0; then E(i, j), 0 < i < n, 0 < j < m is given by distance between the substrings a_0, \ldots, a_i and b_0, \ldots, b_j . It is E(n, m) = 0(X, Y) is defined as the minimum of such total costs. Let E(i, j) be the given by the sum of the costs of the individual operations. The edit distance The cost of a sequence of edit operations that transforms X into Y is A nonnegative real cost function $d(a \rightarrow b)$ is assigned to each edit operation (ii) Deletion – Delete a symbol from a string, denoted as $a \to \lambda$. (iii) Change - Change one symbol into another, denoted as $a \rightarrow b$.

 $E(i, j) = \min \left\{ E(i, j-1) + e(\lambda \rightarrow b_j) \right\}$ $E(i-1, j-1) + e(a_i \rightarrow b_j)$ $E(i-1,j) + e(a_i \rightarrow \lambda)$

time complexity is given by O(nm). The space complexity is also quadratic. next one, then when computing E(i, j) the values that are needed have already been computed. Since it takes constant time to compute E(i, j), the overal If the elements of the table are computed horizontally from each row to the nondecreasing path in the 2D table E(i, j) from the entry (0, 0) to the entry (n, m)The matching problem can be seen as one of finding an optimal

Q.16. Write short note on shape matching.

starting point for the local phase, and which enables us to perform the MRF reduced affine transformation model, which is sufficient to provide an initial the transformation space of each shape. To address this issue, we introduce a Transformations. The efficiency of this formulation relies on effectively sampling we extend the MRF formulation, due to its ability to handle noisy relative the relative transformations $T_{(i,j)}$. Among existing formulations to this problem, **optimizing** the consistency between the induced transformations $T_j^{-1} \circ T_j$ and second step jointly computes an affine transformation T; for each shape by **snapes along** with associated relative transformations $T_{(i,j)}$, $(i,j) \in G$, and the pair-wise affine matching to construct a similarity graph G among the input wo-step strategy of matching multiple shapes, where the first step performs and all shapes are roughly aligned in Σ . This is done by following the principal we jointly compute an affine transformation T; for each shape S; so that in the stage can be divided into a global phase and a local phase. In the global phase, that corresponding parts on different shapes can be easily compared. This Ans. The first stage aligns the input shapes in the common space Σ , so

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optimization as sequential manner. In this case, we only need to sample a 1D space optimization for each type of 1D transformation (e.g., the rotation in the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation in the sample a 1D transformation (e.g., the rotation end).

manner. In particular, at each step the deformation F_i of each shape can beintroduce an objective function, which can be optimized in an alternating optimizing the deformations of all input shapes in large shape collections, we which can be optimized in an all of the collections, we III the recommendation of all input shapes in large shape collections of all input shapes in large shape collections. In the local phase, we proceed to jointly optimize a free-from deformation regulare the density of x, given y, is Gaussian. Scaled eigenvectors of C_x are because of A in the maximum likelihaad and maximum lik delical Gaussian white noise. It is now easy to formulate the likelihood function, had density of x, given y, is Gaussian. Scaled signature of the signature of

PRINCIPAL COMPONENT ANALYSIS, FEATURE EXTRACTION NEURAL NETWORK AND MACHINE LEARNING FOR IMAGE SHAPE RECOGNITION

Q.17. What do you mean by principal component analysis?

allows interpretations that would not ordinarily result. PCA often reveals relationships that were not previously suspected and thereby set of variables. The initial data can then be projected onto this smaller set. reduces the attribute set size by retaining a subset of the initial set of attributes, PCA "combines" the essence of attributes by creating an alternative, smaller resulting in dimensionality reduction. Unlike attribute subset selection, which where $k \le n$. The original data are thus projected onto a much smaller space, dimensional orthogonal vectors that can best be used to represent the data, PCA (also called the Karhunen-Loeve, or K-L, method), searches for k $_{\rm I}$. described by n attributes or dimensions. Principal components analysis, or Ans. Suppose that the data to be reduced consist of tuples or data vectors

transforms are more suitable for data of high dimensionality. transforms, PCA tends to be better at handling sparse data, whereas wavelet to multiple regression and cluster analysis. In comparison with wavelet the problem to two dimensions. Principal components may be used as inputs Multidimensional data of more than two dimensions can be handled by reducing unordered attributes and can handle sparse data and skewed data PCA is computationally inexpensive, can be applied to ordered and

Q.18. What do you mean by factor analysis?

generative latent variable model underlying statistical model. However, PCA can also be derived from a Ans. The PCA model generally used is a distribution-free method with no 13.56

X = Ay + n

case when the noise tends to zero. are called specific factors, instead of noise. Let us make the simplifying interpretation that the elements of y are the unobservable factors. The elements plactor analysis is different from PCA. Factor analysis was originally developed officior analysis (FA). It is called principal factor analysis. Generally, the goal by any α are noise tends to zero. usumption that the data has been normalized to zero mean. of matrix A are called factor loadings. The elements of the additive term n associal sciences and psychology. The model has the form of, with the This approach is one of the methods for the classic statistical technique

that we can assume Gaussian, and their variances can be absorbed into the unknown matrix A so In FA we assume that the elements of y (the factors) are uncorrelated and

 $E\{yy^T\} = I$

observations from equation (i) as the special case of principal FA. We can write the covariance matrix of the noise elements are generally not assumed to be equal or infinitely small, as in factors y_i ; denote $Q = E \{nn^T\}$. It is a diagonal matrix, but the variances of the The elements of n are uncorrelated with each other and also with the

 $E\{xx^{T}\} = C_x = AA^{T} + Q$

the observed covariances from equation (iii). There is no closed-form analytic o-variance matrix. The main problem is then to solve the matrix A of factor solution for A and Q. loadings and the diagonal noise covariance matrix Q such that they will explain In practice, we have a good estimate of C_x available, given by the sample

which $TT^{T} = I$), will produce exactly the same left-hand side. We need some orthogonal transform or rotation of $A \rightarrow AT$, with T an orthogonal matrix (for be used instead. Clearly, this problem does not have a unique solution - any cannot be exactly solved; something similar to a least-squares solution should much smaller than the number of dimensions in the data, so this equation $\operatorname{rom} AA^{T} = C_{x} - Q_{x}$. The number of factors is usually constrained to be Assuming Q is known or can be estimated, we can attempt to solve A

FA typically tries to solve the matrix A in such a way that the variables would extra constraints to make the problem more unique. Now, looking for a factor-based interpretation of the observed variables,

have high loadings on a small number of factors, and very low loadings or remaining factors. The results are then easier to interpret. This principle has a varimax, quartimax, and oblimin rotations. been used in such techniques as varimax, quartimax, and oblimin rotations, and oblimin rotations,

have been found, the original observations can be readily expressed as their all the principal components are retained. Once the principal components are retained once the principal components in the principal components are retained. variance maximization or minimum mean-square error representation. The can be derived from one. It is a linear transformation that is based either on minimum mean-square error representation of the contraction of the PCA model is invertible in the (theoretical) case of no compression, i.e., when Principal component analysis is not based on a generative model, although it is a linear transformation that is based and it is based and it.

obtained as linear functions of the observations linear functions as $x = \sum_{i=1}^{n} y_i w_i$, and also the principal components are simply

$$y_i - w_i x$$

eigenvectors of C_{κ} ; several different estimation methods exist. specific factors or noise which is considered important in some application directly computed from the observations. This is due to the additive $term\ _{0f}$ expressed in terms of the factors, but the values of the factors cannot be fields. Further, the rows of matrix A are generally not (proportional to) The FA model is a generative latent variable model; the observations are

method of determining the factor rotation. redundancy of the FA model. In fact, ICA can be considered as one particular and non-Gaussian – a much stronger assumption that removes the rotational factors or independent components are assumed to be statistically independent Gaussian data. ICA is a similar generative latent variable model, but now the is due to the assumption of Gaussianity of the factors. The factors are further assumed to be uncorrelated, which also implies independence in the case of covariances between the observed variables are used in the estimation, which FA, as well as PCA, is a purely second-order statistical method - only

Q.19. Write the general procedure of principal component analysis (PCA)

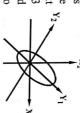
the same range. This step helps ensure that attributes with large domains will Ans. The basic procedure of PCA is as follows -(i) The input data are normalized, so that each attribute falls within

not dominate attributes with smaller domains,

components. The input data are a linear combination of the principal perpendicular to the others. These vectors are referred to as the principal the normalized input data. These are unit vectors that each point in a direction PCA computes k orthonormal vectors that provide a basis for

> new set of axes for the data, providing important "significance" or strength. The principal components essentially serve as a (iii) The principal components are sorted in order of decreasing

groups or patterns within the data. the axes X_1 and X_2 . This information helps identify shows the first two principal components, \hat{Y}_1 and among the data, the second axis shows the next are such that the first axis shows the most variance information about variance. That is, the sorted axes Y2 for the given set of data originally mapped to highest variance, and so on. For example, fig. 5.13



of the original data. order of "significance", the size of the data can be reduced by eliminating the principal components, it should be possible to reconstruct a good approximation weaker components, that is, those with low variance. Using the strongest (iv) Because the components are sorted according to decreasing

Q.20. Explain PCA with example.

graph is decomposed into 10 images (each feature vector corresponds to one on this basis. For example, we select the feature values of the 10 largest in PCA. We think the matrix as a space, then for a symmetric positive definite the eigenvalue is, the more information corresponding eigenvector can have sigenvalue of an image to reconstruct the image as shown in fig. 5.8, the matrix A, its eigenvectors are orthogonal to the space formed by A. The larger Ans. Eigenvalues and eigenvectors are the two most important concepts



Fig. 5.8 The 10 Images Corresponding to the First 10 Principle Eigenvector

difference to the original one, the space composed by the 10 feature vector contains 95% energy of the original image. If the 10 images are superimposed, we can get a picture with not much

The following steps will show how to make the maximum variance and how make the variance of the data distribution are the principal component of the maximum variance and the maximum variance a The idea of PCA is to reduce the data dimension to the dimension make the variance of the data distribution maximum. Those dimensions that the principal common that the princ

that is, all the sample points X minus the mean and divided by the variance law Moving the data center to 0 co-ordinates and normalize the data the mean and divided by the various

P dimensional space, the co-ordinates obtained in P dimensional space, orthogonal vasus of L--, I UT, U is an orthogonal matrix, so $P = U^T$, sample point Xi is project to the orthogonal basis is U = [U1, U2, ..., Up]. The projection matrix is P = [U1, U2, ..., Up]. The projection matrix is P = [U1, U2, ..., Up]. necessary to multiply the projection matrix P, set the P dimensional matrix is not set the p dimensional matrix. and now each sample point is projected to the P dimensional space, it is (ii) Assume that the space after dimension reduction is P dimension is P dimension to the P dimensional control of the P dimensional

dimensional space, then we need to compute the variance, obviously, data variance (iii) Now we get the co-ordinates of each sample point in the lower

after computation, in which Σ is the covariance matrix of X. $\sum_{\mathbf{i}} \mathbf{y_i^T} \mathbf{y_i^i}$, then the variance of the data distribution can be represented as $\mathbf{U^T}_{\Sigma U}$ after dimension reduction is $\sum_i y_i^T y^i$, the value y in step 2 can be carried into

we only need to project x to U, then our goal of dimension reduction can bbasis of the space is U, the U represent the space. As for each new sample $point_X$ Now we get a lower dimensional space, the matrix composed by P orthogonal

achieved. Therefore, the vector after dimension reduction is $y \approx U^T x$. Q.21. What is feature extraction? Discuss advantages of the feature

engineering. Feature engineering is an informal topic, but it is considered are enhanced by constructing set of application-dependent features called feature dimensional data into low dimensional space. The feature extraction results for dimensionality reduction. Feature extraction is used to encode the high essential features. The feature extraction techniques aimed on global structure of decision support system as it identifies abnormal one through selecting the learning problems. Features extraction is an essential one for the implementation Ans. Feature extraction is an essential process for addressing the machine

generate other features that are more significant "Feature extraction is generally Features extraction performs some transformation of original features to

> the information (measured through the variance). that minimizes the redundancy (measured through covariance) and maximizes from a set of redundant or noisy data. PCA is a linear transformation of data introduced by Karl. Many variants of PCA have been proposed. PCA is a used feature extraction approach is Principle Component Analysis (PCA) simple non-parametric method used to extract the most relevant information inear combination of original input variable. The most popular and widely features which have good discriminatory power between classes." An important a simple representation of data representing each variable in feature space as a reatures extraction can be used in this context to reduce complexity and give Intelligence is facing in finding a suitable representation of multivariate data. problem in Neural Networks research and other disciplines like Artificial used to mean the construction of linear combinations aTx of continuous Unit - V 159

removes irrelevant features to acquire higher prediction accuracy during disease medical dataset for efficient disease prediction. The feature extraction technique reduction. Feature extraction is a key process to reduce the dimensionality of diagnosis. of extracting the relevant features from large database for dimensionality Advantages of Feature Extraction - Feature extraction is the process

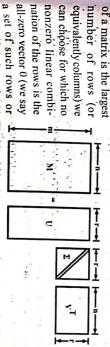
without losing a lot of information of the original feature space. In feature extraction, size of the feature space can often be decreased

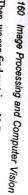
Q.22. Explain the principle of SVD.

number of dimensions. representation to produce an approximate representation with any desired matrix, and also makes it easy to eliminate the less important parts of that singular-value decomposition (SVD), allows an exact representation of any dimensional representation of a high-dimensional matrix. This approach, called Ans. Let us consider a second form of matrix analysis that leads to a low-

that connect the rows and columns of the matrix. Let M be an m x n matrix, and let the rank of M be r. Recall that the rank We explore the idea that the SVD defines a small number of "concepts'

all-zero vector 0 (we say nonzero linear combican choose for which no nation of the rows is the equivalently columns) we number of rows (or of a matrix is the largest 2 11





Then, we can find matrices U, \(\Sigma\), and V as shown in fig. 5.9 with the following

(i) U is an m × r column-orthonormal matrix; that is, each of is

use V in its transposed form, so it is the rows of VT that are orthonormal. columns is a unit vector and the dot product of any two columns is 0. (ii) V is an n × r column-orthonormal matrix. Note that we always

are 0. The elements of Σ are called the singular values of M. Q.23. What do you mean by singular value decomposition? (iii) \(\Sigma\) is a diagonal matrix; that is, all elements not on the main diagonal

SVD can be seen as a method for data reduction. best approximation of the original data points using fewer dimensions. Hence, that once we have identified where the most variation is, it is possible to find the exhibit the most variation. This ties into the third way of viewing SVD, which is a method for identifying and ordering the dimensions along which data points the various relationships among the original data items. At the same time, SVD $_8$ transforming correlated variables into a set of uncorrelated ones that better expose compatible points of view. On the one hand, we can see it as a method for Ans. Singular value decomposition (SVD) can be looked at from three mutually

as possible along the second dimension of the original data second regression line, perpendicular to the first, shown in fig. 5.11. This line captures as much of the original variation as possible. Notice that there is a datapoint, we would have a reduced representation of the original data that line, and took the intersection of those lines as the approximation of the original point and the line. If we drew a perpendicular line from each point to the regression in the sense that it is the line that minimizes the distance between each original of the original data with a 1-dimensional object (a line). It is the best approximation fig. 5.10. The regression line running through them shows the best approximation As an illustration of these ideas, consider the 2-dimensional data points in

visible at first glance. original data not necessarily show subgroupings in the uncorrelated data points that will possible to use these regression ines to generate a set of variation to begin with. It is dimension exhibiting less because it corresponds to a approximating the original data set. It does a poorer job of

Fig. 5.10 Best-fit Regression Line Reduces Data from Two Dimensi into One

> been preserved. main relationships of interest have educe data but be assured that the NLP applications is that we can east. What makes SVD practical for imply ignore variation below a orders it from most variation to the rticular threshold to massively highly variable set of data points and the original data more clearly and pace that exposes the substructure ducing it to a lower dimensional tal are taking a high dimensional The basic ideas behind SVD

Fig. 5.11 Regression Line Along Second Dimension Captures Less Variation in

Original Data

Q.24. How does a neural network work? Explain.

is the result of the pattern of connections and weights, that is, according to the input vector x to the output vector y, where the transformation performed he values of the weight matrix W. Ans. A neural network can be thought of as a black box that transforms

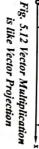
Consider the vector product

his product. It is equivalent to projecting one vector onto the other vector in n-dimensional There is a geometric interpretation for

This notion is depicted in fig. 5.12 for

the two-dimensional case. The magnitude of the resultant vector is given by

 $x*w = \sum x_i w_i$



inputs to the nodes in a neural network. **roduct** is a minimum when both point in opposite directions or when $\theta = 180^{\circ}$ **The Example 1** when both vectors point in the same direction, that is when $\theta = 0$. The This illustrates how the vectors in the weight matrix W influence this

"nere |x| denotes the norm or length of the vector x. Note that this product is

 $x*w = |x| |w| \cos \theta$

Q.25. Find all possible stable states of the neural network

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inactive. In the Bivelines of the connected to each other with weighted connection shows that the two units which the two units to desart to the connection shows that the two units to desarts to the connection permits an active unit to desarts to the connection permits and the connection to the connection permits and the connection permits are connected to each other with the connection permits are connected to each other with the connection permits are connected to each other with the connection permits are connected to each other with the connection permits are connected to each other with the connection permits are connected to each other with the connection permits are connected to each other with the connection permits are connected to each other with the connection permits are connected to each other with the connected to Connections. A pour connection permits an active unit to deaching. processing elements, or inactive. In the given figure, unit filled by black color is active and units which the connected to each other with units which Ans. The above problem is an example of a simple Hoffield net. In which

(One For Each of Ten Vowels)

Unit - V 163

process repeats until the network reaches a stable state, i.e., until no more active, otherwise it becomes inactive. Another random unit is selected, and the connections to those active neighbours. If the sum is positive, the unit become neighbours are active, the unit computer the sum of the weights on the The network works as follows. A random unit is selected. If any of light

stable states of the given figure. Thus by following above procedure, we can determine all the possible

Fig. 5.14 The Four Stable States of the Hopfield Network

Q.26. Discuss the applications of neural network. (R.G.P.V., June 2009)

Write short note on applications of neural network.

(R.G.P.K., June 2010, 2011, May 2018)

network is trained to output one of ten vowels, given a pair of frequencies network can be trained to discriminate between different vowel sounds. The speech recognition. Fig. 5.15 shows how a three-layer back propagation task Connectionist networks have been applied to a number of problems in Ans. The various applications of neural networks are discussed as below-Give any three applications of neural network. (R.G.P.V., June 2016) (i) Connectionist Speech-Speech recognition is a difficult perceptual

Systems to demonstrate that connectionist methods could be applied to real-NET talk, a network that learns to pronounce English text, was one of the first is easier than speech recognition, and high performance programs are available. than viceversa - has also been attacked with neural networks. Speech production Speech Production - The problem of translating text into speech rather

(First and Second Formants)



Fig. 5.15 A Network That Learns to Distinguish Vowel Sounds

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talk succeeds fairly well at this task with a back propagation network. the network will discover the regularities and remember the exceptions. NET simply to present a network with words and their pronunciations, and hope that with one another in unpleasant, unforeseen ways. A connectionist approach is them. Unfortunately, most of the rules have exceptions - consider "xylophone" world be to write all these rules down and use a production system to apply with as "ks" sound, as in "box" and "are". A traditional approach to the problem speech units called phonemes. For example, the letter "x" is usually pronounced and these exceptions must also be programmed in. Also, the rules may interact Linguists have long studied the rules governing the translation of text into

both the engineering and biological aspects of massively parallel vision. of the world. These severe timing constraints strongly suggest that human vision is highly parallel. Connectionism offers many methods for studying interpretations to enable the construction of a stable three-dimensional model the problem, each interpretation must be rapidly integrated with previous scene must be interrupted in about a hundred computational steps. To compound Since individual neural firing rates usually lie in the millisecond range, each resolution; as a result, we must constantly shift our attention among various points of interest. Each snapshot lasts only about two hundred milliseconds. with limited hardware. Only the center of the retina maintains good spatial (ii) Connectionist Vision - Humans achieve significant visual prowess

dissenters. The relaxation process settles on the most likely set of edges in the scene. While traditional vision programs running on sexual computing engines many units think they are located on an edge border, they can override any on the influences of nearly units one use for relaxation is detecting edges. If from a video camera and then these activations are iteratively modified based In a typical system, some neural units receive their initial activation levels Parallel relaxation plays an important role in connectionist vision systems.

i.e., it will violate one constraint if necessary to satisfy the others. Hachiers technique for combining them. Because relaxation treats constraints as sometimes of the constraints are sometimes of the constraints as sometimes of the constraints are someti and texture, uncumularly more structure, then parallel relaxation is an attractive and texture and texture and texture and texture are relaxation treats constraints and attractive and texture and texture are relaxation treats constraints and attractive and texture are relaxation treats constraints are relaxation treats constraints are relaxation treats. and texture, then they are probably part of the same object. If these constraints then parallel relaxation is an attention of the same object. Visual Illicipionics. For example, if two adjacent areas in the score have the same object. If these constraints of the same object. If these constraints of the same object. must reason about which regions of a score require edge detection processing assumes massively parallel machines. must reason about the connectionist approach simply assumes massively parallel machinery, also requires the integration of many. Visual interpretation also requires the integration of many constraint.

The same of the s

to come up with approximate solutions to the to solve many other constraint satisfaction problems. Hopfield and Tank slow a global best-fit interpretation even in the presence of local ambiguity or noise (iii) Combinatorial Problems - Parallel relaxation can also be used

F, C, A, and back to D. the next city by column 2, etc. The tour shown Fig. 5.16 The Representation city is marked by the active unit in column 1, horizontally across the columns. The starting row stands for one city. The tour proceeds how tours themselves are represented. Each number of cities to be toured. Fig. 5.16 shows employs n² neural units, where n is the traveling salesman problem. The system

if city D is far from city G then the fourth unit in column 3 will strongly inhibit the proportion to the distances between cities represented by their rows. For example can only be visited once. Third, units in adjacent columns inhibit each other # visited. Second, every unit inhibits every other unit in its row, because each on weight to every other unit in this column, because only one city at a time can k of a particular problem instance. First of all, every unit is connected with a negative connections. The connection weights are initialized to reflect exactly the constraint Like all Hopfield networks, this n by n array contains a number of weighted of a Travelling Salesman

particular city in a short tour. To find that tour, we start out by giving our units absence of strong inhibition, individual units will prefer to be active. seventh units in columns 2 and 4. There is some global excitation, so in the Notice that each unit represents some hypothesis about the position of

play backgrammar to classify sonar signals, to compress images, and to drive until a stable state is reached. Stable states of the network correspond to shot themselves asynchronously according to the rule. This updating continue random activation values. Once all the weights are set, the units update Other tasks successfully tackled by neural networks, include learning w

> drawbacks of neural network? 0,27. Briefly explain the applications of neural networks. What are the Unit - V 165

(R.GP.V. Dec. 2009)

prawbacks - Drawbacks of neural network are as follows -

Ans. Applications - Refer Q.26.

The neural network needs training to operate,

subjective symptoms and changes after administration of nitroglycerine. network was trained not only by enzymatic data, but also by EKG-phenomena, group developed an integrated decision support system in which a neural proved to be 100% with an 8% false positive rate. Later, the same research trained for the analysis of these heart enzyme levels. Diagnostic accuracy acute myocoardial infarction (AMI) diagnostics. A neural network has been Ans. The applications of neural network in medical field are as follows -(i) Cardiology - Serum enzyme level analysis forms the basis of (R.G.P.V., Nov. 2018)

rate regulation but ortizetal used them to examine heart failure. cardioverter defibrillators. Neural networks have been used to model heart Neural networks were used to study the sophisticated control of

findings in an integrated system is thought to be useful in the diagnostic process. of breast cancer that evaluation of mammographic, cytological and epidemiological status, number of palpable lymphatic nodules, etc.). Neural network recognition data from lymphatic node positive patients (tumor size, tumor hormone receptor the possible recurrence rate of turnors correctly in 960 of 1008 cases by using and selection of therapeutic strategies in breast cancer. A neural network judged (ii) Oncology - There are several systems available for the diagnosis

network analysis of brain SPECT image data. between Alzheimer disease and vascular dementia can be assisted by neural (iii) Neurology - The sometimes difficult differential diagnosis

for the diagnosis of pulmonary embolism. In contrast, neural networks were more accurate than 2 well trained experts such disorders was less successful than conventional classification methods. Pulmonary nodules. According to their results, neural network analysis of together on the development of a system for the classification of solitary (iv) Pulmonology - Pulmonologists and radiologists have worked

be most interesting and most powerful in the field of radiology. Images contain (v) Radiology - To date, the application of neural networks seems to

Q.28. Discuss the applications of neural network in medical field.

architecture of the microprocessor therefore needs to be emulated. (iii) Requires high processing time for large neural networks. (ii) The architecture of a neural network is different from the

Scanned with CamScanner

interpret tnen usung value recess, neural network modeling becomes suitable for much information and the interpret then using conventional rule based systems. By selecting an appropriate the selecting and appropriate the selecting appropriate the selecting appropriate the selection appropr much information and they are so complicated that it's all but impossible to

of liver diseases. The network achieved a recognition accuracy somewhere between the results of residents and those of certified radiologists. and laboratory findings, a neural network was created to diagnose five classes enough data for the differentiation of liver diseases. Based on ultrasonographic Abdominal ultrasound and laboratory investigations do not usually provide

Hearing-aids can well be improved by using neural networks for noise filtering useful for understanding, modeling and treating speech and hearing impairments new and effective method for modeling hearing. This technique could become Table 5.2 shows some other applications of neural networks in medical (vi) Otorhinolaryngology - Neural networks have proven to be a

Table 5.2 Applications of Neural Net

iscipline e e	Application Field Diagnostics, Prognostics Diagnostics Prediction Production
Oncology Paediatrics Neurology EEG Otology-Rhinology-Laryngology Obstetrics and Gynaecology Ophthalmology Radiology	Diagnostics, Prognostics Diagnostics, Prognostics Diagnostics Signal processing, Modelling Diagnostics Signal processing, Modelling Prediction Signal
Clinical chemistry Pathology Cytology Genetics Biochemistry	Signal processing, Modelling Signal processing (X-ray, US, CT) Signal processing, Diagnostics Diagnostics, Prognostics Diagnostics, Re-screening Protein secure
Q.29. Discuss about the convolutional neural networks (CNNs).	ork in the field of Co.

providing better results. For the object detection purpose the most pears in the convolutional networks are going towards deep computational better results. For the chieat data-etthe development of hardware have empowered machines with more popular and used deep learning models consist of the recurrent convolutional

the sides of validity it is more naturally and simply in term of capturing an to the image recognition of objects in the air from the past few years. From convolutional neural networks (CNNs) have been applied with great success convolutional neural networks (CNNs) are becoming important. In the meantime areas in recognition and robotic field. There are a number of reasons that machine learning and computer vision problems. These are used in variety of Convolutional Neural Networks (CNNs) are much successful in various

of CNNs can be controlled by varying their depth and breadth due to their and parameters and that is why they are easier to train. In addition, the capacity networks with similarly-sized layers, CNNs have much fewer connections pixel dependencies are. Thus, compared to standard feed-forward neural architecture performance. CNNs assumes the nature of the image, such as static images and where

unrelated of variations. aspects of the input which are important for discrimination and limit of simple modules such as convolutional layer, pooling layer and fullyfor recognition tasks, higher ranking of dataset representations an increase representation at one level into a higher and more abstract level. Meanwhile, connected layer. Starting with the raw input, each module transforms the Consequently, the typical architecture of CNNs is a multilayer stack

and cause problems in transfer learning. casons, for example, the dataset may not be enough to train the full neural net carning is useful when someone wants to train on their own dataset for various urthermore, in deep learning techniques, besides data formation, transfer ne domain of pattern recognition. It allows a model that consists of multiple chieved great performance improvement in large-scale image classification rocessing layers to study data representation with various levels of abstraction. isks and set off the upsurge of deep learning besides it is a new hot spot in The deep learning technique based on convolutional neural network has

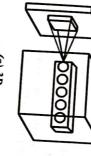
over fitting with small samples. In this review, the technique of machine learning it has been observed that deep neural networks (DNNs) easily suffer from convolutional layer) and training those layers on the related dataset. Nevertheless, neural networks, replacing the fully-connected layers (and potentially the last Specifically, transfer learning may be used to take a pre-trained deep

a convolutional network, it is in use for a long time and got popularity in recent Ans. The most popular neural network in the field of computer vision is

is important to ensure the quality and efficiency of image in terms of capturing verification and clustering that want to train more effectiveness especially in image recognition by using the accurate learning machines method.

Q.30. Explain in detail about the convolution layer,

the complex arrangement of cells in the mammalian brain's visual cortex. convolutional layers – or convolutional networks in general – is loosely based on but extend through the full depth of the input volume. The architecture found in consist of a set of learnable filters or kernels, which have a small receptive field making geometric assumptions about the input data. The layer's parameters which have a small recognitions neural network and aims to resolve the limitations of fully connected layers by Ans. The convolutional layer is the core building block of a convolutional layer is the limitations of fully connected to the limitations of the limitations of fully connected to the limitations of the l





During the forward pass, the learnable filters are convolved with the input Fig. 5.17 Input, Filter and Output of a Convolution in 2D and 3D

filter over the input volume at different overlapping spatial locations as in volume. The intuition behind the discrete convolution operation is to slide a $\mathbf{x}_{\mathbf{f}}^{(\ell)} = \sum_{\mathbf{x}_{\mathbf{u}\mathbf{v}}} \mathbf{x}_{\mathbf{u}\mathbf{v}}^{(\ell-1)} *_{\mathbf{w}}^{(\ell)} + \mathbf{b}_{\mathbf{f}}^{(\ell)}$

and vertical direction is given by u and v. the output of the previous layer, and the spatial extent of the filter in horizontal where $\mathbf{x}_{\mathbf{f}}^{(\ell)}$ represents the current layer's output for a given filter $\mathbf{f}, \mathbf{x}^{(\ell-1)}$

function with respect to the weights and biases of the respective layer as in During the backward pass, we calculate the partial derivatives of the loss

$$\nabla_{\mathbf{w}_{f}^{(\ell)}} \mathcal{L} = \sum_{\mathbf{u}, \mathbf{v}} \left(\nabla_{\mathbf{x}_{f}^{(\ell+1)}} \mathcal{L} \right)_{\mathbf{u}\mathbf{v}} \left(\mathbf{x}_{\mathbf{u}\mathbf{v}}^{(\ell)} * \hat{\mathbf{w}}_{f}^{(\ell)} \right)$$

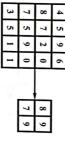
$$\nabla_{\mathbf{b}_{f}^{(\ell)}} \mathcal{L} = \sum_{\mathbf{u}, \mathbf{v}} \left(\nabla_{\mathbf{x}_{f}^{(\ell+1)}} \mathcal{L} \right)$$

where, we denotes a spatially flipped filter in order to compute the cross-

0.31. What do you mean by pooling layer? Explain

periodically insert a pooling layer in between successive convolutional layers. network, and hence to also control overfitting. It is common practice to representation to reduce the amount of parameters and computation in the is a form of non-linear downsampling. The pooling layer partitions the input function of the pooling layer is to progressively reduce the spatial size of the mean of the activations in the previous layer rather than the maximum. The the maximum activation, hence the name max-pooling as shown in fig. 5.18 Another common pooling operation is average pooling, which computes the volume into a set of non-overlapping rectangles and, for each subregion, outputs Ans. Another important concept of convolutional networks is pooling, which





(a) Global

(b) Local

Fig. 5.18 Max-pooling Layer

previous activations is computed as in During the forward pass, the maximum of non-overlapping regions of the

$$\mathbf{x}^{(\ell)} = \max_{\mathbf{u}, \mathbf{v}} \left(\mathbf{x}^{(\ell-1)} \right)_{\mathbf{u}\mathbf{v}}$$

width and height. where u and v denote the spatial extent of the non-overlapping regions in

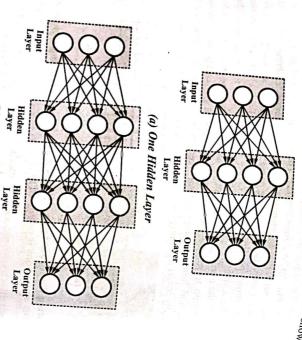
its origin during back propagation. the index of the maximum activation so that the gradient can be routed towards in case of the max-pooling operation, it is common practice to keep track of backward pass is merely an upsampling operation of the upstream derivatives. Since the pooling layer does not have any learnable parameters, the

the amount of downsampling to be performed. they have to be chosen in accordance to each other, they can be interpreted as The hyperparameters of the pooling layer are its stride and filter size. Since

Q.32. What is fully connected layer? Discuss its limitation.

convolutional neural network and is therefore typically inserted after the convolutional layers. The neurons have full connections to all activations in network. It is sometimes referred to as linear or affine layer. Intuitively, the fully connected layer is responsible for the high-level reasoning in a network literature and is equivalent to a hidden layer in a regular artificial Ans. The fully connected layer is a synonym often used in the convolutional

the previous layer, as seen in a regular artificial neural network as shown in



(b) Two Hidden Layers

Fig. 5.19 Fully Connected Layers in an Artificial Neural Network

product of the weights with the previous layer activations followed by a bias The activations of a fully connected layer can be computed with a dot

$$\mathbf{x}^{(\ell)} = (\mathbf{w}^{(\ell)})^{\mathrm{T}} \mathbf{x}^{(\ell-1)} + \mathbf{b}^{(\ell)}$$

 $oldsymbol{b}^{(\ell)}$ denote the activations, weights and biases of the current layer, respectively. where $\mathbf{x}^{(\ell-1)}$ denotes the activations of the previous layer and $\mathbf{x}^{(\ell)}$, $\mathbf{w}^{(\ell)}$, and

biases are computed as in During the backward pass, the gradient with respect to the weights and

$$\nabla_{\mathbf{w}}(\ell) \mathcal{L} = (\mathbf{x}^{(\ell)})^{\mathrm{T}} (\nabla_{\mathbf{x}}(\ell+1) \mathcal{L})$$

$$\nabla_{\mathbf{b}}(\ell) \mathcal{L} = \sum_{i=1}^{n} (\nabla_{\mathbf{x}}(\ell+1) \mathcal{L})_{i}^{\mathrm{T}}$$

where $\nabla_{\mathbf{x}}(\ell+1)$ denotes the upstream derivatives.

Q.33. What is machine learning?

experience. Here, learning means recognizing and understanding the input data the systems in such a way that they automatically learn and improve with Ans. Machine learning is a branch of science that deals with programming

statistics, probability theory, logic, combinatorial optimization, search, knowledge from specific data and past experience with the principles of To tackle this problem, algorithms are developed. These algorithms build It is very difficult to cater to all the decisions based on all possible inputs.

The developed algorithms from the basis of various applications such as-

- Vision processing
- (iv) Pattern recognition

(vi) Data mining (viii) Robotics.

- (v) Games

Ans. The different types of machine learning are shown in fig. 5.20. Q.34. Write and explain different types of machine learning.

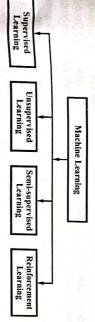


Fig. 5.20 Types of Machine Learning

provided with a given set of inputs with their desired outputs. The machine (i) Supervised Learning - In this type of learning, the machine is

neurons the input connects to, i.e. how many learnable parameters connect The only hyperparameter in a fully connected layer is the number of output

the input to the output.

connected layers do not scale well to high dimensional data such as images spatial structure of images has to be taken into account. Additionally, fully that are close together have the tendency to be highly correlated and thus the ince each pixel of the input has to be connected to the layer's output with a pixels and contributes equally to the predictive performance. However, pixels input feature, i.e. pixel in the image, is completely independent of neighbouring The main limitation of the fully connected layer is the assumption that each

and making wise decisions based on the supplied data.

reinforcement learning and control theory.

(II) Language processing

- (iii) Forecasting (e.g., stock market trends)

- (vii) Expert systems

needs to study those given sets of inputs and outputs and find a general function

In this learning the data are divided into different clusters and hence the learning 'learned by its own' by discovering and adopting, based on the input pattern, as divided into different clusters and hence the learner in the (ii) Unsupervised Learning - This type of learning is termed as

training process. Early examples of this include identifying a person's face on when the cost associated with labeling is too high to allow for a fully labeled classification, regression and prediction. Semi-supervised learning is useful for training. This type of learning can be used with methods such as applications as supervised learning. But it uses both labeled and unlabeled data (iii) Semi-supervised Learning - This fearning is used for the same

which actions yield the greatest rewards. With reinforcement learning, the algorithm discovers through trial and error time. Reinforcement learning is often used for robotics, gaming and navigation learning process ensures less participation of human expertise and saves more with the objective to maximize the efficiency (performance). This continual machine is trained to take specific decisions based on the business requirement (iv) Reinforcement Learning (RL) - In this type of learning

Q.35. Write the advantages of machine learning.

decision making engine for your problem. As you collect more data, the Ans. The five advantages of machine learning are as follows -Accurate - Machine learning uses data to discover the optimal

embed machine learning directly into an automated workflow. learning model can learn new patterns automatically. This allows users to (ii) Automated - As answers are validated or discarded, the machine

scales to handle increased data rates. Some machine learning algorithms can scale to handle large amounts of data on many machines in the cloud. own data, and can be configured to optimize whatever metric drives your business. with machine learning. Machine learning models are custom built from your milliseconds as new data streams in, allowing systems to react in real time. (v) Scalable - As your business grows, machine learning easily (iv) Customizable - Many data-driven problems can be addressed (iii) Fast - Machine learning can generate answers in a matter of

Q.36. Write the disadvantages of machine learning.

Ans. The disadvantages of machine learning are as follows -

based on different algorithms data need to be processed. And, it must be (i) Machine learning has the major challenge called acquisition. Also

> significant impact on results to be achieved or obtained processed before providing as input to respective algorithms. Thus, it has a

major challenge. That need to determine the effectiveness of machine learning (ii) As we have one more term interpretation. That it result is also a

some understanding of the problem at hand to apply the right algorithm. As we have seen that in most cases machine learning fails. Thus, it requires having any surety that it's algorithms will always work in every case imaginable. (iii) We can say uses of machine algorithm is limited. Also, it's not

errors. Brynjolfsson and McAfee said that the actual problem with this inevitable fact. That when they do make errors, diagnosing and correcting them can be of data. Fortunately, there are a lot of training data for image recognition purposes. raining data. As we can say it might be cumbersome to work with a large amount (v) One notable limitation of machine learning is its susceptibility to (iv) Like deep learning algorithm, machine learning also needs a lot of

Q.37. Explain the applications of machine learning.

difficult. As because it will need going through the underlying complexities.

very large data set. analysis software trained to very high accuracy using machine learning over a Over 85% of handwritten mail in the US is sorted automatically, using handwriting US Post Office to automatically sort letters containing handwritten addresses. application of computer vision trained using machine learning is its use by the systems are more accurate than hand-crafted programs. One massive-scale of cells, are developed using machine learning, again because the resulting recognition systems, to systems that automatically classify microscope images Ans. (i) Computer Vision - Many current vision systems, from face

training in a speaker-dependent fashion). phase after the user purchases the software (to achieve greater accuracy by involve two distinct learning phases - one before the software is shipped to program it by hand. In fact, many commercial speech recognition systems recognition accuracy is greater if one trains the system, then if one attempts (training the general system in a speaker-independent fashion), and a second train the system to recognize speech. The reason is simple - the speech for speech recognition all use machine learning in one fashion or another to (ii) Speech Recognition - Currently available commercial systems

symptoms and their geographical distribution. Current work involves adding in the profile of typical admissions so that it can detect anomalous patterns of project involves real-time collection of admissions reports to emergency rooms track disease outbreaks now use machine learning. For example, the RODS across western Pennsylvania, and the use of machine learning software to learn (iii) Bio-surveillance - A variety of government efforts to detect and

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a rich set of additional data, such as retail purchases of over-the-counter medicines to increase the information flow into the system, further increasing the need for the system more complex data set automated learning methods given this even more complex data set.

data consisting of terrain seen initially in the distance, and seen later up close. refine its ability to detect distant objects (training itself from self-collected strategies for stable helicopter flight and helicopter aerobatics. The recent 100 miles in the desert was won by a robot that used machine learning to Darpa-sponsored competition involving a robot driving autonomously for over researchers have demonstrated the use of machine learning to acquire control successfully used in a number of robot systems. For example, several (iv) Robot Control - Machine learning methods have been

recognition, entity recognition, automatic translation, and summarization. easily and smartly. By using NLP developer can perform tasks such as speech It is a better way to analyze, understand and find the meaning of human language other document sets, trying to discover new patterns or to root out corruption. in gathering new possibilities. It is mostly seen in a large pool of legislation or both computer understanding and manipulation of human language and its good (v) Natural Language Processing - It is a field that which involves

prediction and diagnosis is achieved by helping radiologists to make intellectual can be predicted by hospitals to spread expertise which is in short supply. Disease decisions with radiology data (for example – CT, MRI and Radiographs). Proprietary predictive model is used to make predictions such as admissions weight and problematic scenarios, etc. Natural language processing is a technique used for system to read the physician's notes and convert it to digital data. independent even associating each with some attribute information like age, Discrete event simulation is a technique where patients are modeled as an

Q.38. What are machine learning tools? Explain.

tools can automate each step in the applied machine learning process by Machine learning tools make applied machine learning faster, easier. Good choosing the right tool can be as important as working with the best algorithms. data into actionable information. Tools are a big part of machine learning and Ans. Machine learning gives a set of tools that use computers to transform

The machine learning tools are as follows -

- learning project. project from beginning to end. Platforms - Platforms are used to complete machine learning Provide capabilities required at each step in a machine
- (b) The interface may be graphical or command line.
- They provide a lose coupling of features.
- rather than speed, scalability or accuracy. They are provided for general purpose use and exploration

(ii) Library - Library gives capabilities for completing part of a

machine learning project. machine learning project. (a) Provide a specific capability for one or more steps in a

interface requiring programming. (b) The interface is typically an application programming (c) They are tailored for a specific use case, problem type or

environment.

(iii) Graphical User Interfaces -

(a) Allows less-technical users to work through machine

learning. (c) Stronger focus on graphical presentations of information (b) Focus on process and how to get the most from machine

learning techniques.

such as visualization.

(d) Structured process imposed on the user by the interface.

(iv) Command Line Interface -

through machine learning projects. (a) Allows technical users who are not programmers to work

and output to be generated. (b) Frames machine learning tasks in terms of the input required

(c) Promotes reproducible results by recording or scripting

commands and command line arguments. (v) Application Programming Interfaces -

(a) To incorporate machine learning into our own software projects.

(c) Gives the flexibility to use our own processes and (b) To create our own machine learning tools

automations on machine learning projects. (d) Allows combining our own methods with those provided

by the library as well as extending provided methods. (vi) Local Tools - Local tools can be downloaded, installed and run

on local environment.

(b) Control over run configuration and parameterization.(c) Integrate into our own systems to meet our needs. (a) Customized for in-memory data and algorithms.

(vii) Remote Tools - Remote tools can be hosted on a server and

called from local environment. These tools are often referred to as machine learning as a service (MLaaS).

